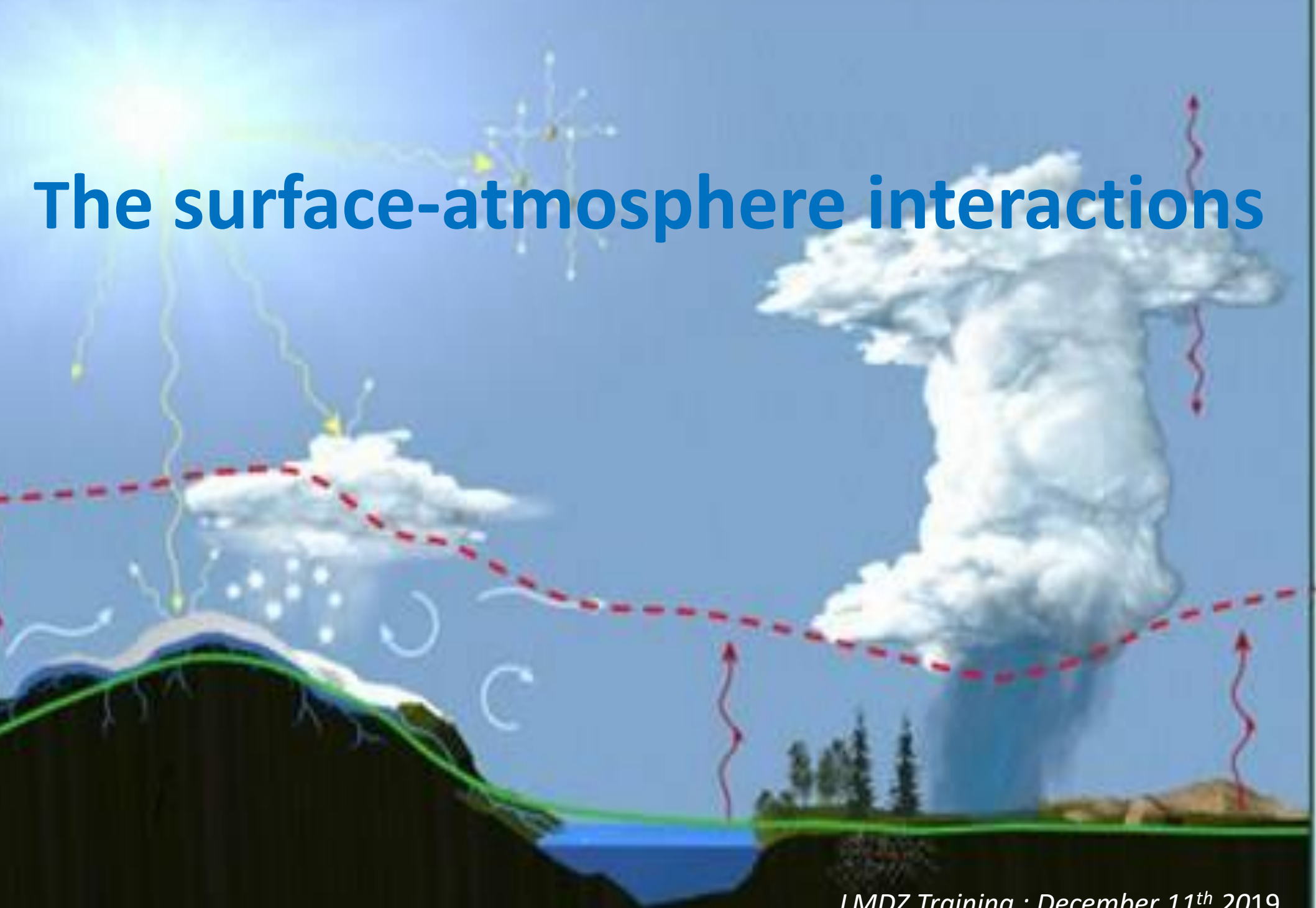


# The surface-atmosphere interactions



# Why the surface atmosphere interactions are important ?

- To describe the climate = One needs to describe interactions between Ocean-Atmosphere-Ice caps-land surfaces under the external solar forcing and the modified atmospheric composition (CO<sub>2</sub>, aerosols, CH<sub>4</sub> .. )
- First order Ocean-Atmosphere interactions dominate (exchange of heat, moisture ..)
- The land-surface interactions are essential for the high frequency variability of near surface meteorology, can strongly modulate the regional climates, impact the hydrological cycle...
- Partially control climate hazards: Heat waves, droughts ... and their consequences e.g famines

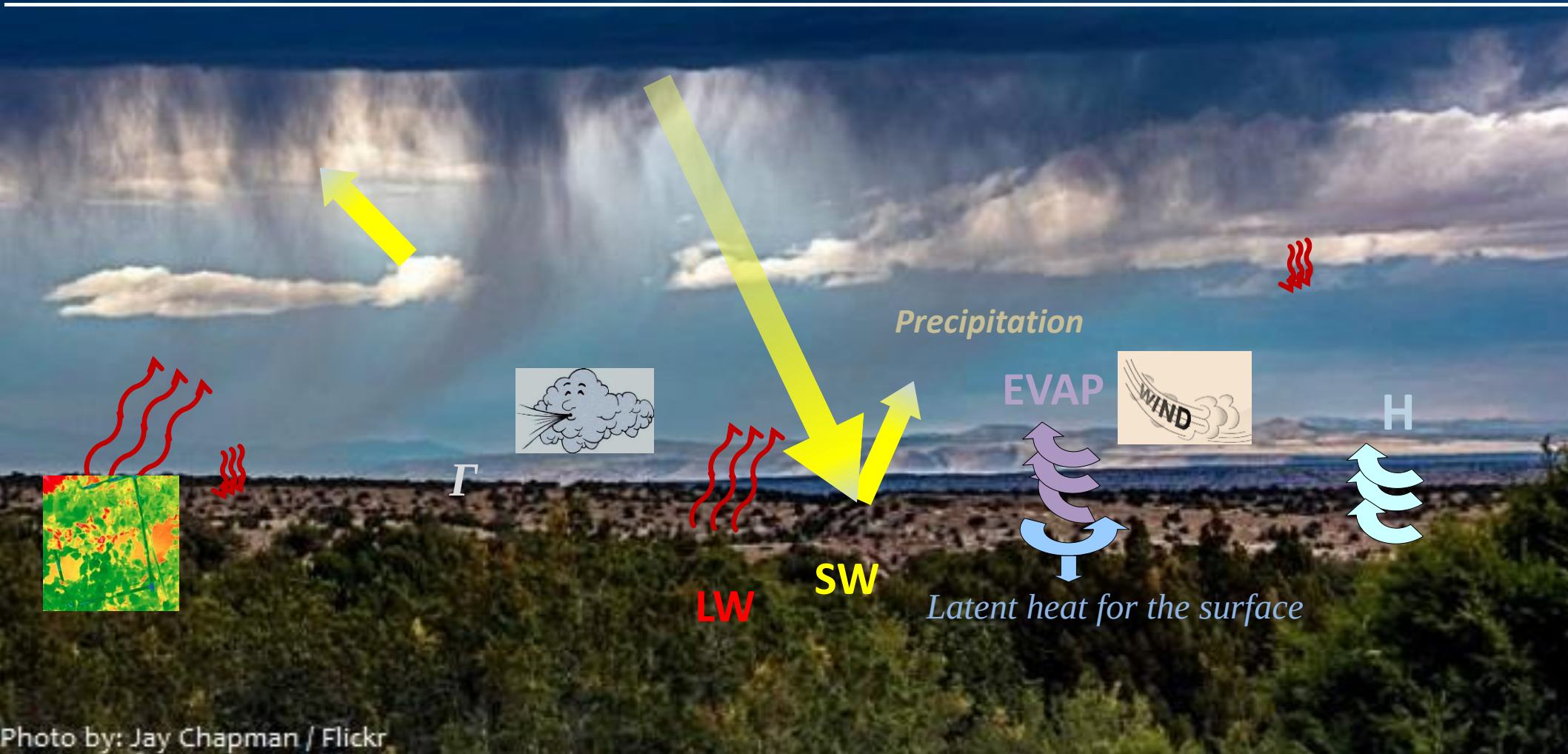


Photo by: Jay Chapman / Flickr

The **atmosphere and the surface are coupled** through *turbulence* (in boundary layer) and *radiation* (SW and LW). Currently, there is no direct influence of the surface to other parametrizations. The surface “receive” precipitation from the atmosphere (no direct feedback).

# Atmosphere-surface interactions

The **atmosphere and the surface are coupled** through *turbulence* (in the boundary layer) and *radiation* (SW and LW). Currently, there are no direct influence of the surface to other parametrizations.

The surface “receive” precipitation from the atmosphere (no direct feedback).

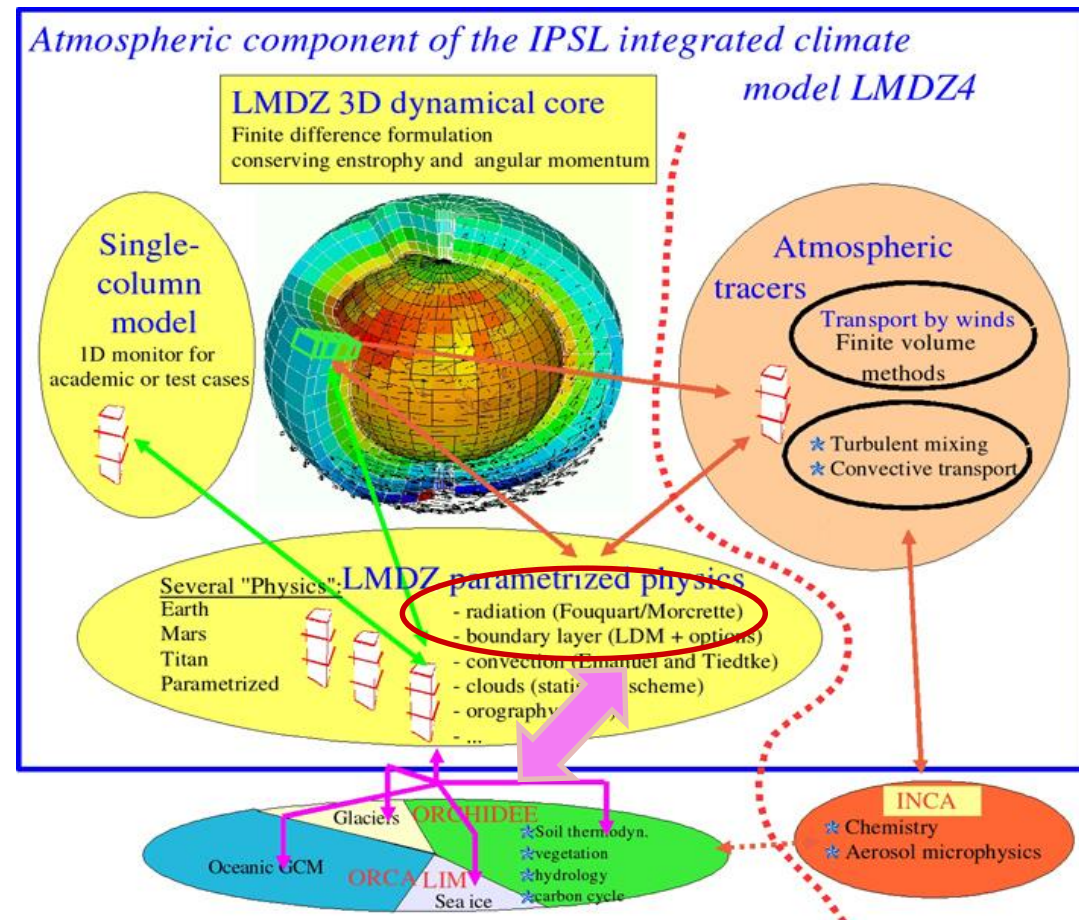
The surface impacts the atmosphere via the orography (factors constant with time), roughness, albedo emissivity

In LMDZ:

Each surface grid can be decomposed in a Maximum of 4 sub-grid of different type: land (\_ter), continental ice (\_lic), open ocean (\_oce) and sea\_ice (\_sic)

**Radiation** at the surface depends on mean surface properties (albedo, emissivity)

**Turbulent diffusion** depends on local sub-grid properties but each sub-surface sees the same atmosphere



## Turbulent diffusion (pbl\_surface)

**Change of a variable X with the time due to the turbulent transport (continuity) :**

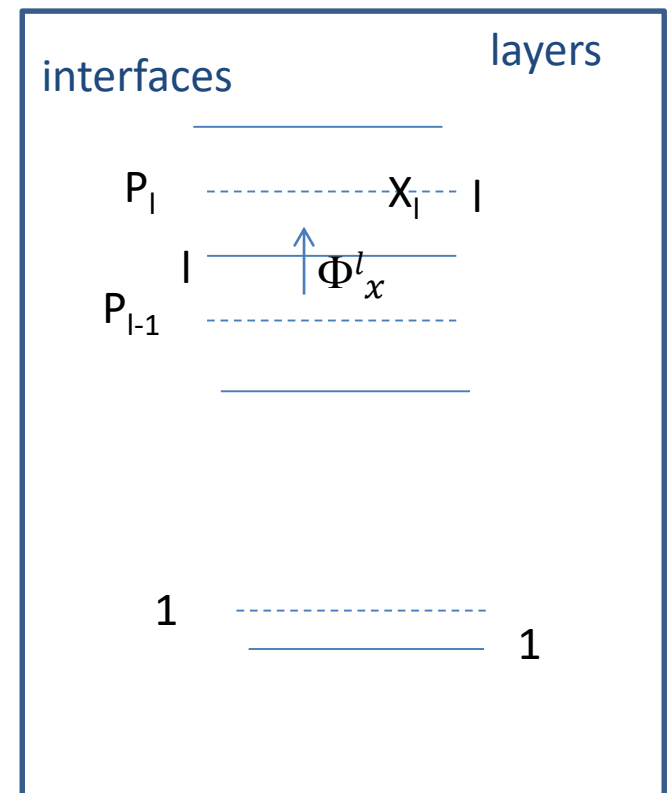
$$\frac{\partial X}{\partial t} = -\frac{1}{\rho} \frac{\partial \Phi}{\partial z} = -\frac{\partial \Phi}{m_l} \quad \begin{array}{l} m_l = \text{mass per surface unit (kg/m}^2\text{)} \\ X = \text{specific humidity, momentum,} \\ \text{moist static energy, tracers} \end{array}$$

$$\Phi = -\rho k_z \frac{\partial X}{\partial z} \quad \begin{array}{l} k_z \text{ Diffusion coefficient (m}^2\text{s}^{-1}\text{)} \\ \Phi: \text{upward positive} \end{array}$$

- Vertical discretization

$$\Phi^l = -K_l (X_l - X_{l-1})$$

$$\delta P = (P_{l-1} - P_l) = \rho g \delta z = m_l g \quad K_l = \frac{k_z \rho^2 g}{P_{l-1} - P_l}$$



$$\Phi_x^l = -K_l (X_l - X_{l-1})$$

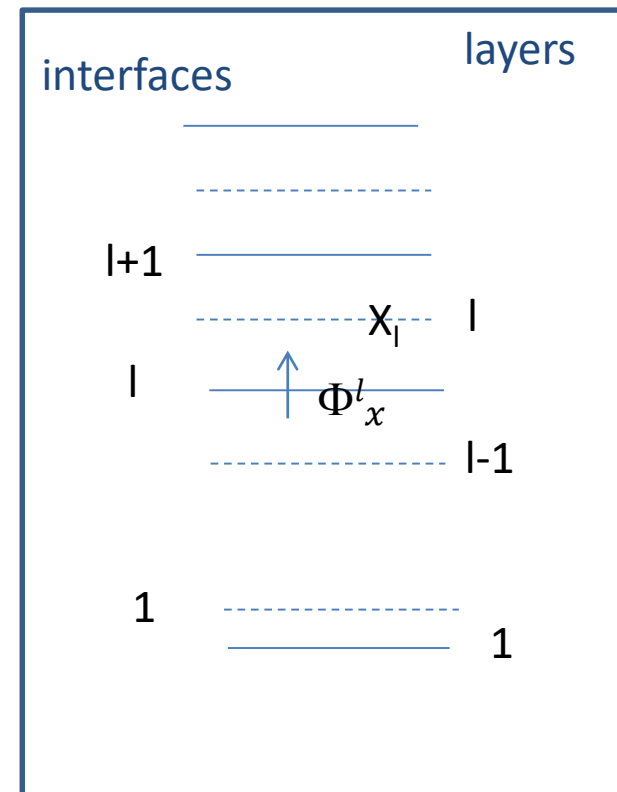
$$m_l \frac{X_l(t + \delta t) - X_l(t)}{\delta t} = \phi_l(t + \delta t) - \phi_{l+1}(t + \delta t)$$

$$m_l \frac{X_l - X_l^0}{\delta t} = \phi_l - \phi_{l+1} \quad \text{with} \quad \begin{array}{l} X_l = X_l(t + \delta t) \\ X_l^0 = X_l(t) \end{array}$$

$$m_l \frac{X_l - X_l^0}{\delta t} = K_{l+1}(X_{l+1} - X_l) - K_l(X_l - X_{l-1})$$

$$\left( \frac{m_l}{\delta t} + K_{l+1} + K_l \right) X_l = \frac{m_l}{\delta t} X_l^0 + K_{l+1} X_{l+1} + K_l X_{l-1}$$

$$-K_l X_{l-1} + \left( \frac{m_l}{\delta t} + K_{l+1} + K_l \right) X_l + K_{l+1} X_{l+1} = \frac{m_l}{\delta t} X_l^0$$



Tri-diagonal system that can be solved for the vector X

## Solving the tridiagonal system

$$\left(\frac{m_l}{\delta t} + K_{l+1} + K_l\right) X_l = \frac{m_l}{\delta t} X_l^0 + K_{l+1} X_{l+1} + K_l X_{l-1}$$

which may be written as:

$$\boxed{(\delta P_l + R_{l+1}^X + R_l^X) X_l = \delta P_l X_l^0 + R_{l+1}^X X_{l+1} + R_l^X X_{l-1}} \quad \underline{(2 \leq l < n)}$$

$$\text{with } R_l^X = g\delta t K_l$$

At the top ( $l=n, \Phi_n=0$ )

$$\boxed{(\delta P_n + R_n^X) X_n = \delta P_n X_n^0 + R_n^X X_{n-1}}$$

At the bottom: ( $l=1$ ):  $m_1 \frac{X_1 - X_1^0}{\delta t} = \Phi_x^1 - \Phi_x^2$

$$m_1 \frac{X_1 - X_1^0}{\delta t} = K_2(X_2 - X_1) - F_1^X$$

$$\boxed{(\delta P_1 + R_1^X) X_1 = \delta P_1 X_1^0 + R_2^X X_2 - g\delta t \underline{F_1^X}}$$

With  $F_1^X$ : flux of  $X$  at the bottom of the first layer (i.e. between the surface and the atmosphere), positive downward.

$$K_l = \frac{k_z \rho^2 g}{P_{l-1} - P_l}$$

## Solving the tridiagonal system

Starting from top:

$$(\delta P_n + R_n^X) X_n = \delta P_n X_n^0 + R_n^X X_{n-1}$$

can be written as:

$$X_n = C_n^X + D_n^X X_{n-1}$$

with

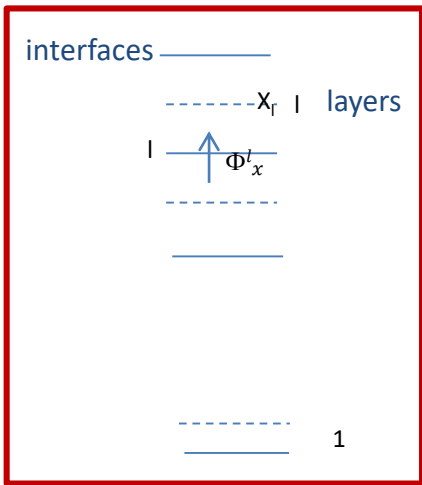
$$C_n^X = \frac{X_n^0 \delta P_n}{\delta P_n + R_n^X}$$

$$D_n^X = \frac{R_n^X}{\delta P_n + R_n^X}$$

with  $R_i^X = g\delta t K_i$



# Solving the tridiagonal system



$$X_{l+1} = C_{l+1}^X + D_{l+1}^X X_l$$

$$(\delta P_l + R_{l+1}^X + R_l^X) X_l = \delta P_l X_l^0 + R_{l+1}^X X_{l+1} + R_l^X X_{l-1} \quad (2 \leq l < n)$$

$$(\delta P_l + R_{l+1}^X (1 - D_{l+1}^X) + R_l^X) X_l = \delta P_l X_l^0 + R_{l+1}^X C_{l+1}^X + R_l^X X_{l-1}$$

with  $R_l^X = g\delta t K_l$

So we obtain by recurrence:

$$X_l = C_l^X + D_l^X X_{l-1} \quad (2 \leq l \leq n)$$

with, for  $(2 \leq l < n)$

depend only on properties in the layers above and the variables at the previous time step.

$$\left\{ \begin{aligned} C_l^X &= \frac{X_l^0 \delta P_l + R_{l+1}^X C_{l+1}^X}{\delta P_l + R_l^X + R_{l+1}^X (1 - D_{l+1}^X)} \\ D_l^X &= \frac{R_l^X}{\delta P_l + R_l^X + R_{l+1}^X (1 - D_{l+1}^X)} \end{aligned} \right.$$

## Solving the tridiagonal system

**At the bottom of the boundary layer**  $X_2 = C_2^X + D_2^X X_1$

$$(\delta P_1 + R_2^X) X_1 = \delta P_1 X_1^0 + R_2^X X_2 - g\delta t F_1^X$$

replacing  $X_2$  in the equation above:

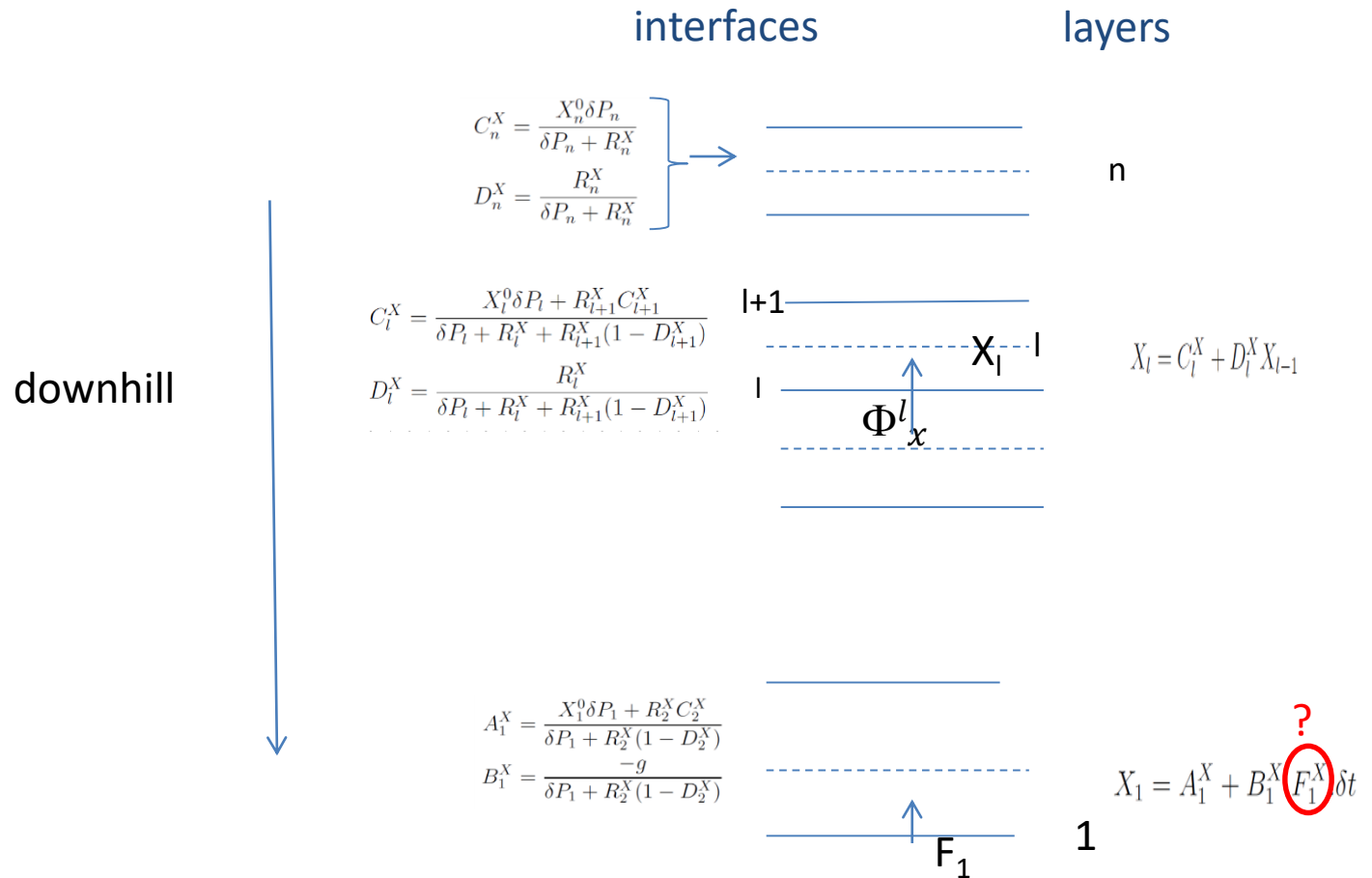
$$X_1 = A_1^X + B_1^X \cdot F_1^X \cdot \delta t$$

with

$$A_1^X = \frac{X_1^0 \delta P_1 + R_2^X C_2^X}{\delta P_1 + R_2^X (1 - D_2^X)}$$

$$B_1^X = \frac{-g}{\delta P_1 + R_2^X (1 - D_2^X)}$$

# Solving the tridiagonal system



$X$  = wind, enthalpie, specific humidity, tracers

$F_1^X$  (flux of water mass, flux of heat, flux of momentum) is either prescribed or computed for each sub-surface

Once  $F_1^X$  is known, the  $X_i$  can be computed from the first layer to the top of the PBL

# Coupling with the surface : compute $T_s$ and $F_1^T$ (sensible heat flux)

## Case of the continental surface and the temperature

- Heat conduction in the soil: Diffusion equation :

$$\left\{ \begin{array}{l} \Phi_T = -\lambda \frac{\partial T}{\partial z} \\ \frac{\partial T}{\partial t} = -\frac{1}{c} \frac{\partial \Phi_T}{\partial z} \end{array} \right. \quad \begin{array}{l} \lambda = \text{thermal diffusivity} \\ c = \text{thermal capacity} \end{array}$$

*Boundary conditions:*

- ✓ bottom :  $\Phi = 0$
- ✓ top: Continuity of the fluxes and the temperature between sub-surface and atmosphere

$$SW_{\text{net}} + LW_d - \underbrace{\varepsilon \sigma T_s^4 + H + L + \Phi_0}_{\text{depend on } T_s} = 0$$

$$L = \beta \rho C_p V C_d (q_s(T_s) - q_1) = \rho C_p V C_d (q_{\text{surf}} - q_1)$$

$$H = -\rho C_p V C_d (T_1 - T_s)$$

## Coupling with the surface : compute $T_s$ and $F_1^T$ (sensible heat flux)

### Case of the continental surface and the temperature

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$$(C) \begin{cases} \Phi_T = -\lambda \frac{\partial T}{\partial z} \\ \frac{\partial T}{\partial t} = -\frac{1}{c} \frac{\partial \Phi_T}{\partial z} \end{cases} \quad \begin{array}{l} \lambda = \text{thermal diffusivity} \\ C = \text{thermal capacity} \end{array}$$

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$$SW_{\text{net}} + LW_d - \underbrace{\varepsilon\sigma T_s^4 + H + L + \Phi_0}_{\text{depend on } T_s} = 0$$

$$H = \beta\rho VC_d (q_1 - q_s(T_s))$$

$$L = \rho VC_d (T_1 - T_s)$$

Vertical discretization and time discretization of C

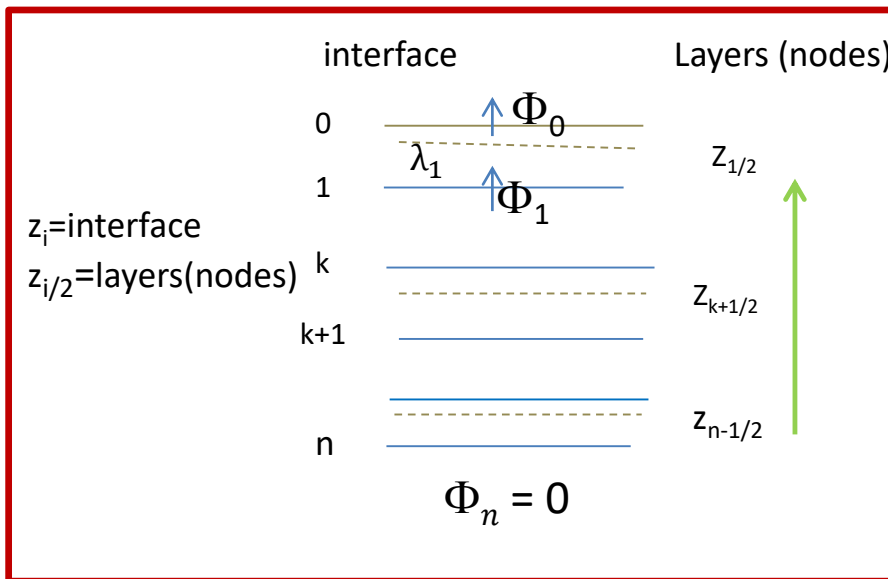
➤ Tridiagonal system as for the atmosphere (different boundary conditions)

- Heat conduction : Diffusion equation  $C \frac{\partial T}{\partial t} = \frac{\partial}{\partial z} \left( \lambda \frac{\partial T}{\partial z} \right)$

$$\Phi_T = -\lambda \frac{\partial T}{\partial z} ;$$

- Top: Continuity between sub-surface and atmosphere + vertical discretization  $\Phi_0 = Rad + \sum F^\downarrow(T_S^t) - \epsilon\sigma(T_S^t)^4$

$$C_{p1/2}^t \frac{T_{1/2}^t - T_{1/2}}{\delta t} = \frac{1}{z_1 - z_0} \left[ \lambda_1 \frac{T_{3/2}^t - T_{1/2}^t}{z_{3/2} - z_{1/2}} \right] + Rad + \sum F^\downarrow(T_S^t) - \epsilon\sigma(T_S^t)^4$$



- Intermediate layers

$$C_{pk+1/2}^t \frac{T_{k+1/2}^t - T_{k+1/2}}{\delta t} = \frac{1}{z_{k+1} - z_k} \left[ \lambda_{k+1} \frac{T_{k+3/2}^t - T_{k+1/2}^t}{z_{k+3/2} - z_{k+1/2}} - \lambda_k \frac{T_{k+1/2}^t - T_{k-1/2}^t}{z_{k+1/2} - z_{k-1/2}} \right]$$

- Bottom :  $\Phi = 0$   $C_{pn-1/2}^t \frac{T_{n-1/2}^t - T_{n-1/2}}{\delta t} = \frac{1}{z_N - z_{N-1}} \left[ -\lambda_{n-1} \frac{T_{n-1/2}^t - T_{n-3/2}^t}{z_{n-1/2} - z_{n-3/2}} \right]$

- Heat conduction : Diffusion equation

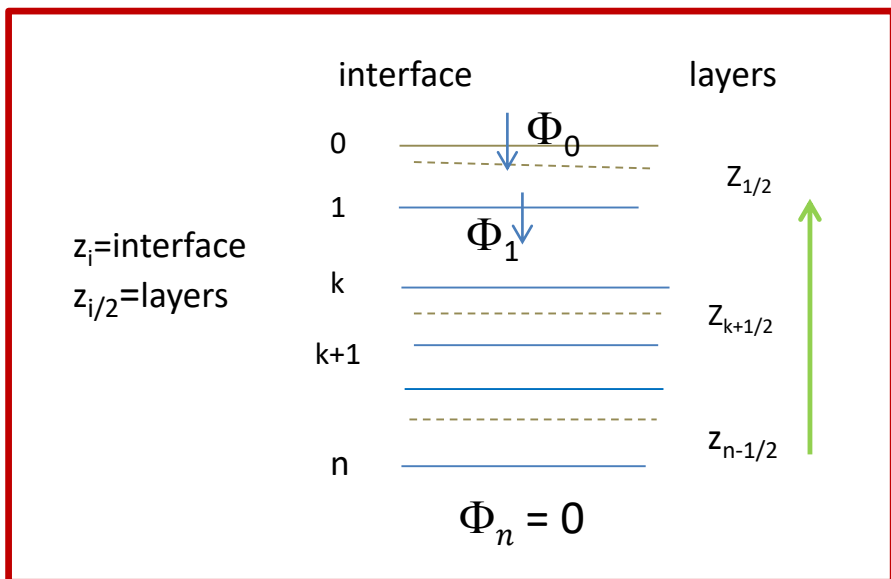
$$\Phi_T = -\lambda \frac{\partial T}{\partial z} ;$$

We obtain by recurrence (same as for atmosphere)

$$\frac{\partial T}{\partial t} = -\frac{1}{c} \frac{\partial \Phi_T}{\partial z}$$

- Top: Continuity between sub-surface and atmosphere**

$$C_p \frac{T_{1/2}^t - T_{1/2}}{\delta t} = \frac{1}{z_1 - z_0} \left[ \lambda_1 \frac{T_{3/2}^t - T_{1/2}^t}{z_{3/2} - z_{1/2}} \right] + Rad + \sum F^\downarrow(T_S^t) - \varepsilon \sigma (T_S^t)^4 \quad T_{3/2}^t = \alpha_1^t T_{1/2}^t + \beta_1^t$$



- Intermediate layers**

$$T_{k+1/2}^t = \alpha_k^t T_{k-1/2}^t + \beta_k^t$$

At  $t$ ,  $\alpha_k$  and  $\beta_k$  depend on  $T_{k1/2}$  at the previous time step they can be computed with a recurrence relationship from one layer to the other.

- Bottom** :  $\Phi_n = 0$

$$T_{n-1/2}^t = \alpha_{n-1}^t T_{n-3/2}^t + \beta_{n-1}^t$$

- Heat conduction : Diffusion equation

We obtain an inner relation

$$\Phi_T = -\lambda \frac{\partial T}{\partial z} ; \frac{\partial T}{\partial t} = -\frac{1}{c} \frac{\partial \Phi_T}{\partial z}$$

- Top: Continuity between sub-surface and atmosphere

$$(1) \quad C_{p1/2}^t \frac{T_{1/2}^t - T_{1/2}}{\delta t} = \frac{1}{z_1 - z_0} \left[ \lambda_1 \frac{T_{3/2}^t - T_{1/2}^t}{z_{3/2} - z_{1/2}} \right] + \Sigma F^\downarrow(T_S^t) - \epsilon \sigma (T_S^t)^4$$

$$(2) \quad T_{3/2}^t = \alpha_1^t T_{1/2}^t + \beta_1^t$$



- Heat conduction : Diffusion equation

We obtain by recurrence:

$$\Phi_T = -\lambda \frac{\partial T}{\partial z} ; \frac{\partial T}{\partial t} = -\frac{1}{c} \frac{\partial \Phi_T}{\partial z}$$

- Top: Continuity between sub-surface and atmosphere

$$(1) \quad C_p \frac{T_{1/2}^t - T_{1/2}^{t-1}}{\delta t} = \frac{1}{z_1 - z_0} \left[ \lambda_1 \frac{T_{3/2}^t - T_{1/2}^t}{z_{3/2} - z_{1/2}} \right] + Rad + \sum F^\downarrow(T_S^t) - \varepsilon \sigma (T_S^t)^4$$

$$(2) \quad T_{3/2}^t = \alpha_1^t T_{1/2}^t + \beta_1^t$$

$$C^* \frac{T_{1/2}^t - T_{1/2}^{t-1}}{\delta t} = G^* + Rad + \sum F^\downarrow(T_S^t) - \varepsilon \sigma (T_S^t)^4$$

$T_s$  : linearly extrapolated from  $T_{3/2}$  and  $T_{1/2}$

At  $t$ ,  $\alpha_k$  and  $\beta_k$  depend on  $T_{k1/2}$  at the previous time step they can be computed with a recurrence relation from one layer to the other.

$$C'^* \frac{T_s^t - T_s^{t-1}}{\delta t} = G' * + Rad + \sum F^\downarrow(T_S^t) - \varepsilon \sigma (T_S^t)^4$$

Hourdin 1993 (thèse)

Wang, Cheruy, Dufresne 2016 GMD

- Heat conduction : Diffusion equation

We obtain by recurrence:

$$\Phi_T = -\lambda \frac{\partial T}{\partial z} ; \frac{\partial T}{\partial t} = -\frac{1}{c} \frac{\partial \Phi_T}{\partial z}$$

- Top: Continuity between sub-surface and atmosphere

$$(1) \quad C_p \frac{T_{1/2}^t - T_{1/2}^{t-1}}{\delta t} = \frac{1}{z_1 - z_0} \left[ \lambda \frac{T_{3/2}^t - T_{1/2}^t}{z_{3/2} - z_{1/2}} \right] + Rad + \sum F^\downarrow(T_S^t) - \varepsilon \sigma (T_S^t)^4$$

$$(2) \quad T_{3/2}^t = \alpha_1^t T_{1/2}^t + \beta_1^t$$

$$C^* \frac{T_{1/2}^t - T_{1/2}^{t-1}}{\delta t} = G^* + Rad + \sum F^\downarrow(T_S^t) - \varepsilon \sigma (T_S^t)^4$$

$T_S$  : linearly extrapolated from  $T_{3/2}$  and  $T_{1/2}$

$$C'^* \frac{T_S^t - T_S^{t-1}}{\delta t} = G'^* + Rad + \sum F^\downarrow(T_S^t) - \varepsilon \sigma (T_S^t)^4$$

**Implicit equation for  $T_S$**

Hourdin 1993 (thèse)

Wang, Cheruy, Dufresne 2016 G

Solved using the sensitivity of the flux to the surface temperature to calculate the flux at the new time-step

At  $t$ ,  $\alpha_k$  and  $\beta_k$  depend on  $T_{k1/2}$  at the previous time step they can be computed with a recurrence relation from one layer to the other.

t-1

t

Downhill

$C_n^X D_n^X$

n

$C_l^X D_l^X$

l+1

l

$X_l$

$X_l = C_l^X + D_l^X X_{l-1}$

$\Phi_x^l$

$A_1^X B_1^X$

$X_1 = A_1^X + B_1^X \cdot F_1^X \delta t$

1

$F_1$

$T_s^{t-1}$

$\alpha^k, \beta^k$

At t  $\alpha_k$  and  $\beta_k$  depend on  $T_k$  at the previous time step and on the underlying layers :  
They can be pre-computed

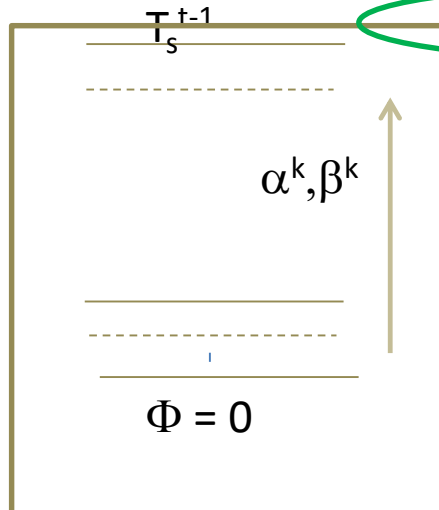
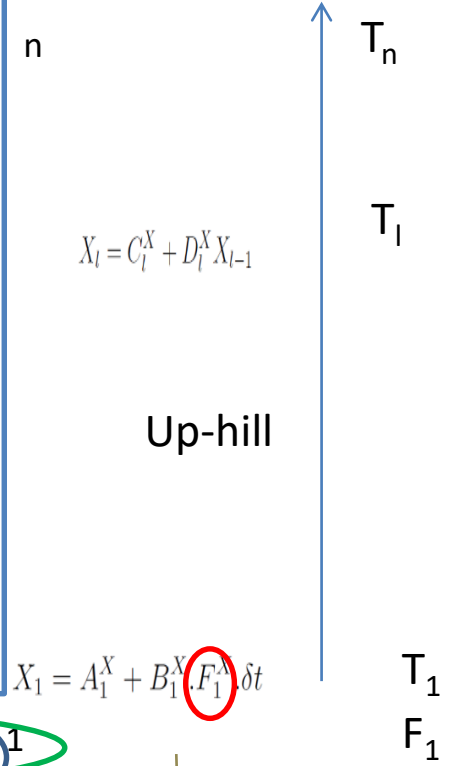
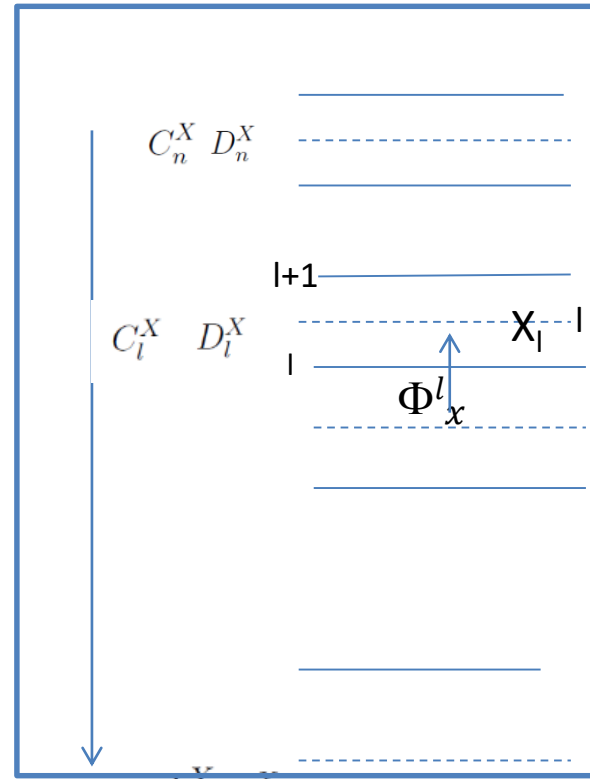
$\Phi = 0$

t-1

t

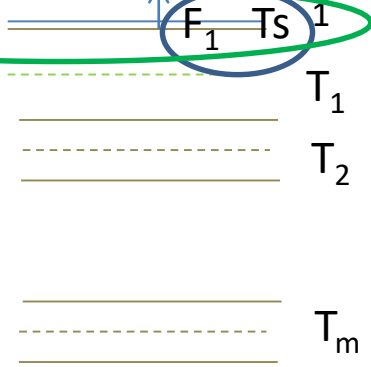
Down-hill

Up-hill



At t  $\alpha_k$  and  $\beta_k$  depend on  $T_k$  at the previous time step and on the underlying layers :  
They can be pre-computed

$$X_1 = A_1^X + B_1^X (F_1^A) \delta t$$

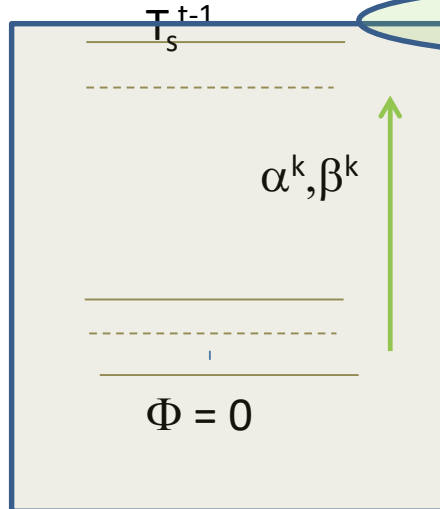
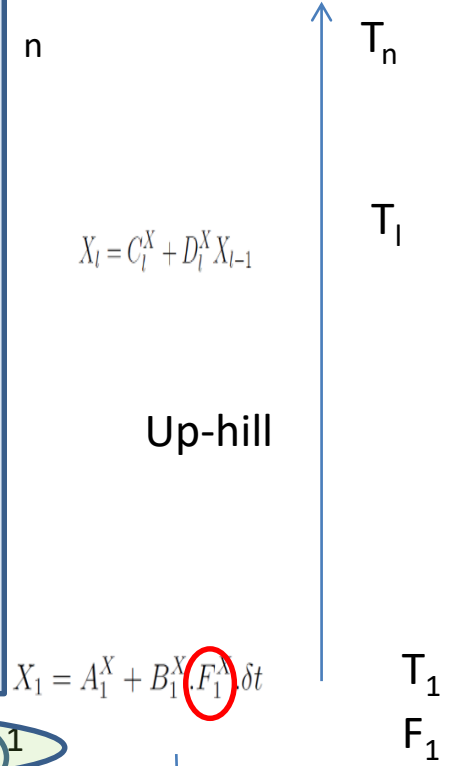
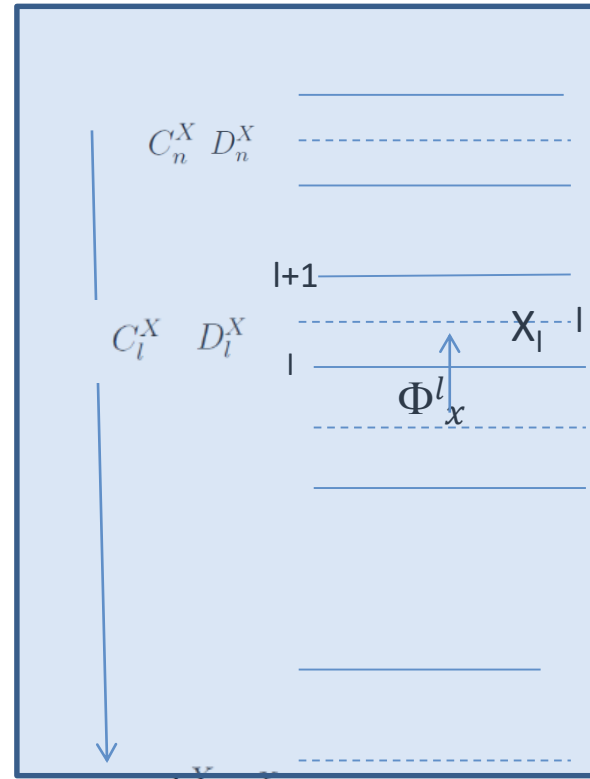


t-1

t

Down-hill

Up-hill



At t  $\alpha_k$  and  $\beta_k$  depend on  $T_k$  at the previous time step and on the underlying layers :  
They can be pre-computed

$$\Phi = 0$$

$$\alpha^k, \beta^k$$

$$X_l = C_l^X + D_l^X X_{l-1}$$

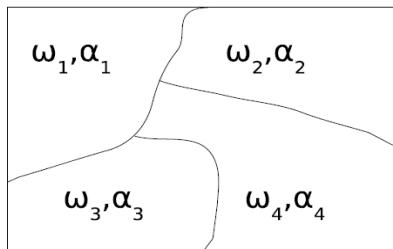
$$X_1 = A_1^X + B_1^X (F_1^A) \delta t$$

# Coupling between atmospheric column(s) and sub-surfaces

Each grid cell is divided into several sub-areas or "sub-surfaces" of fractions  $\omega_i$

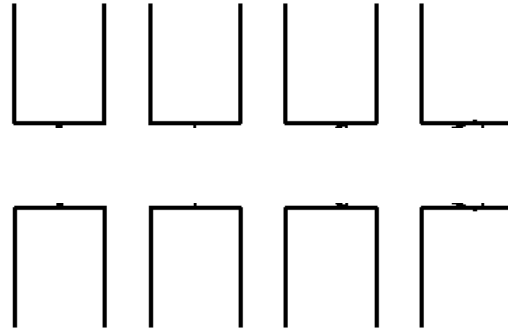
## Sub-surfaces

$$\sum_i \omega_i = 1$$



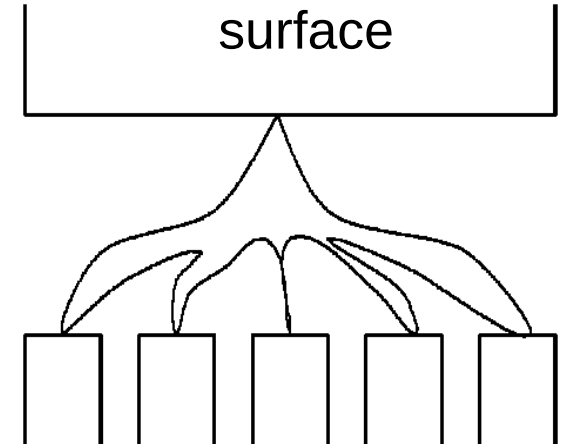
## Turbulent flux

One PBL over **each** sub-surface



## Radiative flux

One column **covers all** the sub-surface



**Each sub surface has to compute  $F_1$  using variables  $X_p$ ,  $A_1$  and  $B_1$**

The boundary layer tendencies in the atmosphere are mixed between sub-columns (equivalent of averaging the surface flux)

# Derivation of local sub-surface **net solar radiation** from grid average net solar radiation

The grid average net flux  $\Psi_s$  at surface has been computed for each grid point by the radiative code

We want (1) to conserve energy and (2) to take into account the value of the local albedo  $\alpha_i$  of the surface

We compute the downward SW radiation as

with the mean albedo

$$\alpha = \sum_i \omega_i \alpha_i \quad F_{\downarrow}^s = \frac{\Psi_s}{(1 - \alpha)}$$

**For each sub-surface  $i$** , the absorbed solar radiation reads:  $\psi_i^s = (1 - \alpha_i) F_{\downarrow}^s$

$$\psi_i^s = \frac{(1 - \alpha_i)}{(1 - \alpha)} \bar{\Psi}^s$$

One may verify that this procedure ensures energy conservation,  $\sum_i \omega_i \psi_i^s = \Psi_s$

# Derivation of local sub-surface **net longwave radiation** from grid average net longwave radiation

The net longwave (LW) radiation  $\bar{\Psi}^L$  has been computed by the radiative code for each grid cell. How to split it depending on the sub-surfaces local properties and ensuring energy conservation?

If the downward longwave flux  $F_{\downarrow}$  is uniform within each grid, the net LW flux for a sub-surface  $i$  may be written as:

$$\psi_i^L(T_i) = \epsilon_i (F_{\downarrow} - \sigma T_i^4) \quad (1)$$

where  $T_i$  is the surface temperature of sub-surface  $i$  and  $\epsilon_i$  its emissivity. A linearization around the mean temperature  $\bar{T}$  gives:

$$\psi_i^L(T_i) \approx \epsilon_i (F_{\downarrow} - \sigma \bar{T}^4) - 4\epsilon_i \sigma \bar{T}^3 (T_i - \bar{T}) \quad (2)$$

To conserve the energy, the following relationship must be true:

$$\sum_i \omega_i \psi_i^L = \bar{\Psi}^L \quad (3)$$

Using Eq. 2 gives

$$\sum_i \omega_i \psi_i^L = \bar{\epsilon} (F_{\downarrow} - \sigma \bar{T}^4) - 4\sigma \bar{T}^3 \sum_i \omega_i \epsilon_i (T_i - \bar{T}) \quad (4)$$

where  $\bar{\epsilon} = \sum_i \omega_i \epsilon_i$  is the mean emissivity.



# Derivation of local sub-surface **net longwave radiation** from grid average net longwave radiation

$$\sum_i \omega_i \psi_i^L = \bar{\epsilon} (F_{\downarrow} - \sigma \bar{T}^4) - 4\sigma \bar{T}^3 \sum_i \omega_i \epsilon_i (T_i - \bar{T}) \quad (4)$$

where  $\bar{\epsilon} = \sum_i \omega_i \epsilon_i$  is the mean emissivity. The second term on the right hand side is zero if

$$\bar{T} = \frac{\sum_i \omega_i \epsilon_i T_i}{\bar{\epsilon}} \quad (5)$$

To ensure energy conservation, we need in addition to verify:

$$\bar{\Psi}^L = \bar{\epsilon} (F_{\downarrow} - \sigma \bar{T}^4) \quad (6)$$

Which is consistent with the definition of the net LW flux at the surface. We rewrite now Eq. 2 as:

$$\psi_i^L(T_i) \approx \frac{\epsilon_i}{\bar{\epsilon}} \bar{\Psi}^L - 4\epsilon_i \sigma \bar{T}^3 (T_i - \bar{T}) \quad (7)$$

Due to radiative code limitation, in LMDZ, we always must have  $\epsilon_i = 1$

# Call tree

## In subroutine PHYSIQ

loop over time steps

CALL `change_srf_frac` : Update fraction of the sub-surfaces (pctsrfr)

....

**CALL `pbl_surface`** Main subroutine for the interface with surface

Calculate net radiation at sub-surface

*Loop over the sub-surfaces `nsrf`*

Compress variables (Consider only one surface type and only the points for which the fraction for this sub-surface is not zero)

CALL `cdrag`: coefficients for turbulent diffusion at surface (`cdragh` and `cdragm`)

CALL `coef_diff_turb`: coef. turbulent dif. in the atmosphere (`ycoefm` et `ycoefm.`)

CALL `climb_hq_down` downhill for enthalpy H and humidity Q

CALL `climb_wind_down` downhill for wind (U and V)

CALL `surface models` for the various surface types: **`surf_land`, `surf_landice`, `surf_ocean` or `surf_seaice`**. **Each surface model computes:**

- evaporation, latent heat flux, sensible heat flux
- surface temperature, albedo (emissivity), roughness lengths

CALL `climb_hq_up` : compute new values of enthalpy H and humidity Q

CALL `climb_wind_up` : compute new values of wind (U and V)

Uncompress variables : (some variables are per unit of sub-surface fraction, some are per unit of grid surface fraction)

Cumulate in global variables after weighting by sub-surface fractions

Surface diagnostics : (T, q, wind are evaluated at a reference level (2m) owing to an interpolation scheme based on the MO laws).

*End Loop over the sub-surfaces*

Calculate the mean values over all sub-surfaces for some variables

**End `pbl-surface`**

About the surface models: land, ocean, sea-ice , land-ice

For land : simplified land surface model, hydrology= bucket or “beta clim”,  
constant thermal inertia (soil /snow) , albedo and rugosity from a file.  
or Soil-vegetation-atmosphere transfer (SVAT) model (ORCHIDEE)

For ocean: Forced, fully coupled (with NEMO), coupled with a slab-ocean

For sea ice depends on the coupling with the ocean (forced, coupled, slab)

For land-ice : snow properties calculated with sisvat if ok\_snow= T.  
otherwise simplified (as for land + simplified snow prop., rugo, albedo)

About the values interpolated at a reference level near the surface (e.g. 2m)

Principle: Constant flux in the surface layer and similarity laws: Non dimensional vertical gradient of horizontal wind, potential temperature, specific humidity are assumed to be universal function of a stability parameter  $z/L$  ( $L$  = Monin-Obukhov law) or of the Richardson Number (Louis 82).

$$\frac{kz}{u_*} \frac{\partial u}{\partial z} = \phi_M\left(\frac{z}{L}\right) ; \quad \frac{kz}{\theta_*} \frac{\partial \theta}{\partial z} = \phi_H\left(\frac{z}{L}\right) ; \quad \frac{kz}{q_*} \frac{\partial q}{\partial z} = \phi_q\left(\frac{z}{L}\right)$$

Integrating these equations gives

$$\frac{kx}{u_*} = \ln\left(\frac{z}{z_0}\right) - \psi_H\left(\frac{z}{L}\right) + \psi_H\left(\frac{z_0}{L}\right)$$

$$\frac{k(\theta - \theta_0)}{\theta_*} = \ln\left(\frac{z}{z_0}\right) - \psi_H\left(\frac{z}{L}\right) + \psi_H\left(\frac{z_0}{L}\right)$$

Louis shows that one can use the Richardson (bulk) number instead of the monin Obukhov length

$$\frac{kx}{u_*} = \frac{\ln(z/z_0)}{F_M^{1/2}\left(R_b^b, \frac{z}{z_0}\right)}$$

$$\text{II} \quad \frac{k(\theta - \theta_0)}{\theta_*} = \frac{\ln\left(\frac{z}{z_0}\right)}{F_H\left(R_b^b, \frac{z}{z_0}\right)} F_M^{1/2}\left(R_b^b, \frac{z}{z_0}\right)$$

Louis shows that one can use the Richardson (bulk) number instead of the mean Ekman length

$$\frac{k u}{u_*} = \frac{\ln(z/z_0)}{F_M^{1/2}(R_i^b, \frac{z}{z_0})}$$

$$\text{II} \quad \frac{k(\theta - \theta_0)}{Q_*} = \frac{\ln\left(\frac{z}{z_0}\right)}{F_M(R_i^b, \frac{z}{z_0})}$$

if one writes II for 2 levels (first atm. level and reference level)

$$\frac{\theta_{ref} - \theta_0}{\theta_1 - \theta_0} = \frac{\ln\left(\frac{z_{ref}}{z_0}\right)}{\ln\left(\frac{z_1}{z_0}\right)} \cdot \frac{F_M^{1/2}\left(R_i^{ref}, \frac{z_{ref}}{z_0}\right)}{F_M^{1/2}\left(R_i^1, \frac{z_1}{z_0}\right)} \cdot \frac{F_M\left(R_i^1, \frac{z_1}{z_0}\right)}{F_M\left(R_i^{ref}, \frac{z_{ref}}{z_0}\right)}$$

$$\theta_0 = T_S$$

→ evaluate  $\theta_{ref} = f(\theta_2, \theta_1, \text{stability}, z_1, z_{ref}, R_i^1, R_i^{ref})$

$$\frac{q_{ref} - q_0}{q_1 - q_0} = \frac{\ln\left(\frac{z_{ref}}{z_0}\right)}{\ln\left(\frac{z_1}{z_0}\right)} \cdot \frac{F_M^{1/2}\left(R_i^{ref}, \frac{z_{ref}}{z_0}\right)}{F_M^{1/2}\left(R_i^1, \frac{z_1}{z_0}\right)} \cdot \frac{F_M\left(R_i^1, \frac{z_1}{z_0}\right)}{F_M\left(R_i^{ref}, \frac{z_{ref}}{z_0}\right)}$$

Some properties -

stability function in the stable case:  $\Psi_H\left(\frac{z}{L}\right) = -\frac{5}{L}$   
( $L > 0$ )

$$\frac{\theta - \theta_0}{\theta_*} = \frac{1}{k} \left[ \ln \frac{z}{z_0} + \frac{5z}{L} \right]$$

at  $z = z_0$ ,  $\theta_* = \text{cte}$  and does not depend on  $z$ .

$$\rightarrow \frac{d\theta}{dz} = \theta_* = \text{cte} = \text{function monotone of } z$$

For a stability:  $\theta_s \leq \theta \leq \theta_1$

In the unstable case:  $\frac{\theta - \theta_0}{\theta_*} = \ln\left(\frac{z}{z_0}\right) + 2 \ln\left[1 + \left(1 - \frac{16z}{L}\right)^{1/2}\right]$   
 $L < 0$

$\frac{d\theta}{dz}$  not always monotone -

$$F\left(\frac{z}{L}\right) = \frac{-16}{L} \cdot \frac{1}{\left(1 - \frac{16z}{L}\right)^{1/2} \left[1 + \left(1 - \frac{16z}{L}\right)^{1/2}\right]}$$

$$F\left(\frac{z}{L}\right) < 0$$

- Technical note : Description of the interface with the surface and the computation of the turbulent diffusion in LMDZ (J.L.Dufresne) Thèse F. Hourdin 1993 (section 3.3.3 and annexes)
- Wang F., F. Cheruy, J.L. Dufresne, 2016: The improvement of soil thermodynamics and its effects on land surface meteorology in the IPSL climate model. Geosci. Model Dev., 9, 363–381, 2016 [www.geosci-model-dev.net/9/363/2016/](http://www.geosci-model-dev.net/9/363/2016/)
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## Coupling with the surface : Compute $F_x^1$

$A_1$  and  $B_1$  rely on the vertical diffusion scheme

$$F_x^1 = \rho C_d^x |V| (X_1 - X_s) = \frac{X_1 - A_1}{B_1 \delta t}$$

$$X_1 = A_1^X + B_1^X \cdot F_1^X \cdot \delta t$$

Value of  $X_1$  if  $F_1=0$

Sensitivity of  $X_1$  to  $F_1$

$C_d^x$  drag coefficient (Monin Obukhov, constant flux in the surface layer) depends on

- roughness lengths (gustiness, vegetation), orography
- Richardson number (boundary layer stability)
- Formulation depends on the sub-surface type

Once  $X_s$  is known,  $X_1$  and  $F_x^1$  are known



## IMPLICIT SOLVING FOR $T_s$

$$C' * \frac{T_s^t - T_s}{\delta t} = G' * +Rad + \sum F^\downarrow(T_s^t) - \epsilon \sigma (T_s^t)^4$$

$$F_X^1 = \text{Bulk formula} = \rho C_d^x |V| (X_1 - T_s) = K_1 (X_1 - T_s)$$

$$F_X^1 = \frac{X_1 - A_1}{B_1 \delta t} = M_1 + N_1 T_s$$

$$X_1 = A_1^X + B_1^X \cdot F_1^X \cdot \delta t$$

Value of  $X_1$  if  $F_1=0$

Sensitivity of  $F_1$   
to  $X_1$

$$M_1 = \frac{K_1 A_1}{1 - \delta t K_1 B_1} \quad \pi = (P_0 / P_1)^k$$

$$N_1 = - \frac{\pi K_1 A_1}{1 - \delta t K_1 B_1}$$

$A_1$  and  $B_1$  known