

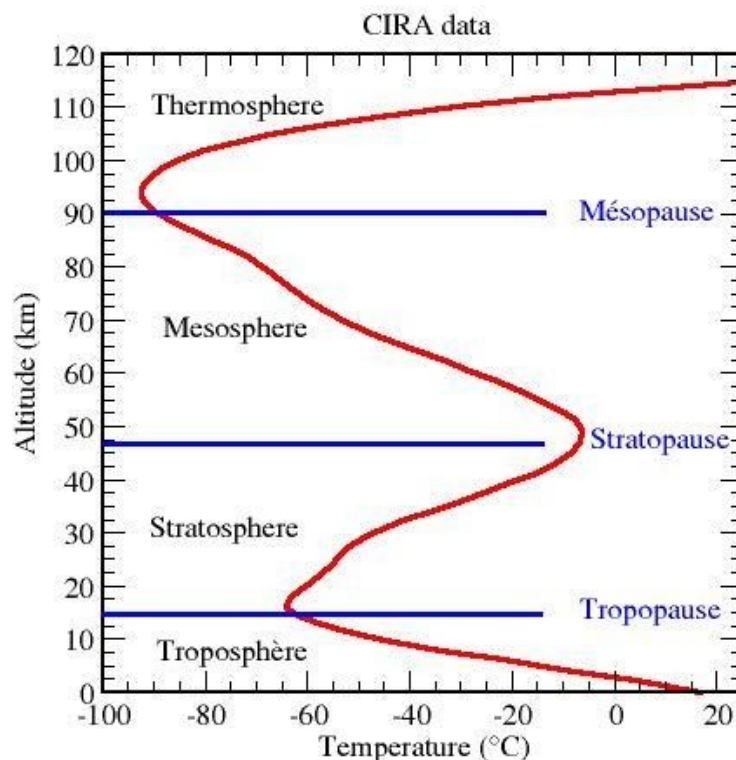
# General Circulation of the Stratosphere and modelisation

- a) Basic climatologies
- b) Interpretation of the dynamics with a heuristic model
- c) Brewer Dobson circulation
- d) Middle latitudes dynamics  
    Stratospheric sudden warmings
- e) Equatorial dynamics  
    Semi annual and quasi-biennial oscillations
- f) Convective gravity waves parameterization and impact in the tropics
- g) Frontal gravity waves parameterization and impacts in the midlatitudes

# General Circulation of the Stratosphere and modelisation

## a) Basic climatologies

Global average of Temperature as a function of altitude

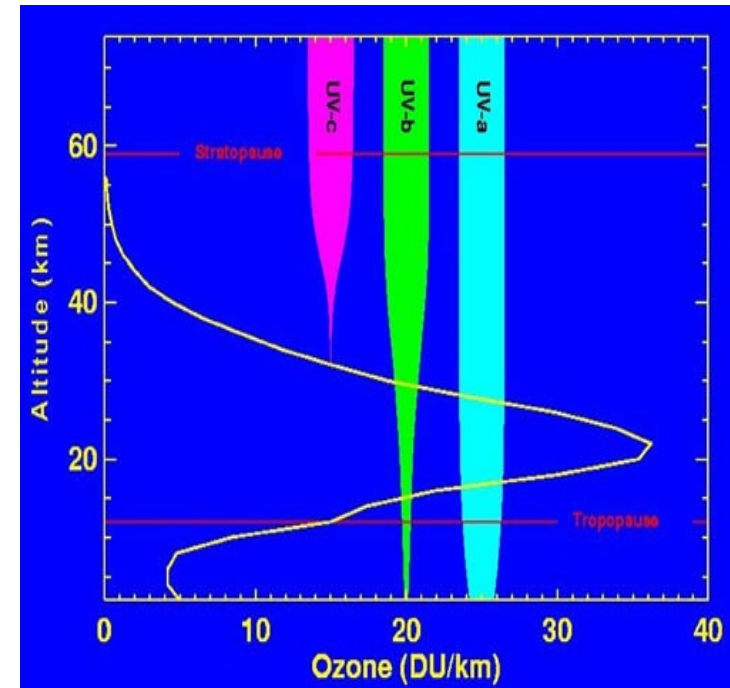


- CIRA data (1988): Rockets, radiosondes, satellites above 110km.
- Troposphere:  $T$  decreases with  $z^*$ , the heating comes from the surface, whereas the water vapor and clouds cool the atmosphere above via infrared emission (IR).
- The middle atmosphere:
  - contain 2 of the 3 layers of the neutral atmosphere: the stratosphere and the mesosphere.
  - The chemical major constituents are still well mixed
  - There is a Max in  $T$  at 50km due to  $O_3$ . This defines the stratopause separating the stratosphere and the mesosphere
- Above 90km lies the thermosphere, a layer highly exposed to sun radiation and the X-rays ionised the constituents. It contains the ionosphere (80-500km) where Aurora Borealis occur.
- Extremely thin in mass,  $T$  can vary from 600K to 1800K in one day.
- The atmosphere there is no longer neutral, is no longer well mixed: the composition varies according to the mass of the molecules because of the large distance between them.

# General Circulation of the Stratosphere and modelisation

## a) Basic climatologies

- Absorption of UV-b by O<sub>3</sub> is driving the middle atmosphere circulation



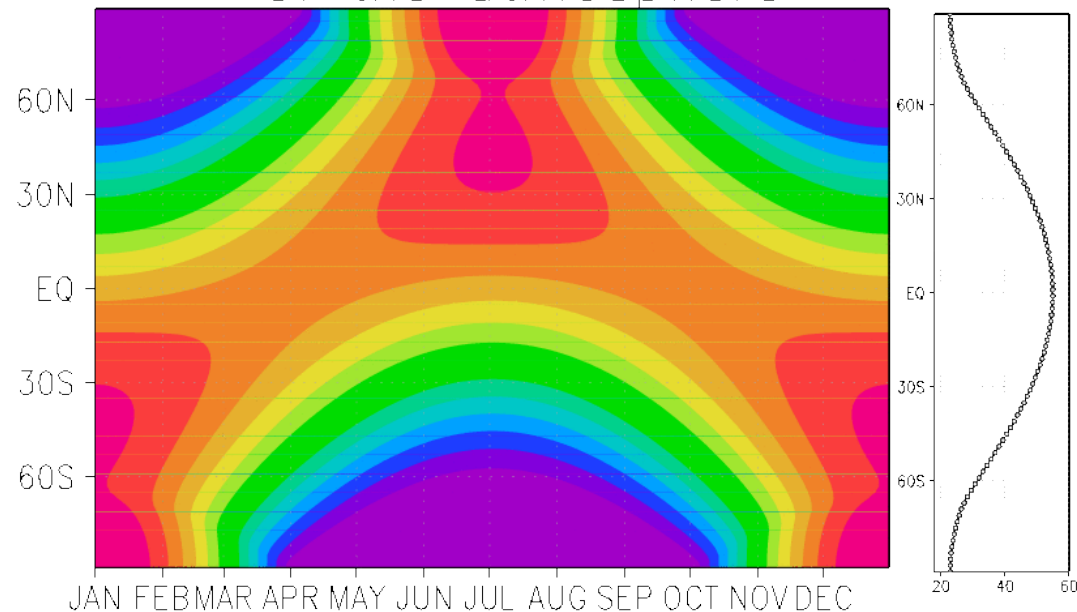
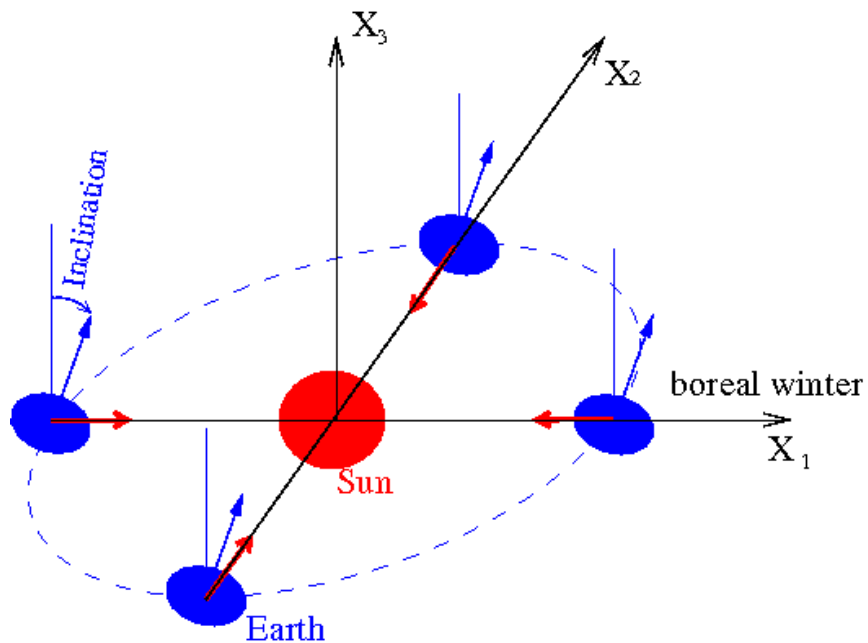
Profil d'Ozone aux moyennes latitude et  
Altitude de pénétration des UV-a, UV-b, UV-c

# General Circulation of the Stratosphere and modelisation

## a) Basic climatologies

Heating by ozone build-up the stratosphere above the stratosphere

Sunlight at the submit  
of the atmosphere



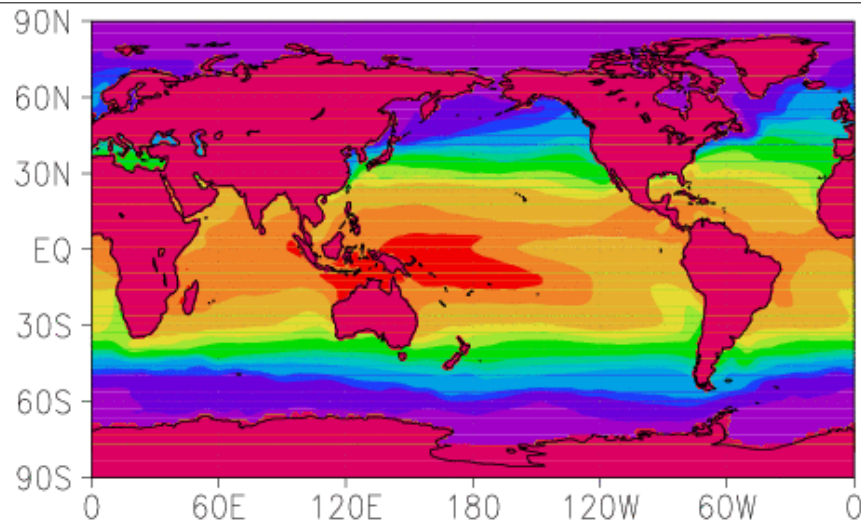
Ozone re-emit quasi immediatly, and through chemical heating the UV-radiation it absorbs ( $O+O_2 \rightarrow O_3$ )

The daily average sunlight is maximum at the pole in summer  
In mean over the year the sunlight stays maximum at the Equator

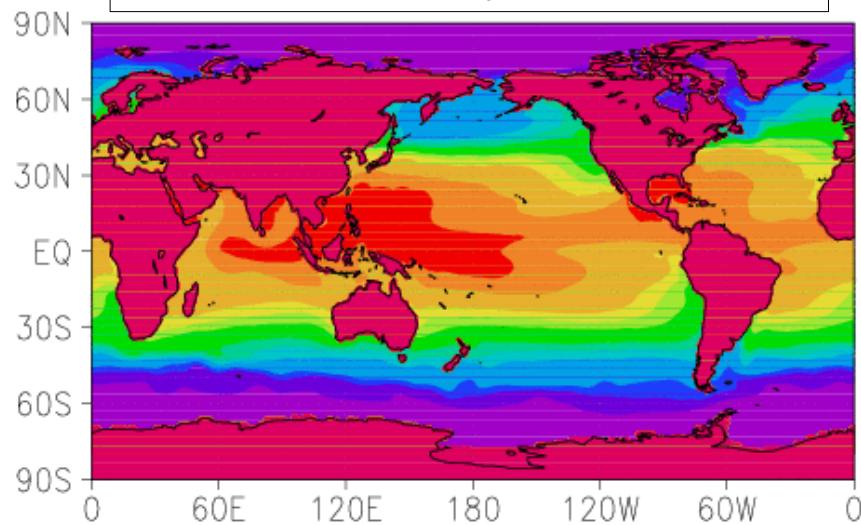
# General Circulation of the Stratosphere and modelisation

## a) Basic climatologies

Sea surface T in January  
ECMWF (1993-1997)



July



SST is always warmer in the tropical regions

It also maintain a high rate of humidity and therefore a strong greenhouse effect in the tropical regions

Troposphere is in first place forced by the bottom, and will therefore has an annual cycle much less dramatic than the middle atmosphere

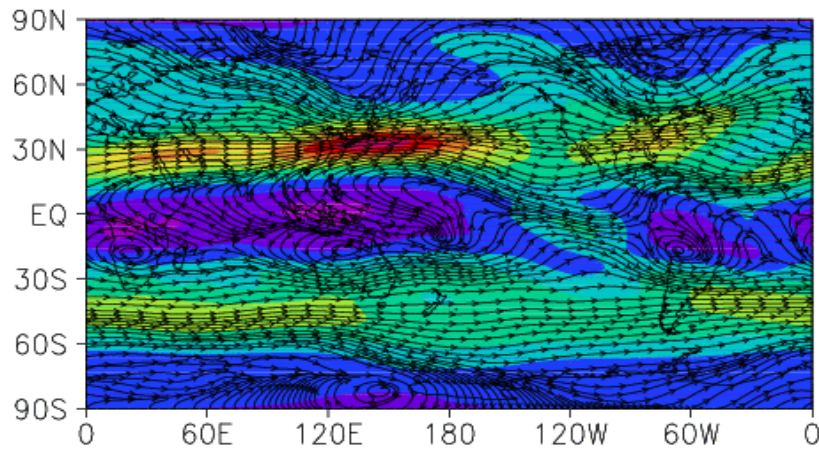
# General Circulation of the Stratosphere and modelisation

## a) Basic climatologies

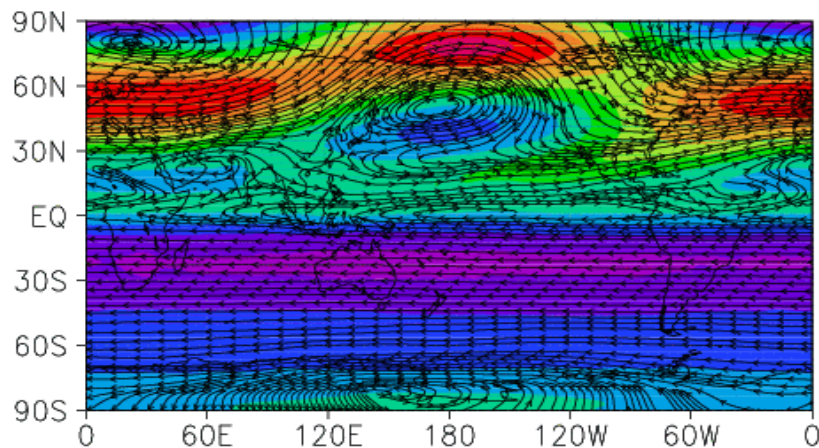
An extremely remarkable example of the difference between the general Circulations in the troposphere and in the stratosphere

ECMWF (93-97) winter wind

Tropopause (12km)



Stratosphere (40km)



Winter time mean climatologies:

- The winds in the troposphere are eastward in both hemisphere and in the mid-latitudes.
- In the stratosphere the winds are eastward in the winter hemisphere and westward in the summer hemisphere.



# General Circulation of the Stratosphere and modelisation

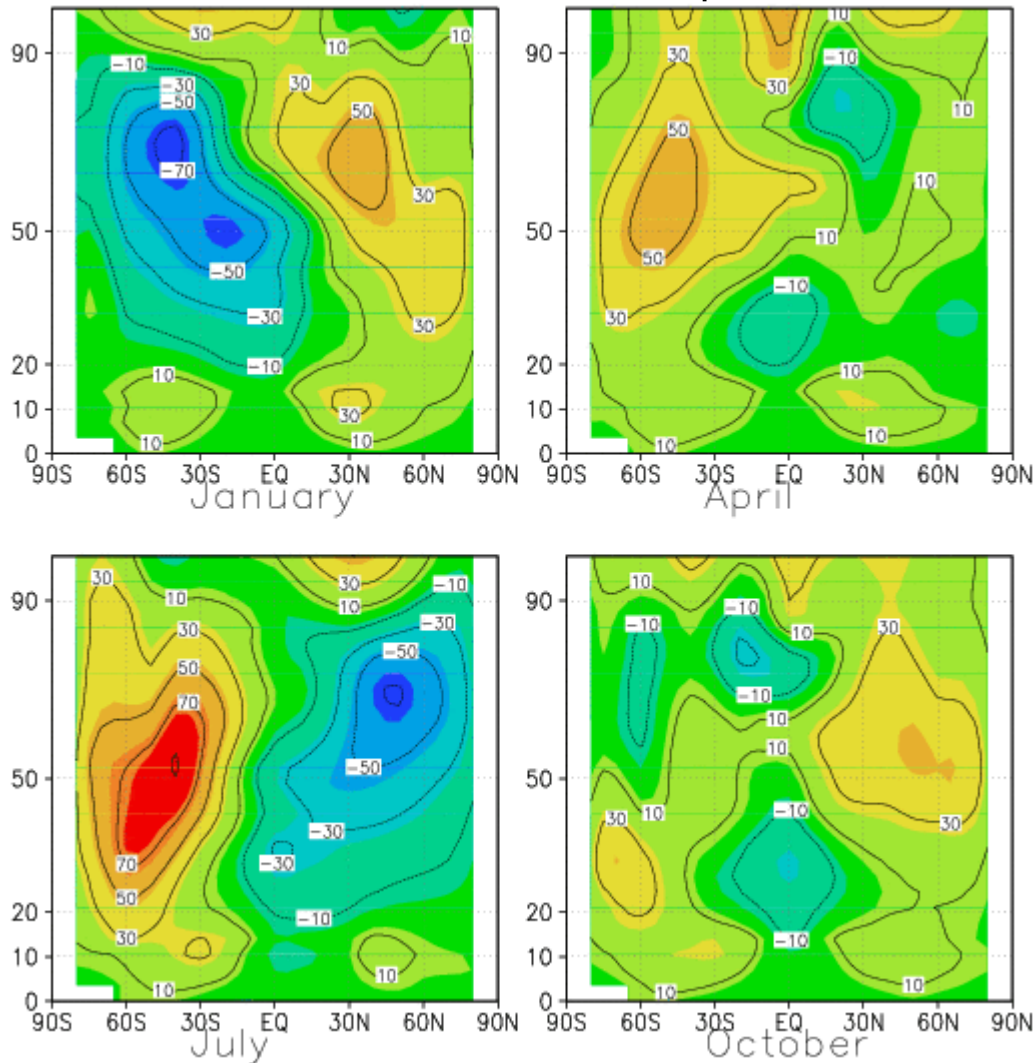
## a) Basic climatologies

Zonal mean zonal wind climatologies (CIRA dataset)

U (m/s)

Solstices

Equinoxes



- In all seasons there are two westerly jets near below the subtropical tropopause. These westerlies extend almost down to the surface (0-16km) and characterize the midlatitude circulations.
- Still in troposphere, the winds tend to be slightly westward (easterly) in the tropics.
- In the middle atmosphere (20-90km), the winds are eastward (westerlies) in the winter hemisphere and westward in the summer hemisphere.
- In spring and fall the middle atmosphere jets are eastward in both hemisphere (equinox).
- Note, that during the winters, the jets in the southern hemisphere (July) are stronger than in the northern hemisphere (January).

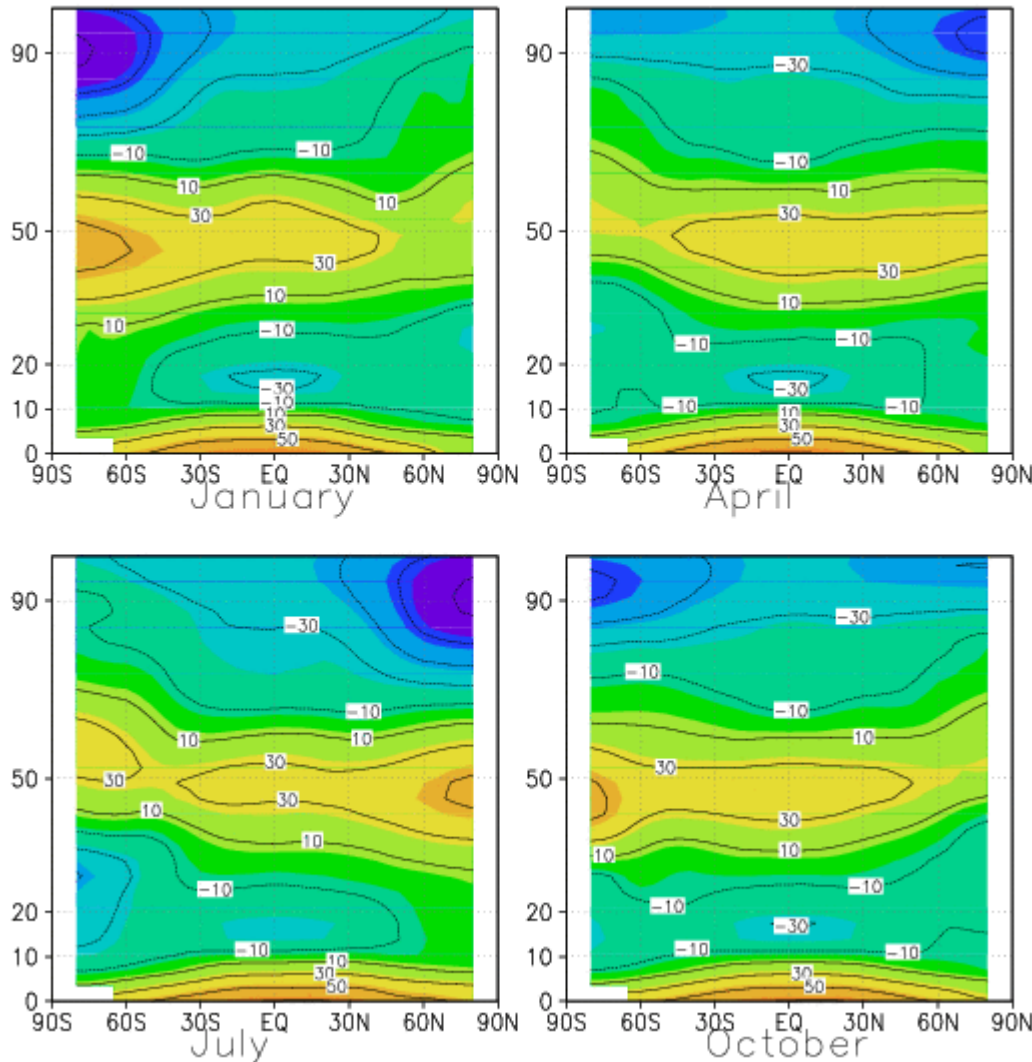
# General Circulation of the Stratosphere and modelisation

## a) Basic climatologies

Zonal mean temperature climatologies (CIRA dataset)  
T-230 (K)

Solstices

Equinoxes



- Temperature decay with altitude in the troposphere.
- There is a minimum at the tropical tropopause (a greenhouse effect due to the presence of water vapour).
- In the stratosphere ( $20\text{km} < z < 50\text{km}$ ), T decreases from the summer pole to the winter pole.
- At the stratopause (50km) in the summer hemisphere, there is a max in T.
- During solstices and in the upper mesosphere (70-90km) T increases from the summer pole to the winter pole!
- Still in the solstices and at the mesopause, (90km) there are pronounced minima in T (~180K) over the summer pole!!



# General Circulation of the Stratosphere and modelisation

## b) Interpretation with a simplified model

### Equations

$$\left( \frac{\partial}{\partial t} + \frac{v}{a} \frac{\partial}{\partial \phi} \right) u - \left( 2\Omega + \frac{u}{a \cos \phi} \right) v \sin \phi = 0$$

$$\left( \frac{\partial}{\partial t} + \frac{v}{a} \frac{\partial}{\partial \phi} \right) v + \left( 2\Omega + \frac{u}{a \cos \phi} \right) u \sin \phi = -\frac{1}{a} \frac{\partial \Phi}{\partial \phi}$$

$$\frac{\partial \Phi}{\partial t} + \frac{1}{a \cos \phi} \frac{\partial \Phi v \cos \phi}{\partial \phi} = Q_{03} - \overline{Q_{03}^\phi} - \alpha (\Phi - \Phi_0)$$

Angular momentum conservation:

$$\left( \frac{\partial}{\partial t} + \frac{v}{a} \frac{\partial}{\partial \phi} \right) (u \cos \phi + a \Omega \cos^2 \phi) = 0$$

Donne pour des mouvements de petite amplitude (initialement):

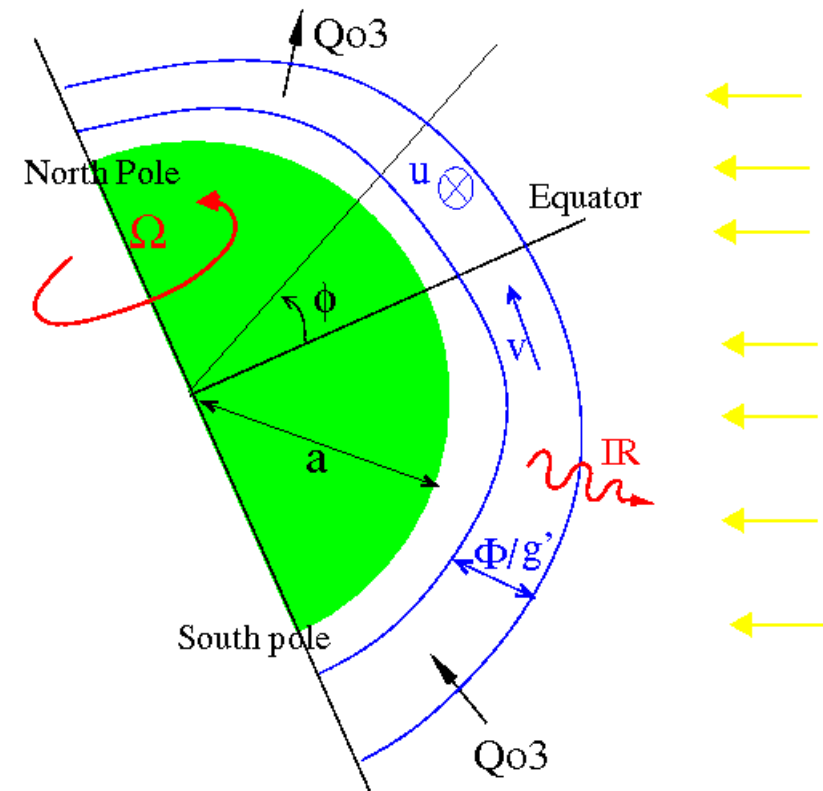
Geostrophic Equilibrium:

$$2\Omega \sin \phi u = -\frac{1}{a} \frac{\partial \Phi}{\partial \phi}$$

Thermal equilibrium

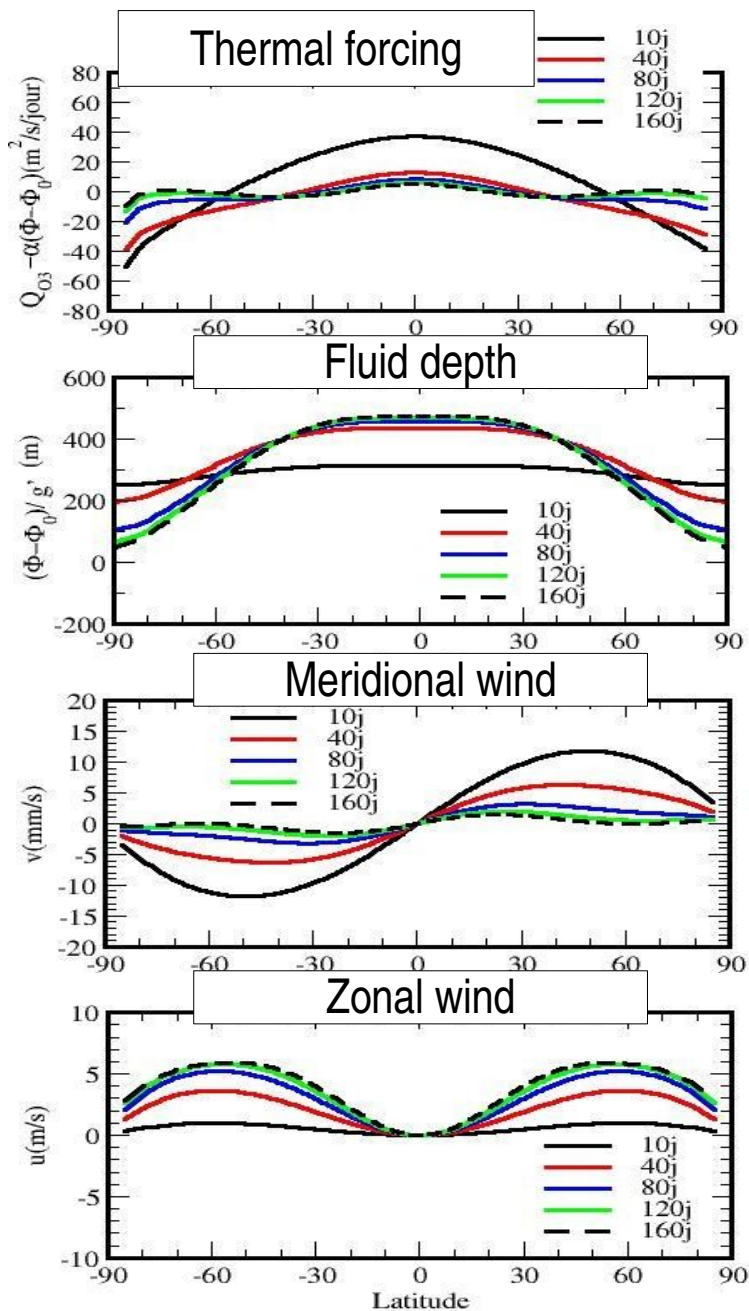
(proprio à ce modèle et pour  $\tau \rightarrow \infty$ )

$$Q_{03} - \overline{Q_{03}^\phi} = \alpha (\Phi - \Phi_0)$$



# General Circulation of the Stratosphere and modelisation

## b) Interpretation with a simplified model

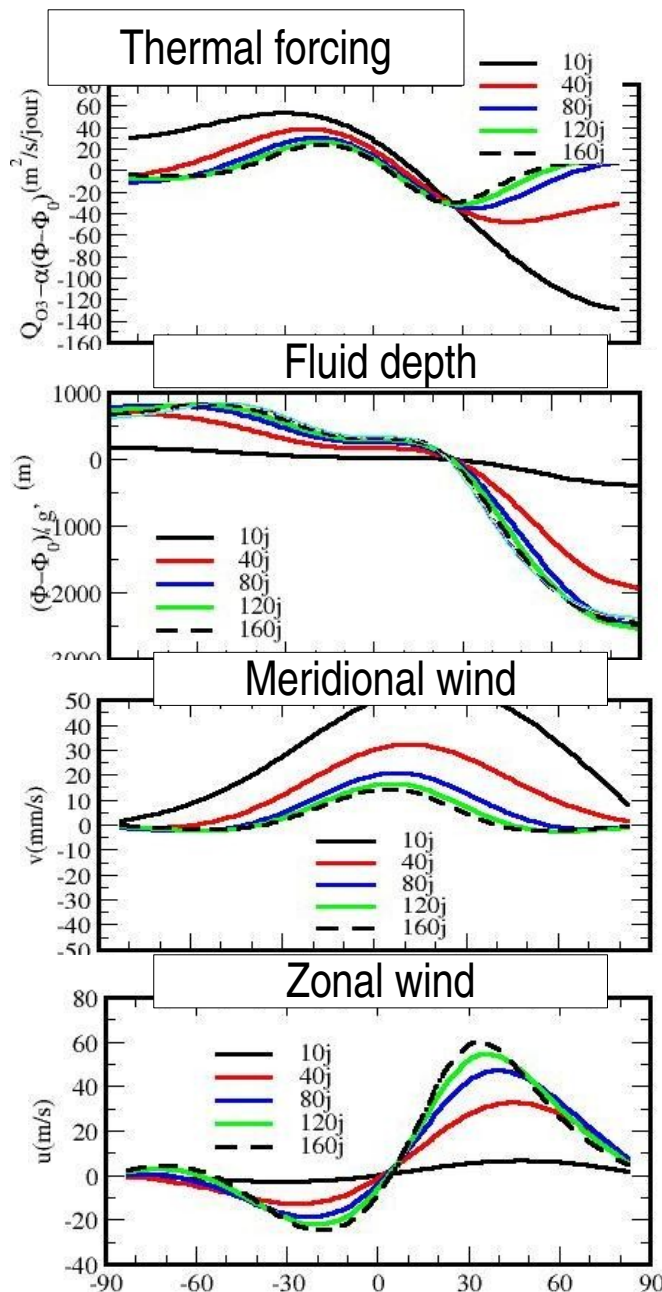


### Results for Equinoxes

- At the beginning (10d) the diabatic forcing is due to  $O_3$  only, it induces an increase of  $\Phi$  at the equator and a decrease in the mid and polar latitudes
- A radiative equilibrium between the diabatic Heating and the IR cooling is reached after 160d. The diabatic forcing is then very small.
- Initially, the heating induces a meridional motion ( $v$ ) toward the north in the NH, toward the south in the SH.
- Although our model is for the middle atmosphere here during equinox, the results shown are also adapted to the tropospheric Hadley cells, and which are due to a diabatic heating in the mid troposphere centred near the equator during all seasons.
- Note that  $v$  becomes very small at equilibrium (160d). Does this question the existence of the Hadley cells except in the transient cases?
- By angular momentum conservation, this meridional displacement produced positive zonal winds in both hemisphere.
- Note that  $u$  is in geostrophic equilibrium with  $\Phi$  in the midlatitudes.

# General Circulation of the Stratosphere and modelisation

## b) Interpretation with a simplified model

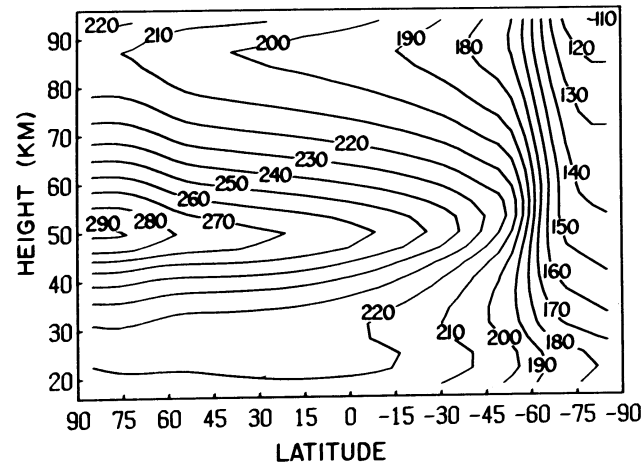


### Results for January

- At the beginning (10d), the diabatic forcing is due to  $O_3$  only. It induces an increase of  $\Phi$  in the southern Hemisphere and a decrease in the Northern hemisphere.
- A radiative equilibrium between the forcing due to  $O_3$  and the IR cooling is reached after 160d.
- The initial forcing due to  $O_3$  induce a meridional displacement ( $v$ ).  $v$  becomes very small when we get near the steady state (160d).
- Again the model is not efficient to explain steady-state meridional circulations.
- By angular momentum conservation, these displacements induced negative zonal winds ( $u$ ) in the SH and positive zonal winds in the NH.
- Note that:
  - The westerlies in the NH are much stronger in amplitude than the easterlies in the SH.
  - $U$  is in geostrophic balance with  $\Phi$  in the midlatitudes:

# General Circulation of the Stratosphere and modelisation

## b) Interpretation with a simplified model



The middle atmosphere is not in thermal equilibrium

Result here from a radiative code alone,

The zonal wind is evaluated from the T field via the thermal wind balance

Fig. 2.34. Radiative equilibrium temperature distribution for northern (left) summer solstice. [From Wehrbein and Leovy (1982), with permission.]

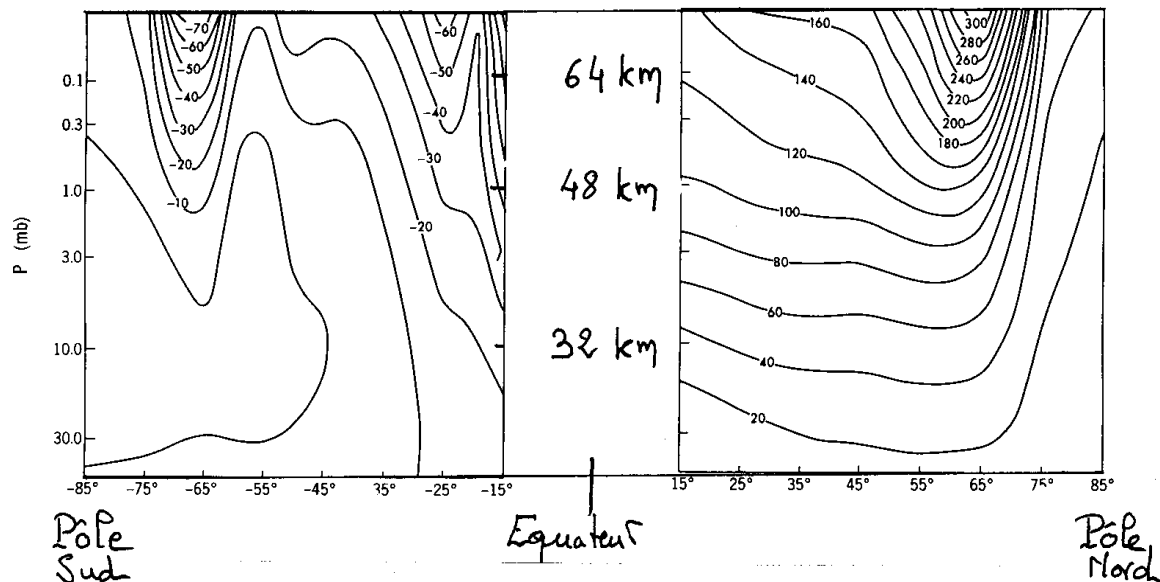
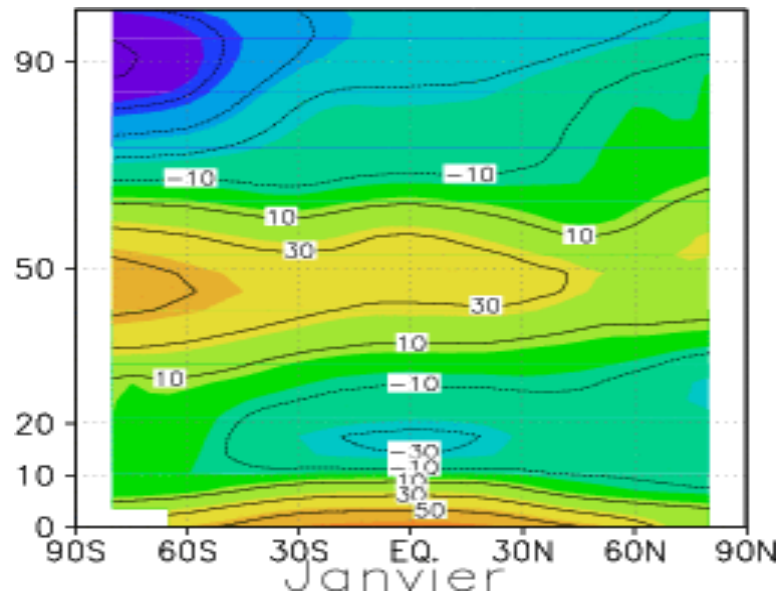


Fig. 7.1. Zonal gradient wind  $u_g$  that is in thermal-wind balance with the temperature field  $T_g$  of Fig. 1.2 and equals the observed climatological zonal wind at 100 mb. (a) Northern Hemisphere (winter), (b) Southern Hemisphere (summer). (Courtesy of Dr. S. B. Fels.)

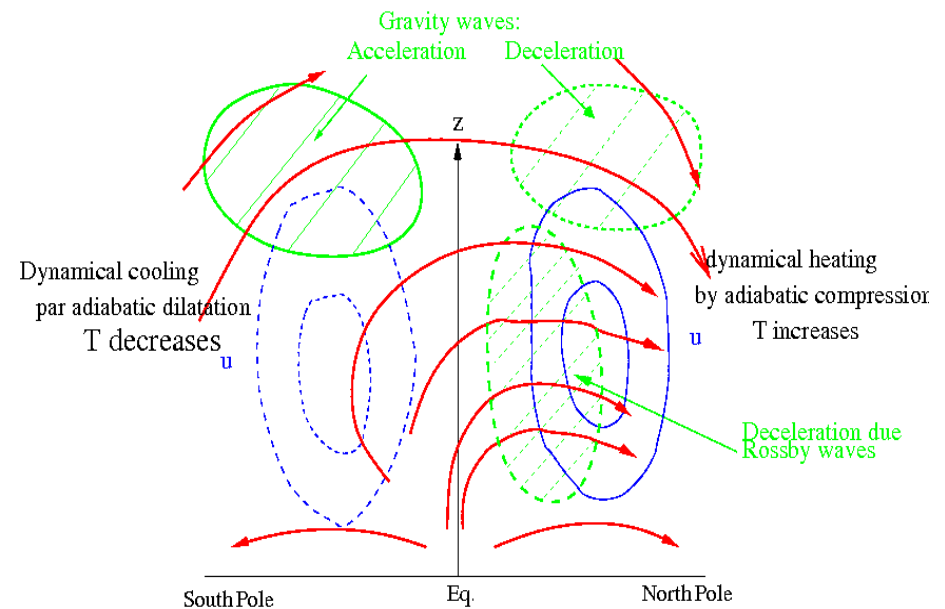
# General Circulation of the Stratosphere and modelisation

## c) The Brewer Dobson Circulation

January Temperatures



The meridional circulation driven by waves and the « downward control »

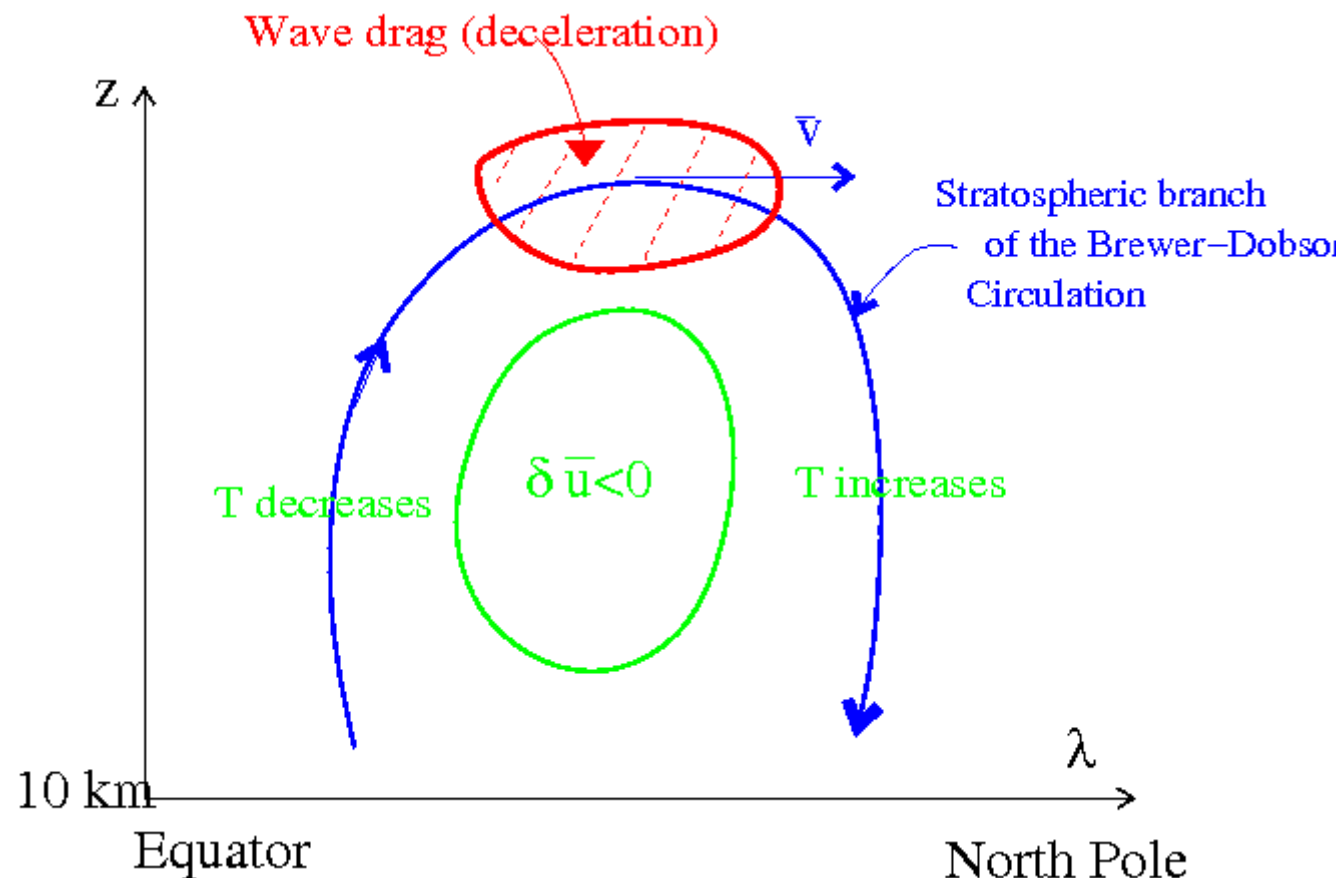




# General Circulation of the Stratosphere and modelisation

## c) The Brewer Dobson Circulation

More about the downward control, or how to decelerate a rapidly rotating fluid on a sphere!

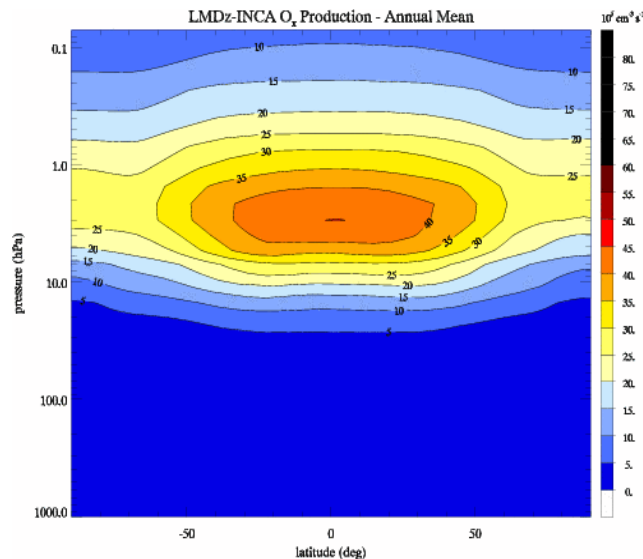


# General Circulation of the Stratosphere and modelisation

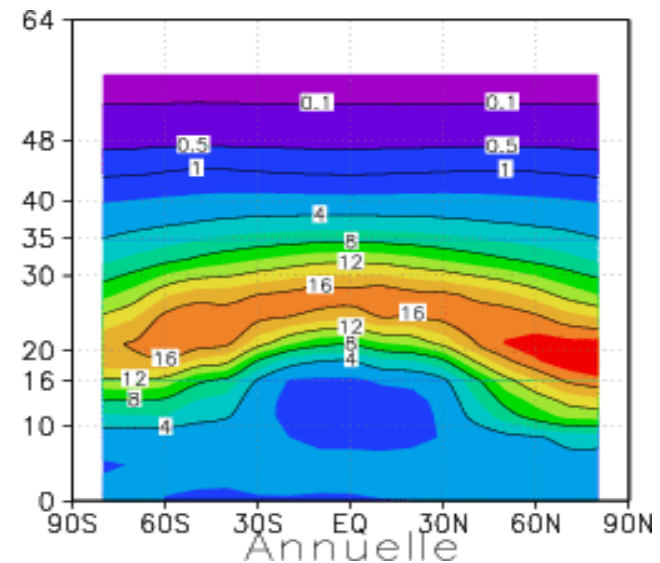
## c) The Brewer Dobson Circulation

The ozone is produced in majority around the equatorial tropopause, but accumulates up at much lower altitudes and latitudes!

Annual mean production  
Of  $O_3$



Annual mean of  $O_3$

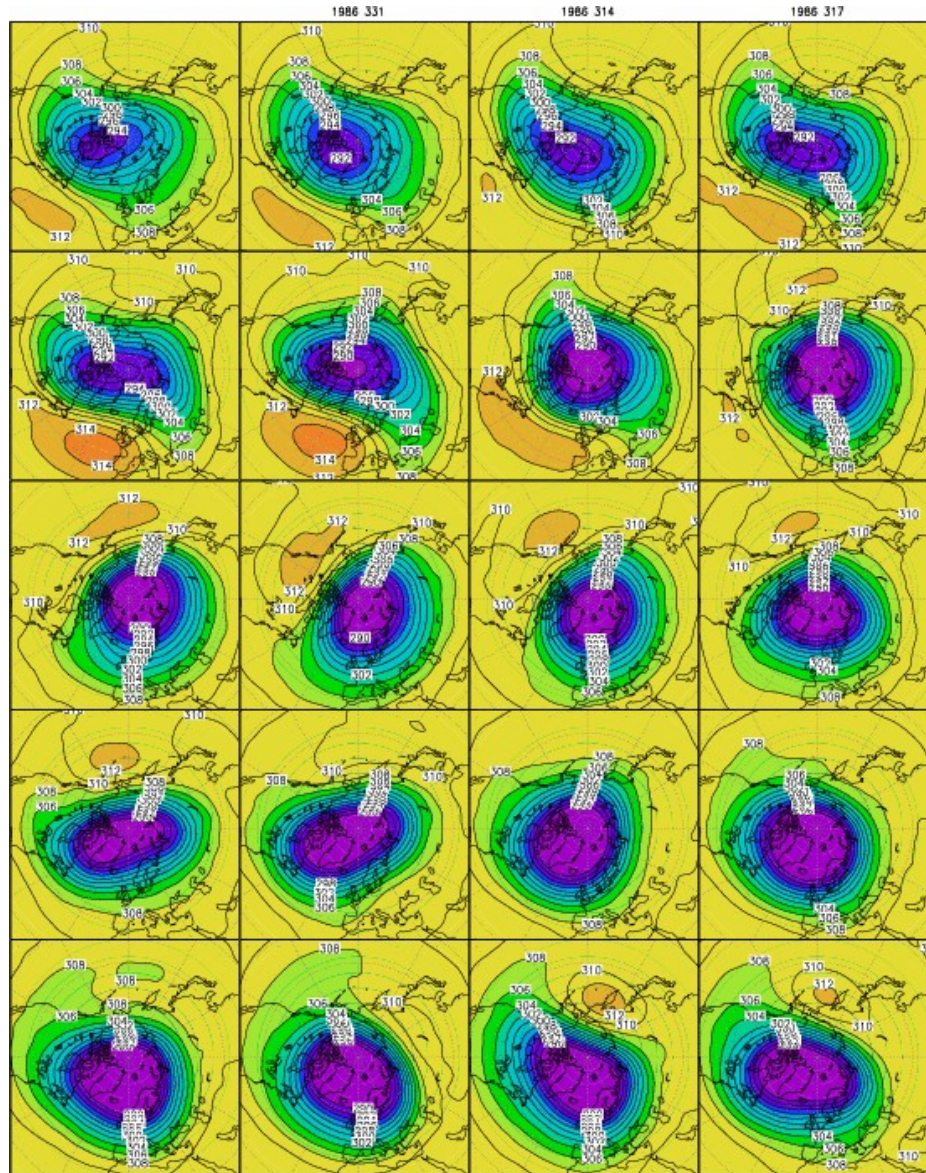


# General Circulation of the Stratosphere and modelisation

## d) Midlatitude Dynamics

In the stratosphere  
the Rossby waves  
also play a very large rôle  
on the mean climate  
and variability

(here evolution of a  
geopotential map  
at  $z=32\text{km}$  every  
3 days)

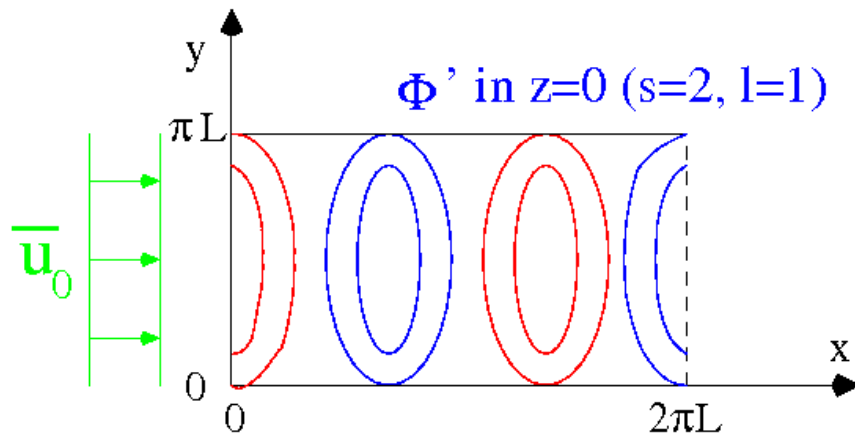


# General Circulation of the Stratosphere and modelisation

## d) Midlatitude Dynamics

These Rossby waves are very slow, they are quite intermittent and are forced by the low frequency variability of the tropospheric weather.

Vertical structure equation of a quasi-steady Rossby wave on a laterally bounded beta plane. Quasi-Geostrophic approximation is made.



$$\hat{\Phi}_{zz} + \left( \frac{N^2}{f^2} \left( \frac{\beta}{\bar{u}_0} - k^2 - l^2 \right) - \frac{1}{4H^2} \right) \hat{\Phi} = 0$$

Only vertical propagation if the mean wind is  $>0$   
(in winter)

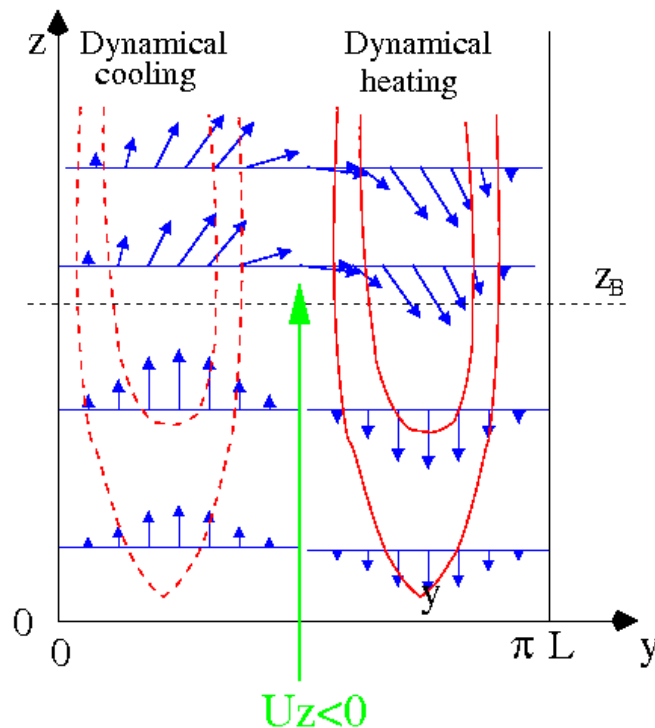
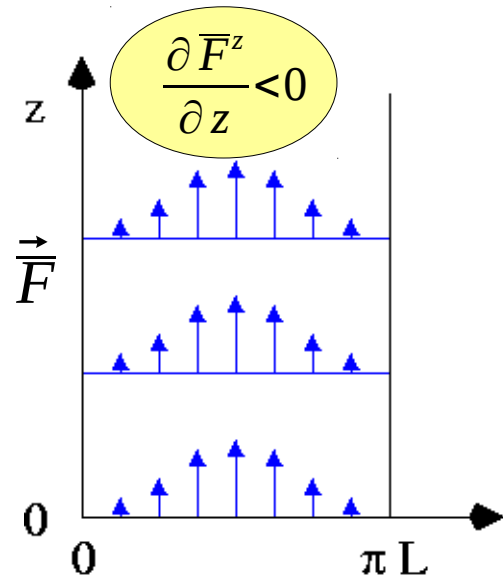
Only the very long modes can propagate vertically

# General Circulation of the Stratosphere and modelisation

## d) Midlatitude Dynamics

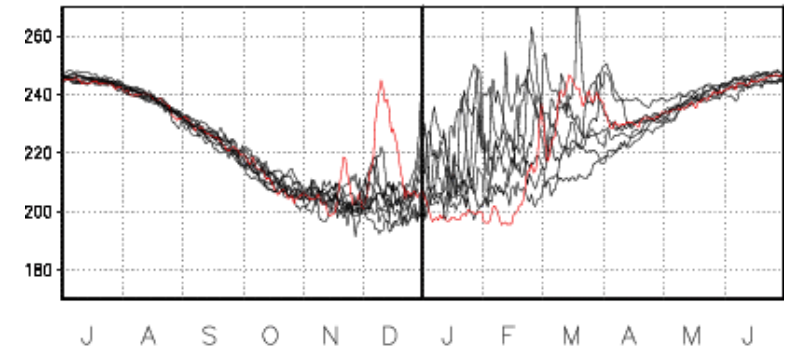
These Rossby waves as well break (in this case via barotropic instabilities rather than by convective instability for the Gws). This yields to the Stratospheric warmings

Vertical structure equation of a quasi-steady Rossby wave on a laterally bounded beta plane. Quasi-Geostrophic approximation is made.

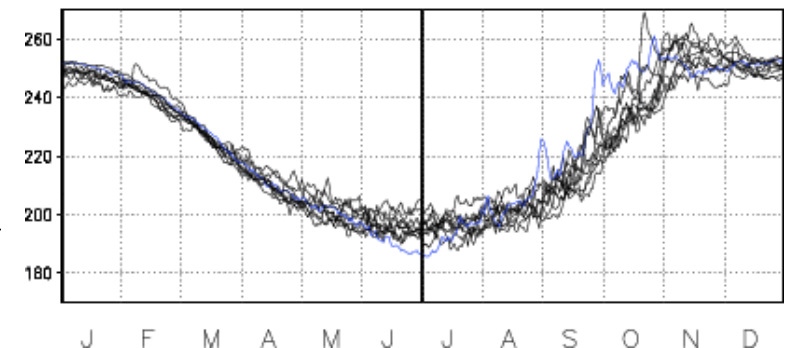


Temperature at the poles

T au Pole Nord a 32km



T au Pole Sud a 32km



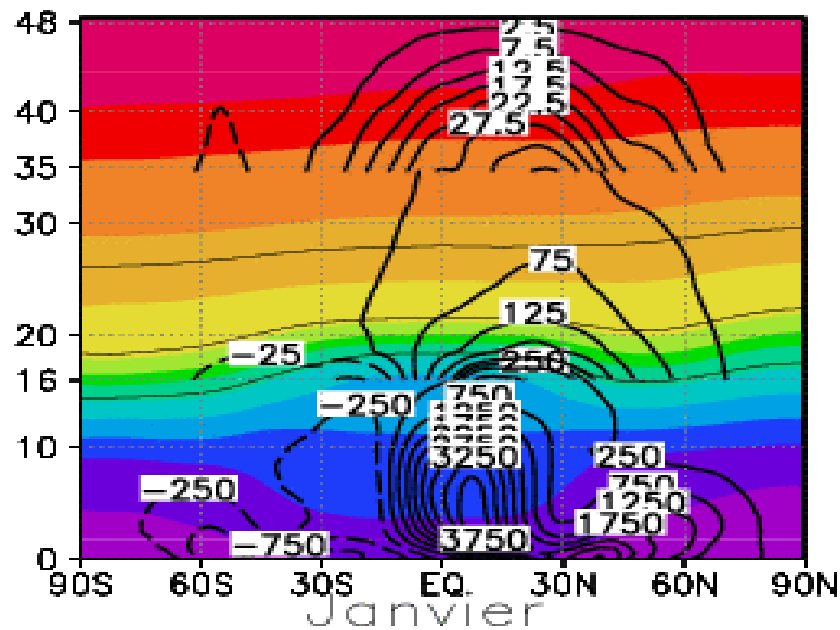


## General Circulation of the Stratosphere and modelisation

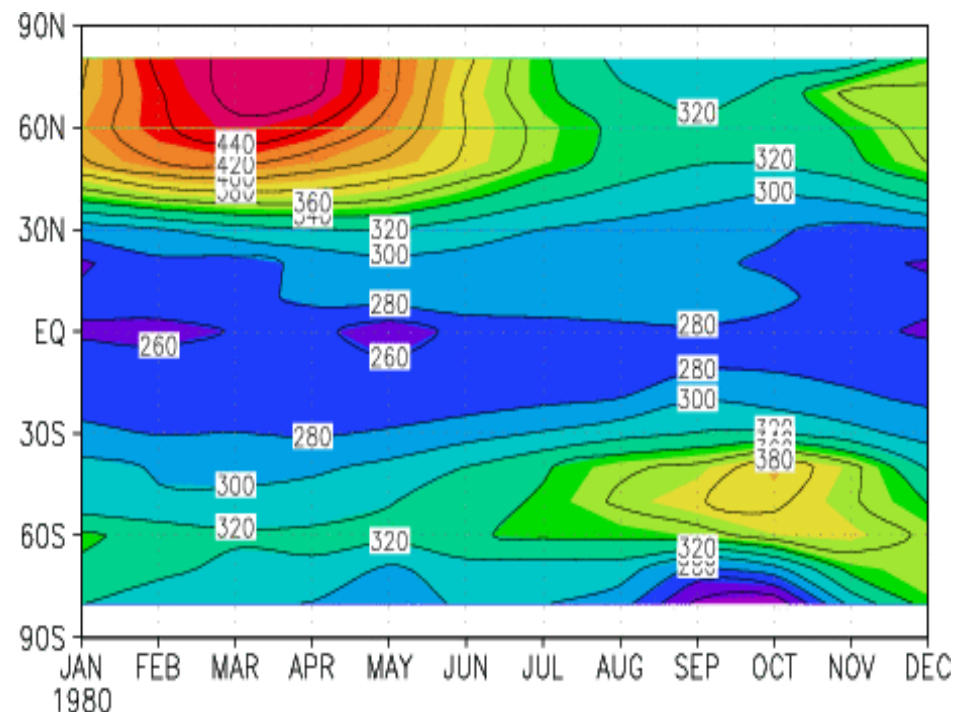
### c) The Brewer Dobson Circulation

The ozone is produced in majority around the equatorial tropopause, but accumulates up at much lower altitudes and latitudes!

## Streamfunction of the meridional circulation, January (TEM formalism)



## Annual Cycle of O3



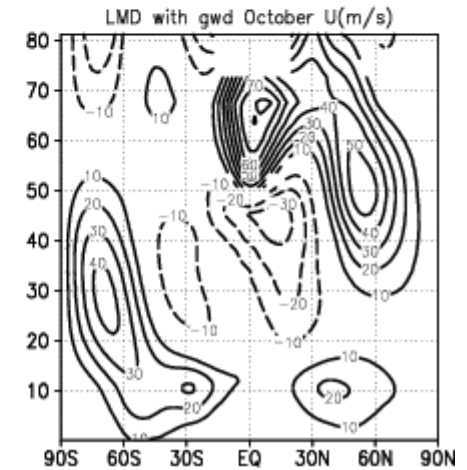
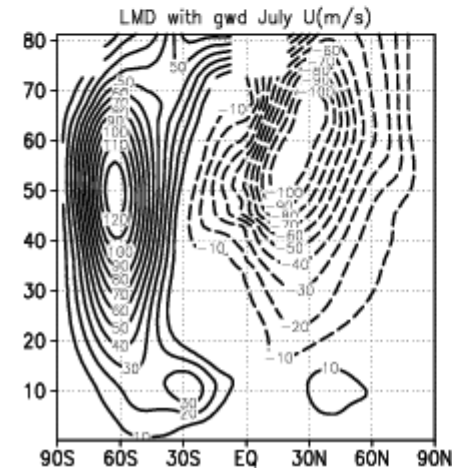
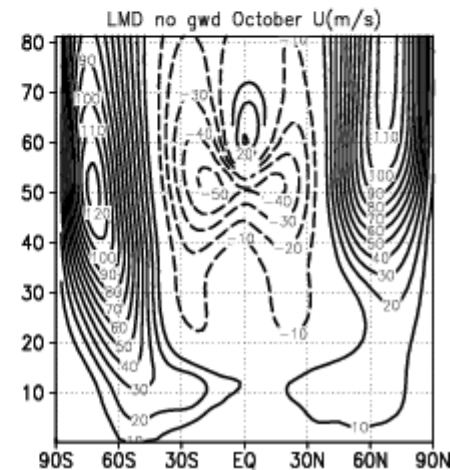
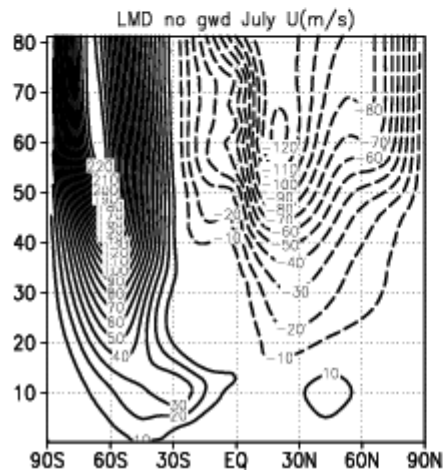
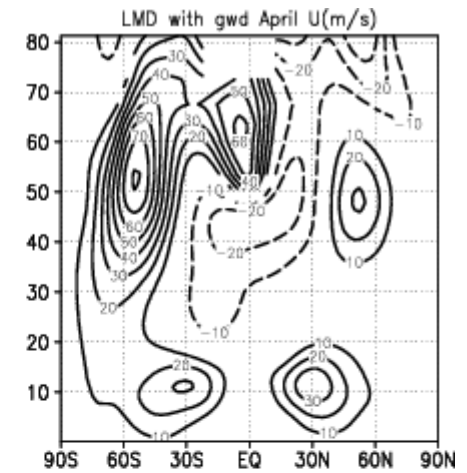
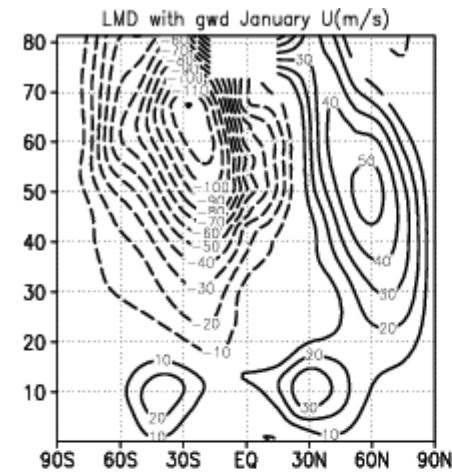
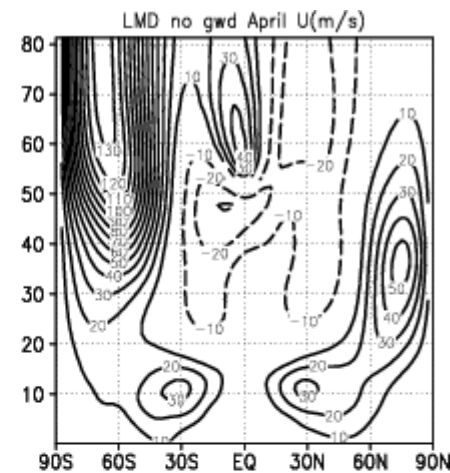
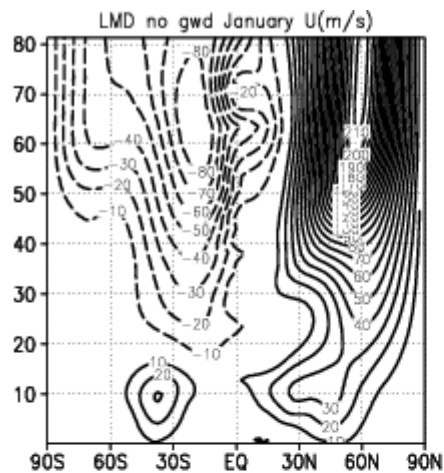
# General Circulation of the Stratosphere and modelisation

## c) The Brewer Dobson Circulation

The effect of gravity waves can be well seen in the mesosphere if we compare simulations with and without parameterization LMDz  
(Lott et al. 2005, Lott Millet 2010):

without

with



# General Circulation of the Stratosphere and modelisation

## d) Equatorial Dynamics

Zonal wind at the Equator: Semi annual and quasi biennial oscillation

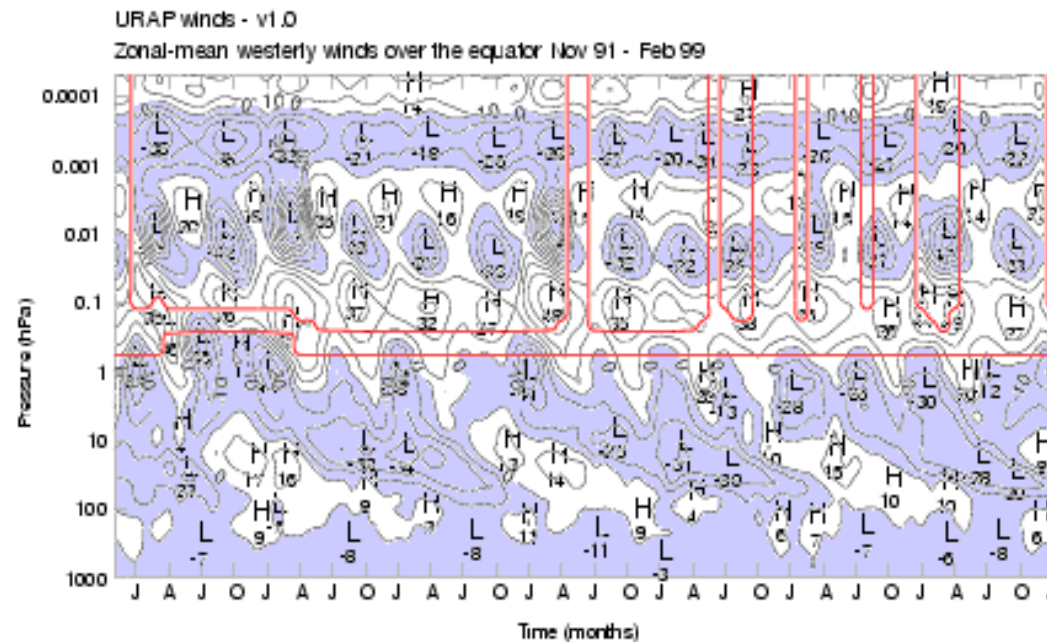


Figure 6. Time series of zonal-mean westerly winds over the equator, from November 1991 to February 1999. The tick marks along the x-axis mark each January, April, July and October. The additional lines show where the values are mainly derived from interpolated or climatological data.

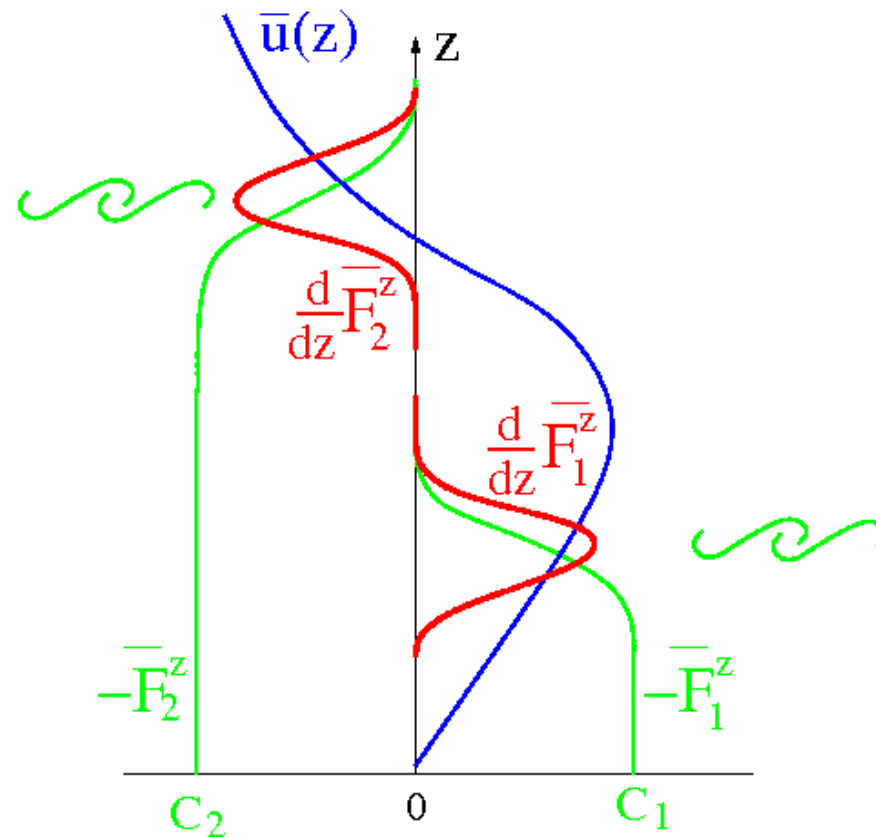
(UARS observations, Swinbank and Ortland, 1997)

# General Circulation of the Stratosphere and modelisation

## d) Equatorial Dynamics

The plumb model for a semi-annual oscillation driven by two gravity waves

$$\rho_0 \frac{\partial \bar{u}}{\partial t} = \sum_{i=1}^2 \frac{\partial \bar{F}_i^z}{\partial z} + \frac{\partial}{\partial z} v \frac{\partial \bar{u}}{\partial z}$$



# General Circulation of the Stratosphere and modelisation

## e) Convective gravity waves parameterization

*Classical arguments to justify stochastic parameterizations*

*(Palmer et al. 2005, Shutts and Palmer 2007, for the GWs: Piani et al. (2005, globally spectral scheme) and Eckeman (2011, multiwaves scheme))*

1) The spatial steps  $\Delta x$  and  $\Delta y$  of the unresolved waves is not a well defined concept (even though they are probably related to the model gridscales  $\delta x$   $\delta y$ ). The time scale of the GWs life cycle  $\Delta t$  is certainly larger than the time step ( $\delta t$ ) of the model, and is also not well defined.

2) The mesoscale dynamics producing GWs is not well predictable (for the mountain gravity waves see Doyle et al. MWR 11).

These calls for an extension of the concept of triple Fourier series, which is at the basis of the subgrid scale waves parameterization to that of stochastic series:

$$w' = \sum_{n=1}^{\infty} C_n w'_n \quad \text{where} \quad \sum_{n=1}^{\infty} C_n^2 = 1$$

The  $C'_n$ s generalised the intermittency coefficients of Alexander and Dunkerton (1995), and used in Beres et al. (2005).



# General Circulation of the Stratosphere and modelisation

## e) Convective gravity waves parameterization

For the  $w'_n$  we use linear WKB theory of hydrostatic GWs, and treat the breaking as if each  $w'_n$  was doing the entire wave field (using Lindzen (1982)'s criteria for instance):

$$w'_n = \Re \left\{ \hat{w}_n(z) e^{z/2H} e^{i(k_n x + l_n y - \omega_n t)} \right\} \quad \hat{w}_n, k_n, l_n, \omega_n \text{ chosen randomly}$$

WKB passage from one level to the next with a small dissipation (Eliassen Palm flux):

$$\vec{F}(z+dz) = \frac{\vec{k}}{|\vec{k}|} \text{sign}(\Omega) \left( \frac{1 + \text{sign}(\Omega(z+\delta z) \cdot \Omega(z))}{2} \right) \text{Min} \left( |\vec{F}(z)| e^{-2 \frac{\nu m^3}{\Omega} \delta z}, \rho_r \frac{|\Omega^3|}{2N} e^{-(z+\delta z)/H} S_c^2 \frac{k^{*2}}{|\vec{k}^4|} \right)$$

Critical level

Eliassen-Palm theorem  
with dissipation

Breaking

$S_c, k^*$ : Tunable parameters

$$m = \frac{N |\vec{k}|}{\Omega} \quad \text{Vertical wavenumber}$$

$$\Omega = \omega - \vec{k} \cdot \vec{u} \quad \text{Intrinsic frequency}$$

Few waves (say  $M=8$ ) are launched at each physical time step ( $\delta t=30\text{mn}$ ), but their effect is redistributed over a longer time scale ( $\Delta t=1\text{day}$ ), via an AR-1 protocole:

$$\left( \frac{\partial \vec{u}}{\partial t} \right)_{GWs}^{t+\delta t} = \frac{\Delta t - \delta t}{\Delta t} \left( \frac{\partial \vec{u}}{\partial t} \right)_{GWs}^t + \frac{\delta t}{M \Delta t} \sum_{n'=1}^M \frac{1}{\rho} \frac{\partial \vec{F}_n^z}{\partial z}$$

# General Circulation of the Stratosphere and modelisation

## e) Convective gravity waves parameterization

$$P'_r = \sum_{n=1}^{\infty} C_n P'_n \text{ where } P'_n = \Re \left[ \hat{P}_n e^{i(\vec{k}_n \cdot \vec{x} - \omega_n t)} \right] \quad \text{taking} \quad |\hat{P}_n| = P_r$$

The subgrid scale standard deviation of the precipitation equals the gridscale mean

Distributing the related diabatic forcing over a depth  $\Delta z$  it is quite easy to place the forcing in the right hand side of a “wave” equation:

$$\rho c_p \left( \frac{DT'}{dt} + \frac{DT_0}{dz} w' \right) = L_w P' \frac{e^{-z^2/\Delta z^2}}{\Delta z} \rightarrow \frac{\Omega^2}{k^2} \hat{w}_{zz} + N^2 \hat{w} = \frac{R L_w}{\rho H c_p} \hat{P} \frac{e^{-z^2/\Delta z^2}}{\Delta z}$$

EP-flux at the launch level:

$$\vec{F}_{nl} = \rho_r \frac{\vec{k}_n |\vec{k}_n|^2 e^{-m_n^2 \Delta z^2}}{|\vec{k}_n| N \Omega_n^3} G_{uw} \left( \frac{R L_w}{\rho_r H c_p} \right)^2 P_r^2$$

New tuning parameter (could be a random number)

$$k_n, l_n, \omega_n$$

Are still chosen randomly

$$m_n = \frac{N |\vec{k}_n|}{\Omega_n}, \Omega_n = \omega_n - \vec{k}_n \cdot \vec{U}$$

# General Circulation of the Stratosphere and modelisation

## e) Convective gravity waves parameterization

### Offline tests with ERAI and GPCP

$$G_{uw}=2.4, S_c=0.25,$$

$$k^*=0.02\text{km}^{-1},$$

$$m=1\text{kg/m/s}$$

$$Dt=1\text{day and } M=8$$

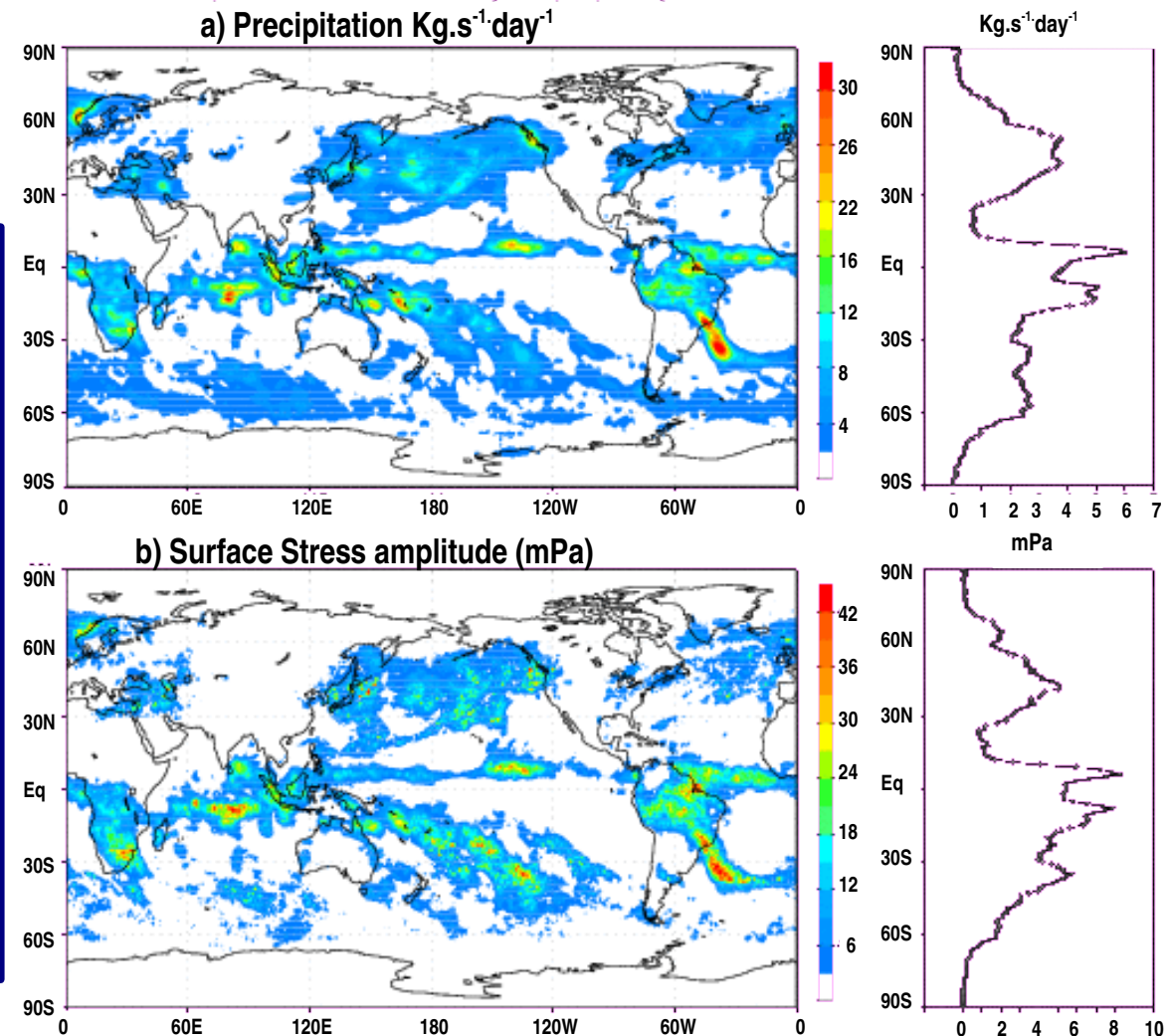
$$Dz=1\text{km (source depth}\sim 5\text{km)}$$

Precipitations and surface stresses averaged over 1 week  
(1-7 January 2000) **Results for GPCP data and ERAI**

**The CGWs stress is now well distributed along where there is strong precipitations**

**It is stronger on average in the tropical regions, but quite significant in the midlatitudes.**

**The zonal mean stress comes from very large values issued from quite few regions.**

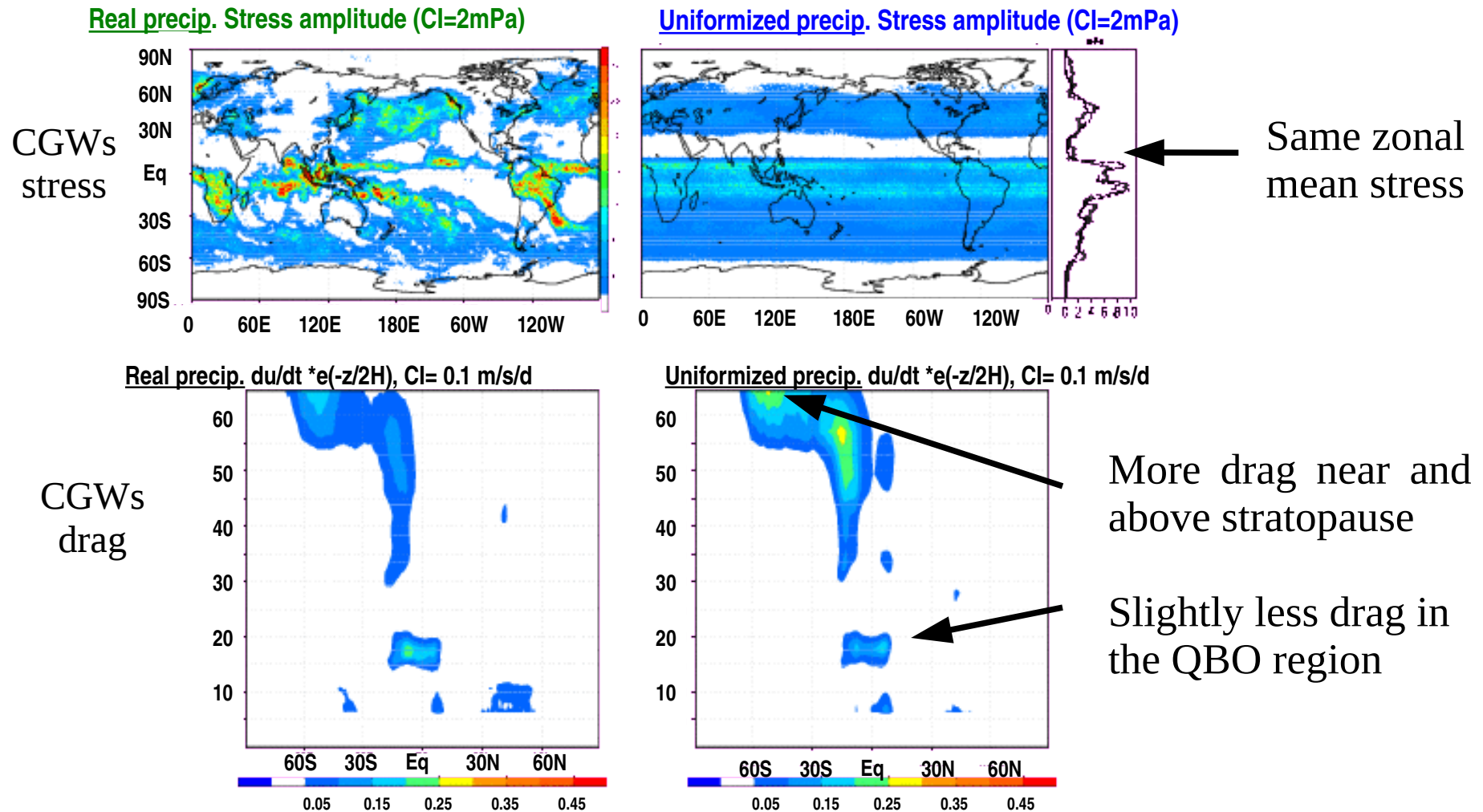


# General Circulation of the Stratosphere and modelisation

## e) Convective gravity waves parameterization

### Offline tests with ERAI and GPCP

Benefit of having few large GWs rather than a large ensemble of small ones:



# General Circulation of the Stratosphere and modelisation

## e) Convective gravity waves parameterization

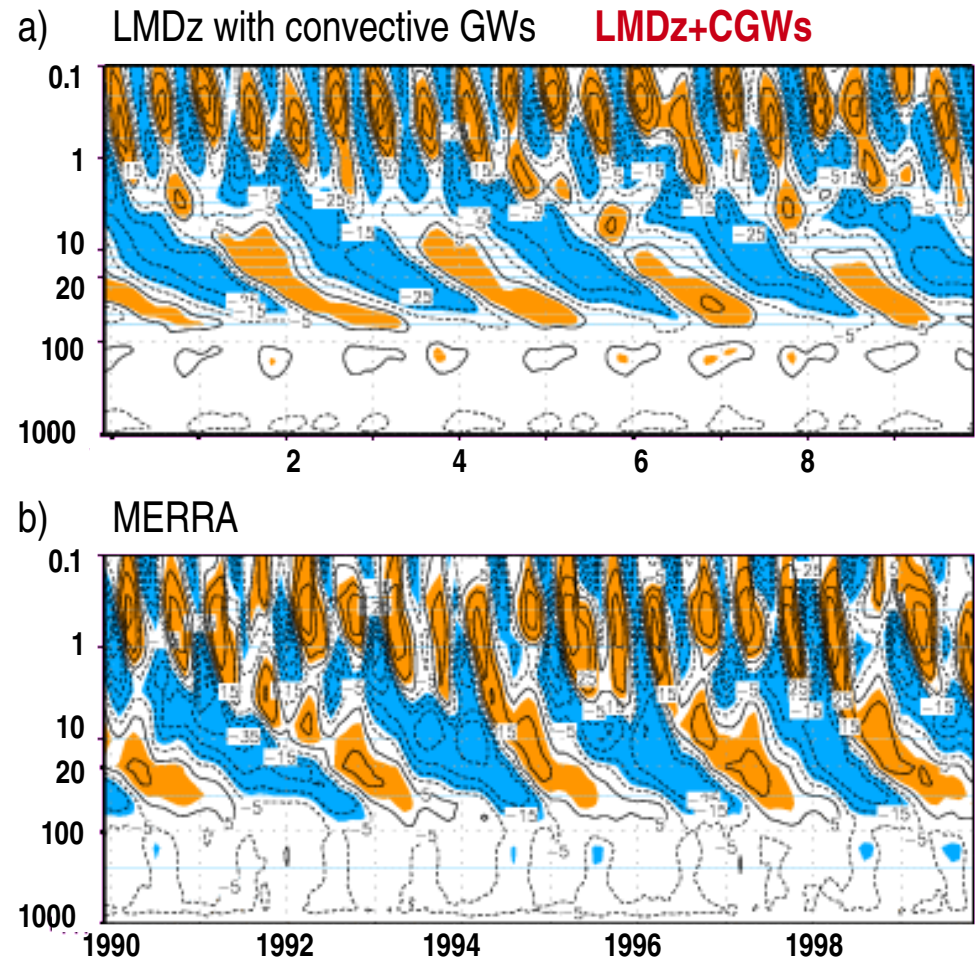
### Online results with LMDz

LMDz version with 80 levels,  $\Delta z < 1\text{km}$   
In the stratosphere

QBO of irregular  
period with mean  
around 26month,

20% too small amplitude

Westerly phase lacks of connection  
with the stratopause SAO



Lott and Guez, JGR13



# General Circulation of the Stratosphere and modelisation

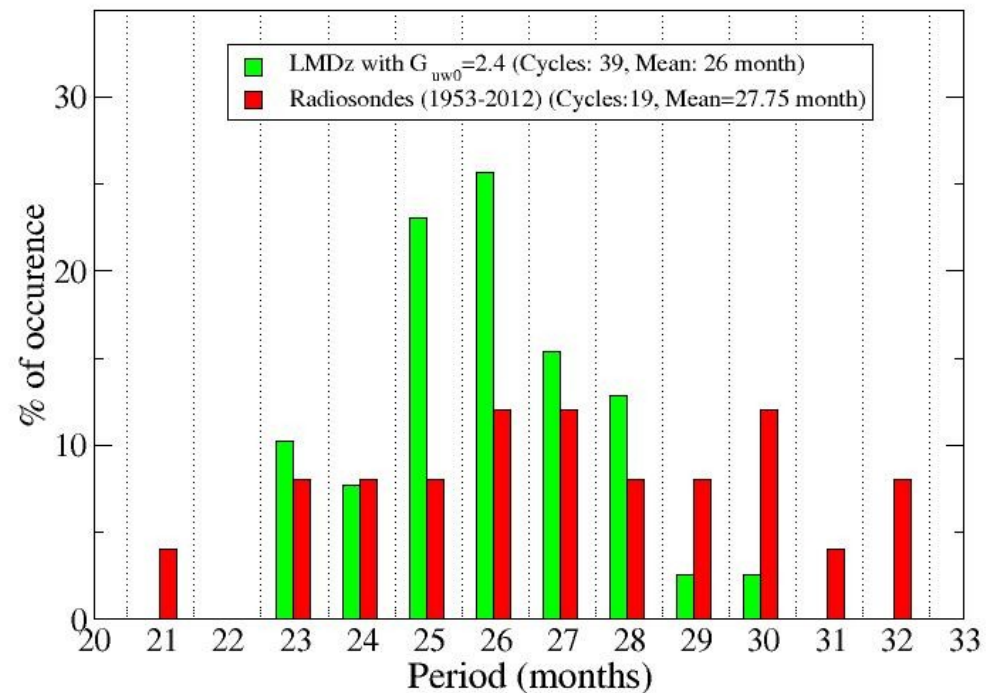
## e) Convective gravity waves parameterization

### Online results with LMDz

#### Histogram of QBO periods

Relatively good spread of the periods  
taking into account that it is a forced  
simulation with climatological SST  
(no ENSO)

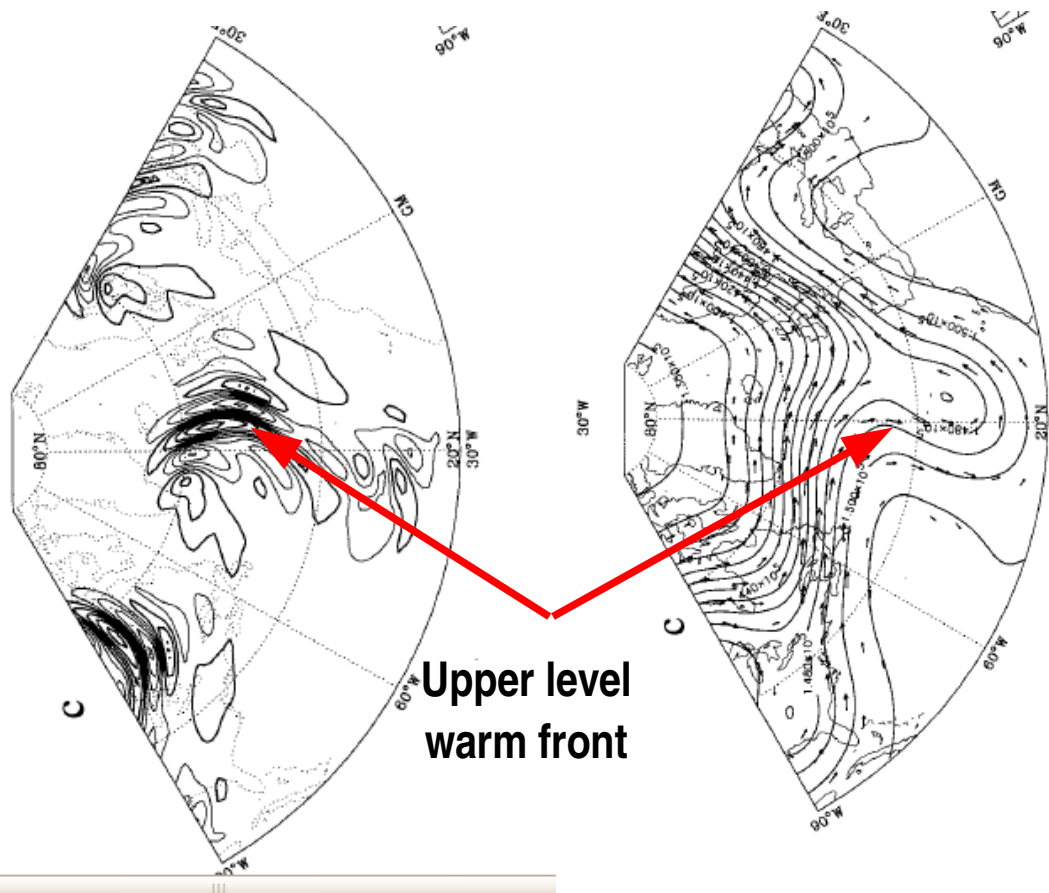
Periods related to the annual cycle  
(multiples of 6 months) are not favoured:  
probably related to the weak relations  
with the SAO



# General Circulation of the Stratosphere and modelisation

## f) Frontal gravity waves parameterization

Simulations to support these parameterizations:



O'Sullivan and Dunkerton (1995)

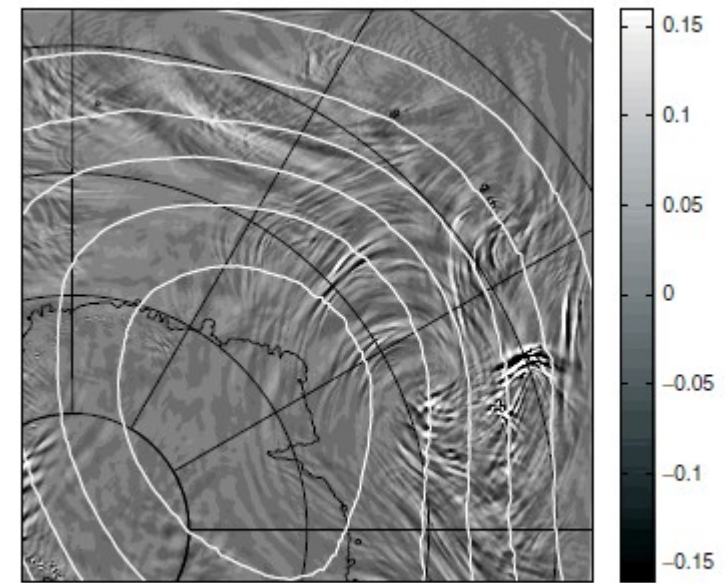


Figure 16. As Figure 2(b), but from a simulation with doubled horizontal resolution ( $\Delta x = 10$  km).

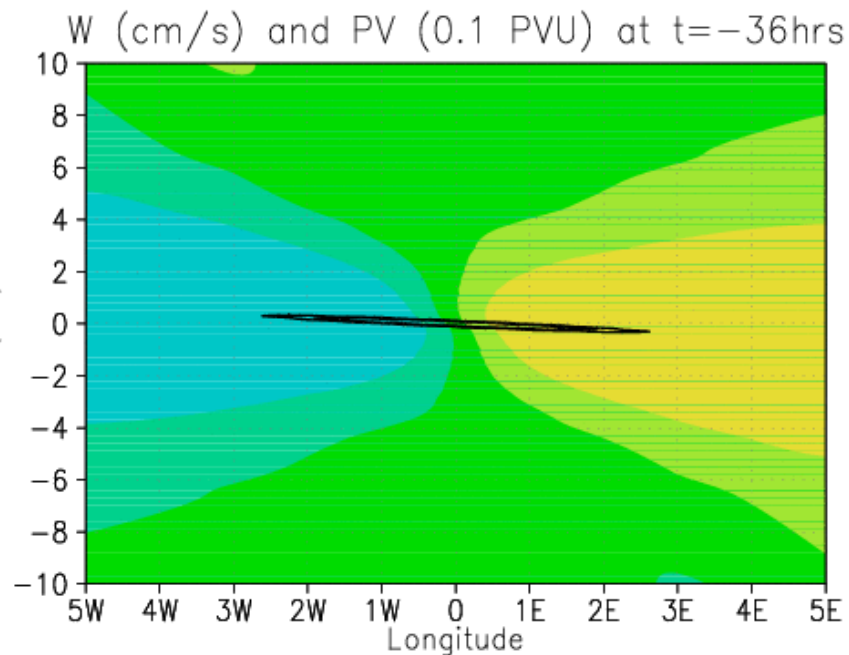
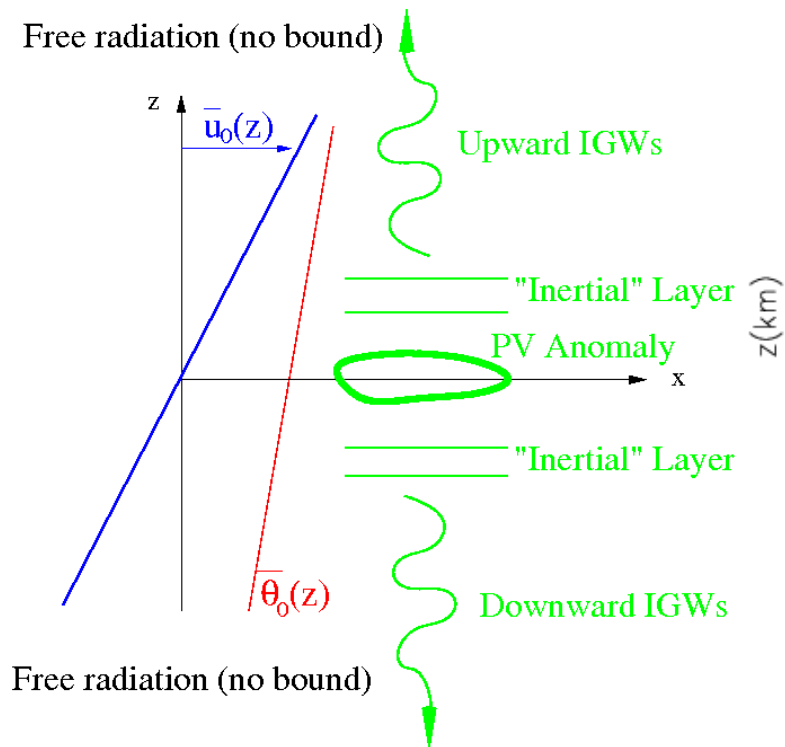
Results confirmed by much higher resolution simulations

Plougonven Hertzog and Guez (2012)

# General Circulation of the Stratosphere and modelisation

## f) Frontal gravity waves parameterization

General setup: A 3D  $(x,y,z)$  PV anomaly advected in a rotating ( $f=\text{cte}$ ), stratified (BV freq  $N=\text{cte}$ ) shear flow (vertical shear  $\Lambda=\text{cte}$ ).

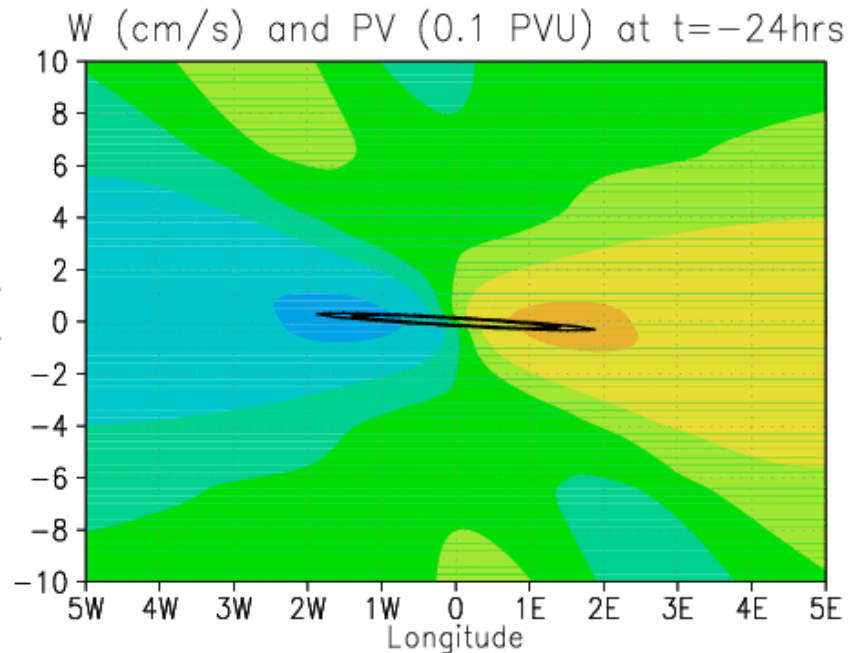
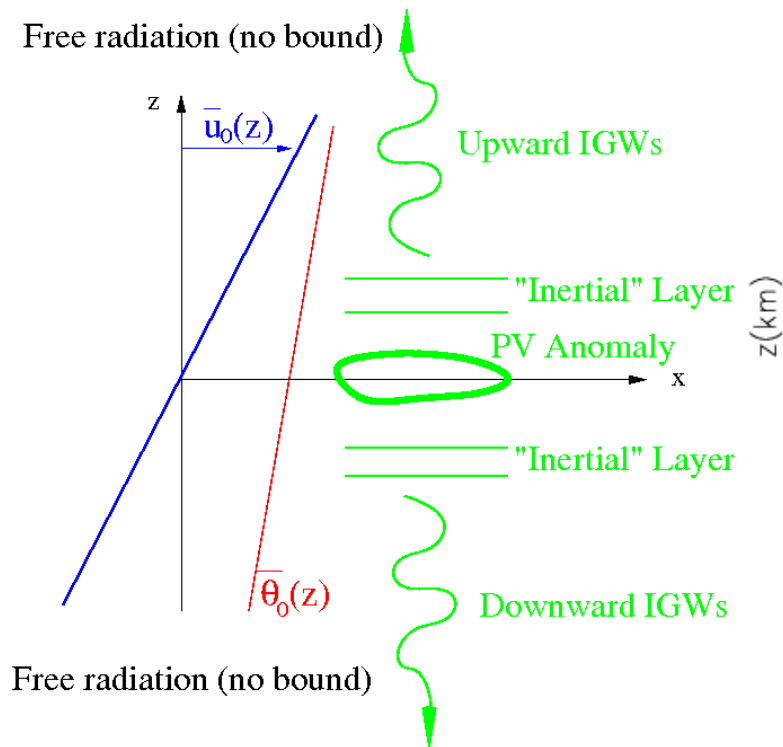


Spontaneous adjustment theory: *Lott, Plougonven and Vanneste, JAS 2010, JAS 2012.*

# General Circulation of the Stratosphere and modelisation

## f) Frontal gravity waves parameterization

General setup: A 3D  $(x,y,z)$  PV anomaly advected in a rotating ( $f=\text{cte}$ ), stratified (BV freq  $N=\text{cte}$ ) shear flow (vertical shear  $\Lambda=\text{cte}$ ).

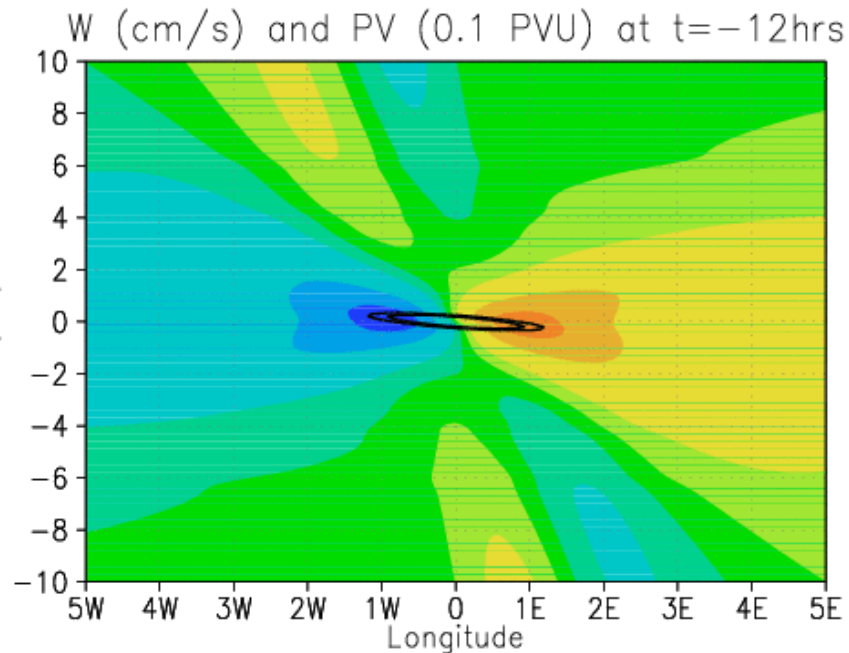
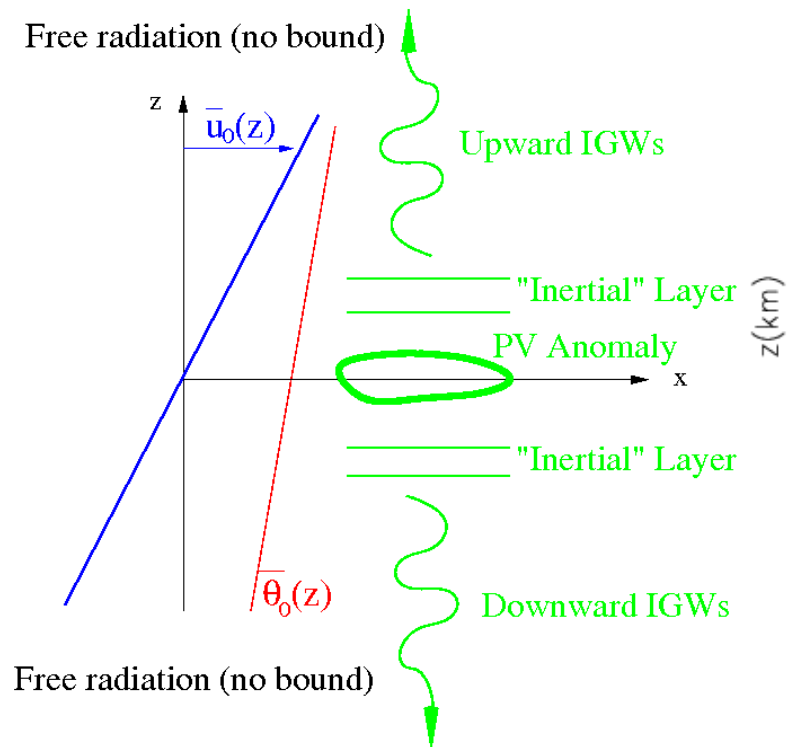


Spontaneous adjustment theory: *Lott, Plougonven and Vanneste, JAS 2010, JAS 2012.*

# General Circulation of the Stratosphere and modelisation

## f) Frontal gravity waves parameterization

General setup: A 3D  $(x,y,z)$  PV anomaly advected in a rotating ( $f=\text{cte}$ ), stratified (BV freq  $N=\text{cte}$ ) shear flow (vertical shear  $\Lambda=\text{cte}$ ).

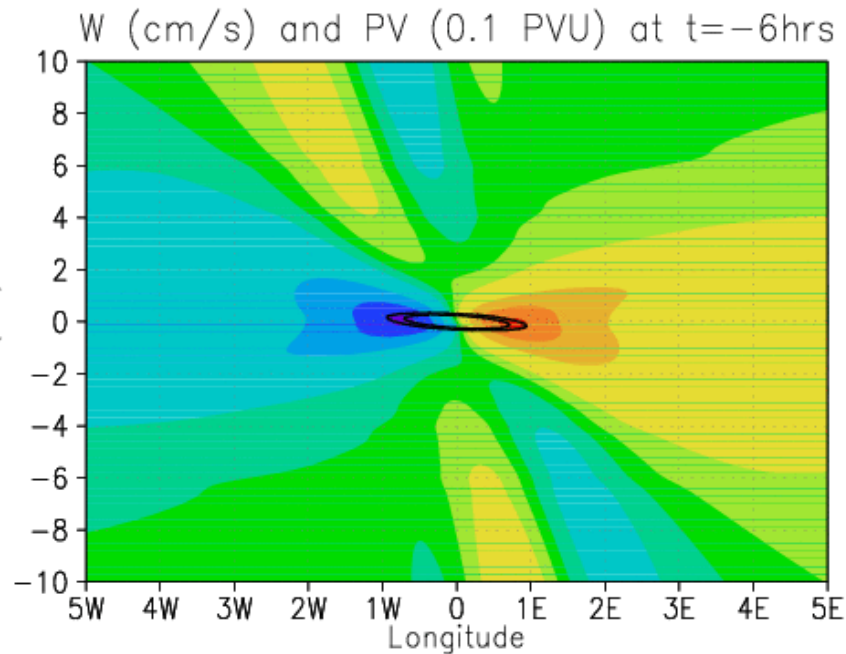
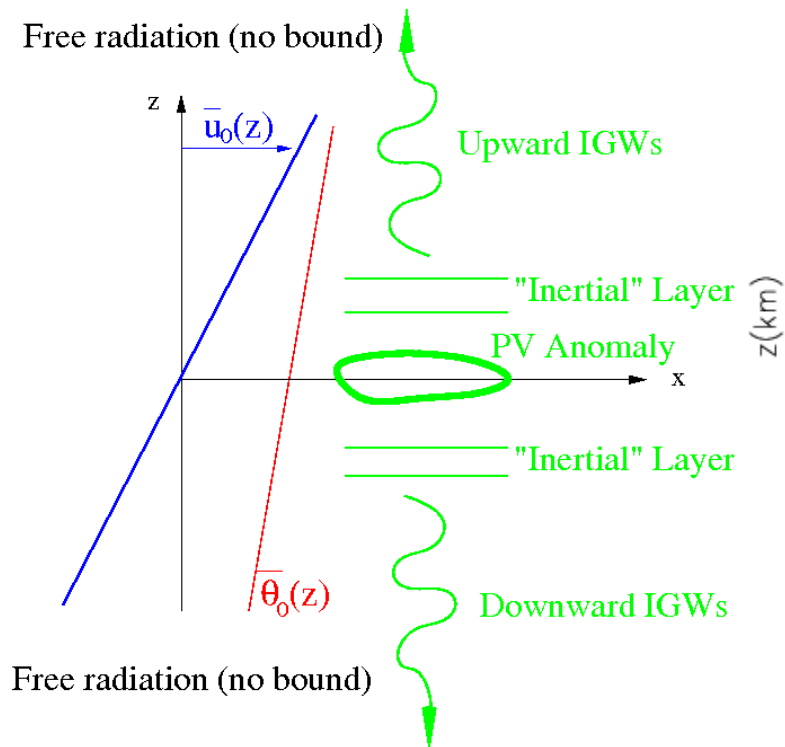


Spontaneous adjustment theory: *Lott, Plougonven and Vanneste, JAS 2010, JAS 2012.*

# General Circulation of the Stratosphere and modelisation

## f) Frontal gravity waves parameterization

General setup: A 3D  $(x,y,z)$  PV anomaly advected in a rotating ( $f=\text{cte}$ ), stratified (BV freq  $N=\text{cte}$ ) shear flow (vertical shear  $\Lambda=\text{cte}$ ).



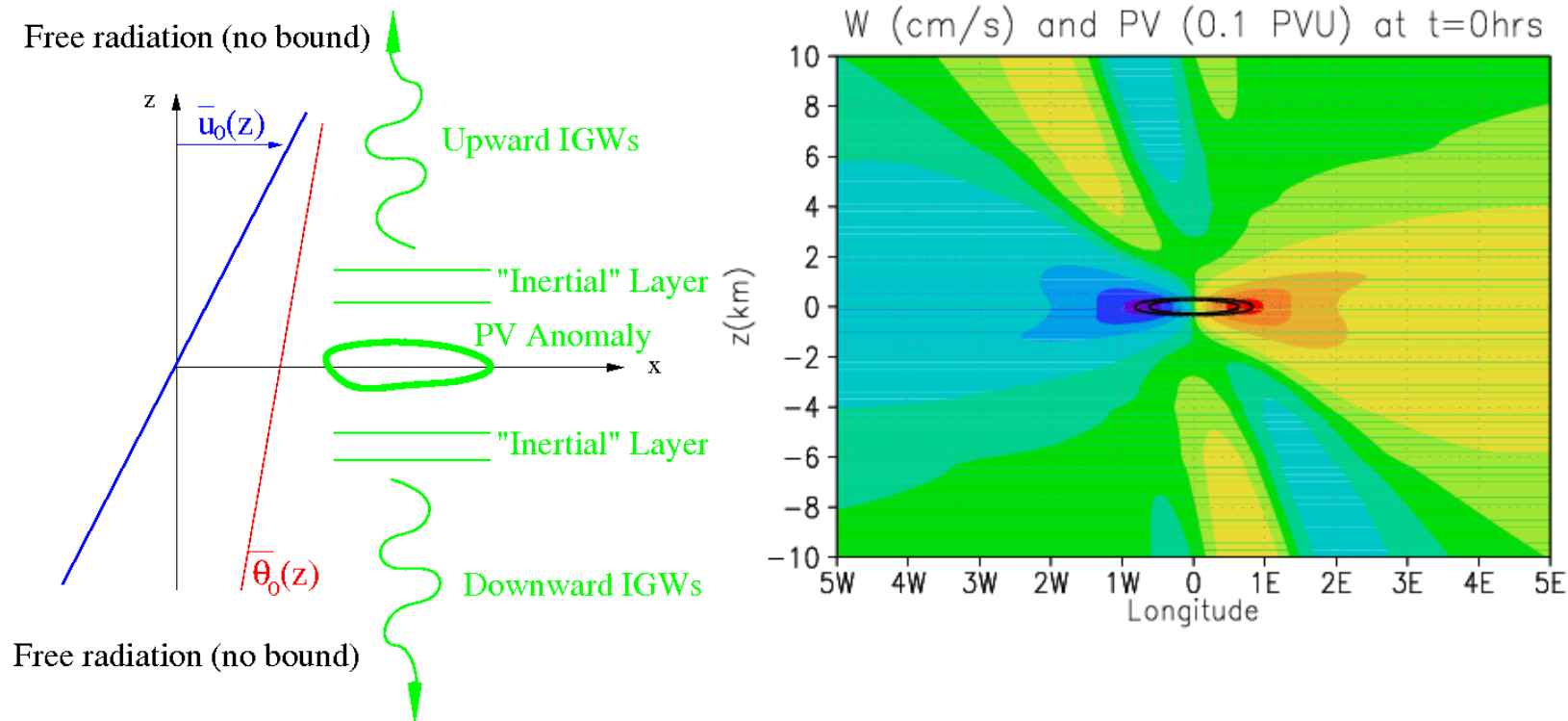
Spontaneous adjustment theory: *Lott, Plougonven and Vanneste, JAS 2010, JAS 2012.*



# General Circulation of the Stratosphere and modelisation

## f) Frontal gravity waves parameterization

General setup: A 3D  $(x,y,z)$  PV anomaly advected in a rotating ( $f=\text{cte}$ ), stratified (BV freq  $N=\text{cte}$ ) shear flow (vertical shear  $\Lambda=\text{cte}$ ).

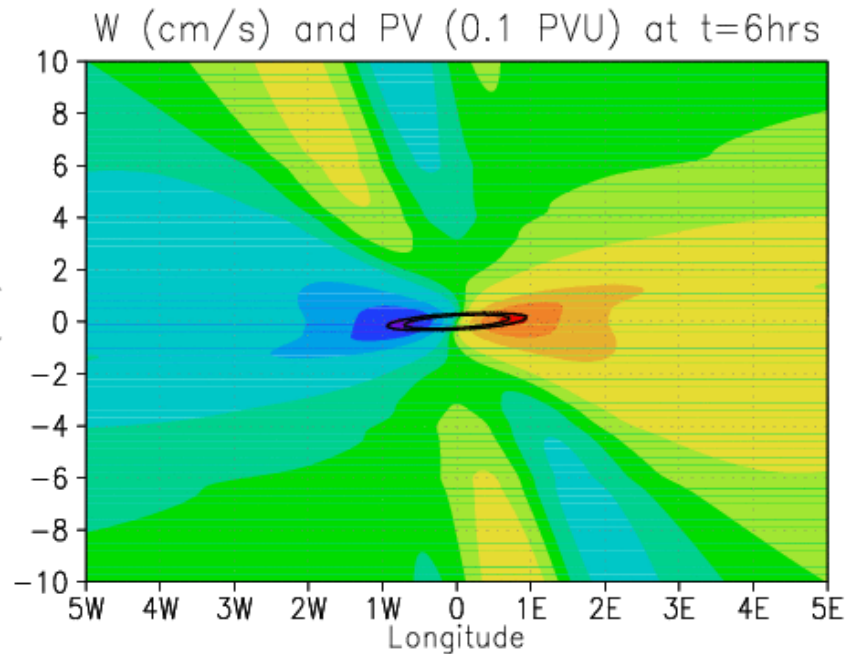
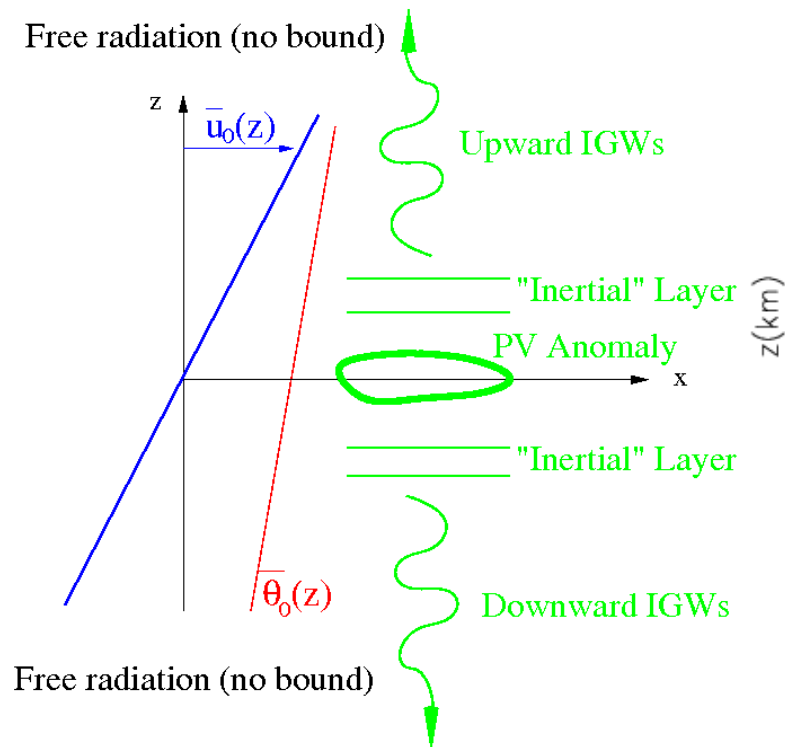


Spontaneous adjustment theory: *Lott, Plougonven and Vanneste, JAS 2010, JAS 2012.*

# General Circulation of the Stratosphere and modelisation

## f) Frontal gravity waves parameterization

General setup: A 3D  $(x,y,z)$  PV anomaly advected in a rotating ( $f=\text{cte}$ ), stratified (BV freq  $N=\text{cte}$ ) shear flow (vertical shear  $\Lambda=\text{cte}$ ).

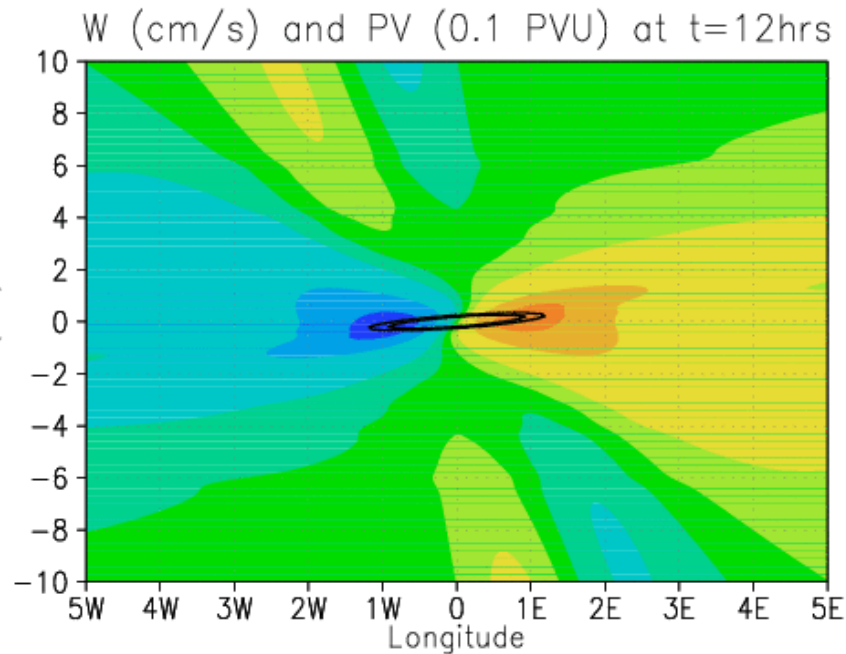
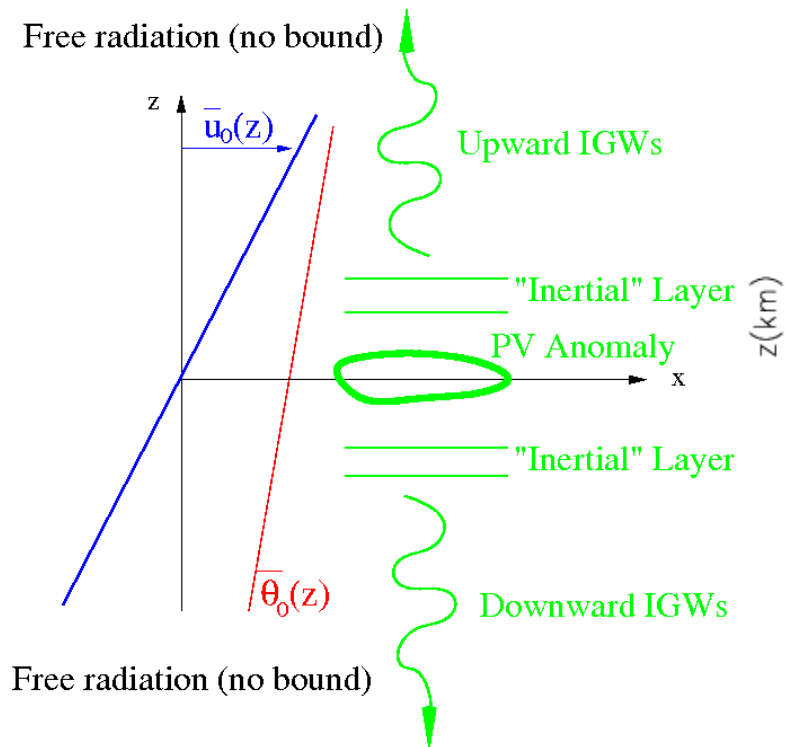


Spontaneous adjustment theory: *Lott, Plougonven and Vanneste, JAS 2010, JAS 2012.*

# General Circulation of the Stratosphere and modelisation

## f) Frontal gravity waves parameterization

General setup: A 3D  $(x,y,z)$  PV anomaly advected in a rotating ( $f=cte$ ), stratified (BV freq  $N=cte$ ) shear flow (vertical shear  $\Lambda=cte$ ).

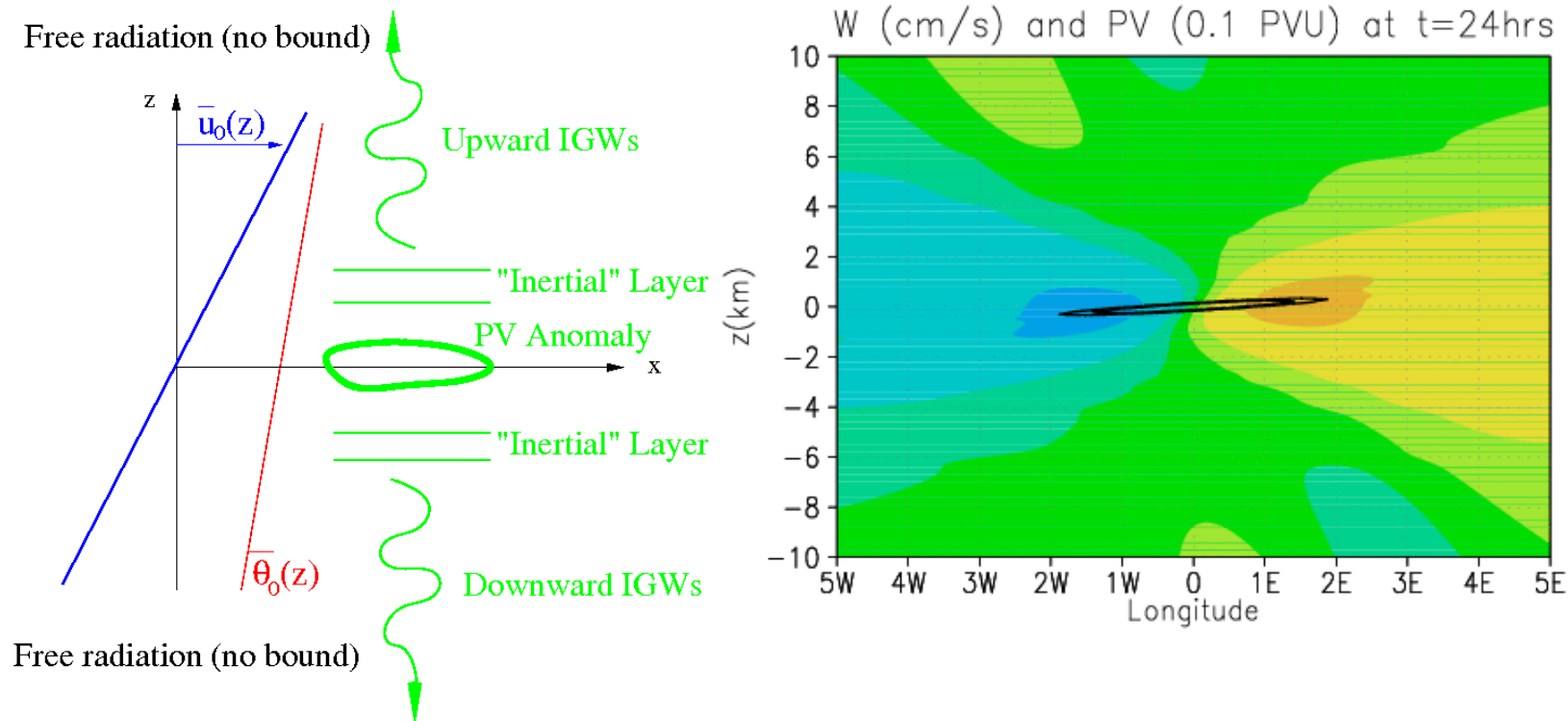


Spontaneous adjustment theory: *Lott, Plougonven and Vanneste, JAS 2010, JAS 2012.*

# General Circulation of the Stratosphere and modelisation

## f) Frontal gravity waves parameterization

General setup: A 3D  $(x,y,z)$  PV anomaly advected in a rotating ( $f=\text{cte}$ ), stratified (BV freq  $N=\text{cte}$ ) shear flow (vertical shear  $\Lambda=\text{cte}$ ).

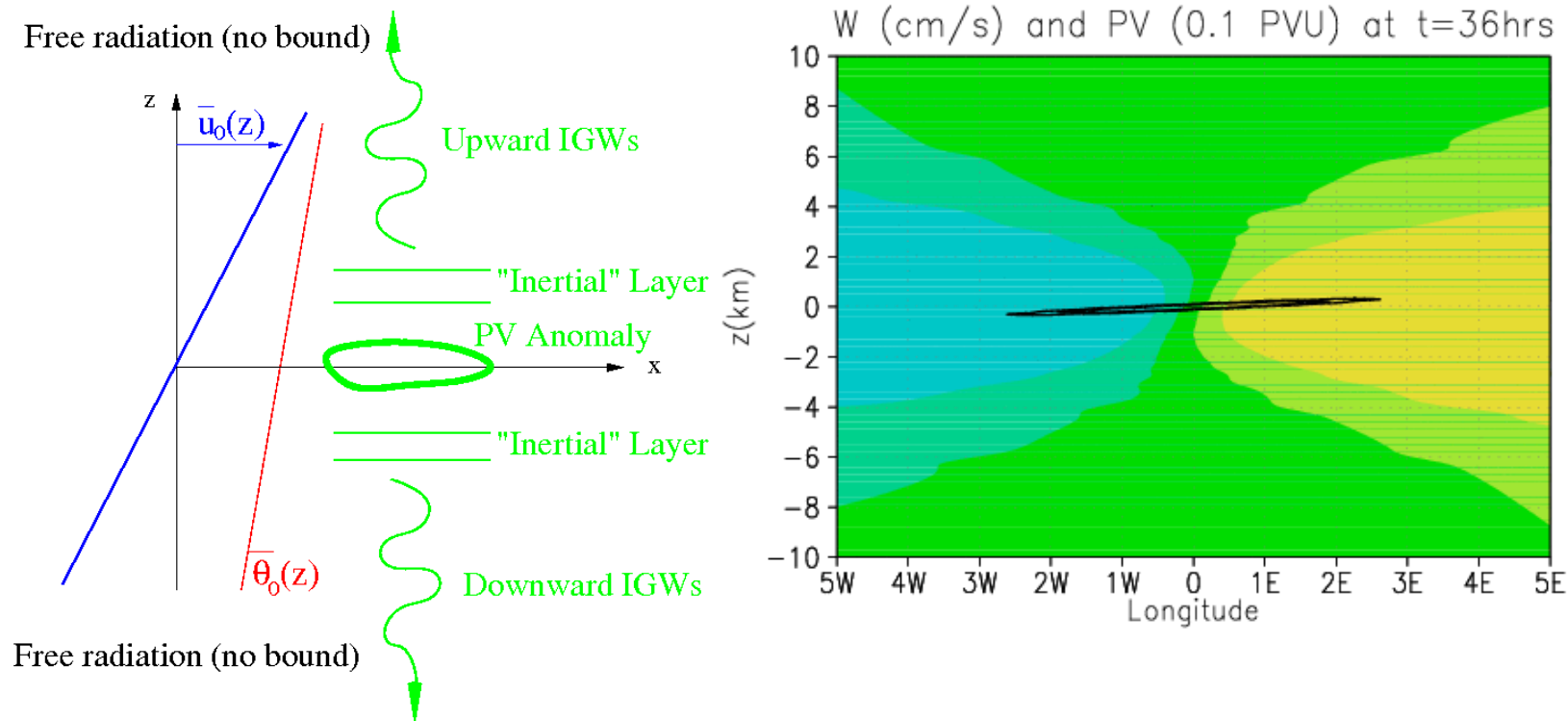


Spontaneous adjustment theory: *Lott, Plougonven and Vanneste, JAS 2010, JAS 2012.*

# General Circulation of the Stratosphere and modelisation

## f) Frontal gravity waves parameterization

General setup: A 3D  $(x,y,z)$  PV anomaly advected in a rotating ( $f=\text{cte}$ ), stratified (BV freq  $N=\text{cte}$ ) shear flow (vertical shear  $\Lambda=\text{cte}$ ).



Spontaneous adjustment theory: *Lott, Plougonven and Vanneste, JAS 2010, JAS 2012.*

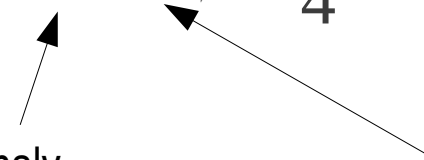


# General Circulation of the Stratosphere and modelisation

## f) Frontal gravity waves parameterization

The wave stress is predictable in closed analytical form:

$$F \approx \frac{\rho g^2}{f \theta^2 N^3} (\rho q' \sigma_z)^2 \frac{e^{-\pi \frac{N}{\Lambda}}}{4}$$



PV anomaly

Characteristic depth of the PV anomaly

Valid for various PV distributions, and over long time scale (compared to the ½ hour interval at which subgrid-scale parameterisation routines are updated)

We next take for the PV  $q$  the GCM gridscale PV anomalies (as a measure of the subgrid scales one, again a “white” spectrum *hypothesis*)

Now it is the subgrid scale vorticity which is considered as a “white” stochastic series:

$$q' = \sum_{n=1}^{\infty} C_n q_n' \quad \text{where} \quad q_n' = \Re \left[ \hat{q}_n e^{i(\vec{k}_n \cdot \vec{x} - \omega_n t)} \right] \quad \text{taking} \quad |\hat{q}_n| = |q_r|$$

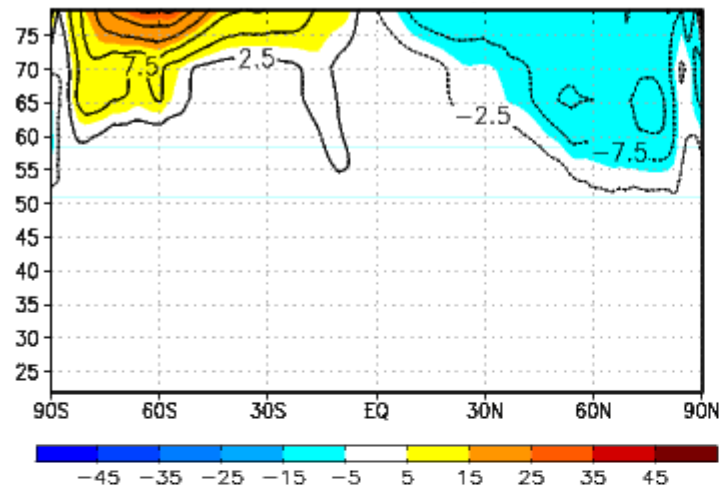
For  $\sigma_z$  the GCM's layer depth, stochastic treatment of the  $k$ 's,  $\omega$ 's, ect...

# General Circulation of the Stratosphere and modelisation

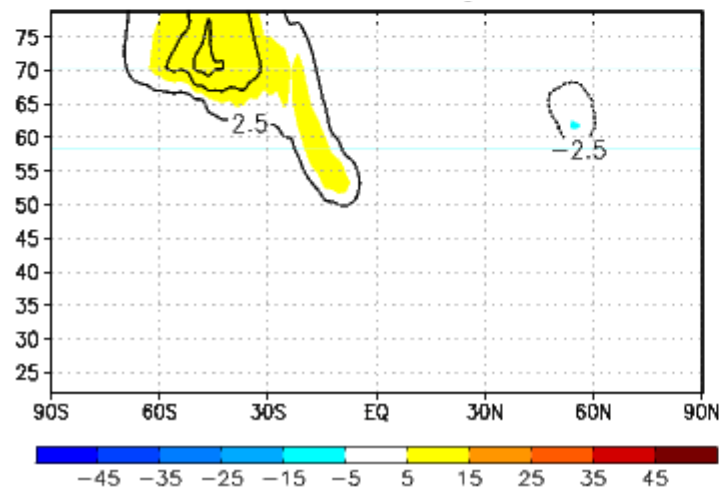
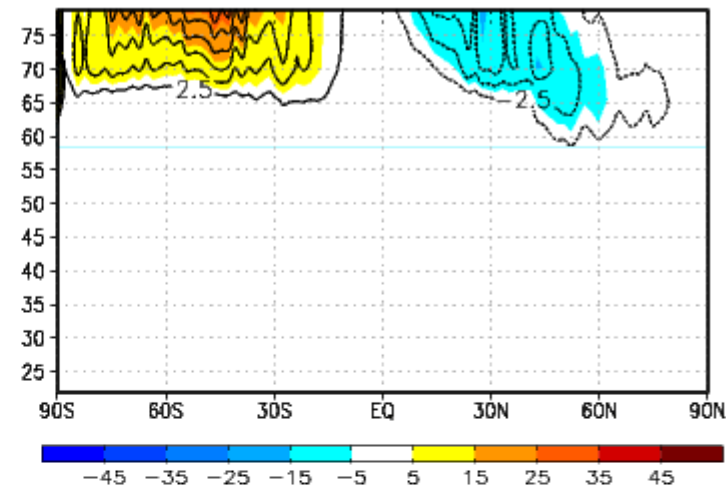
## f) Frontal gravity waves parameterization

The “smoking gun” theory predicts about the right amount of drag compared to a highly tuned globally spectral scheme (January, all in m/s/day)

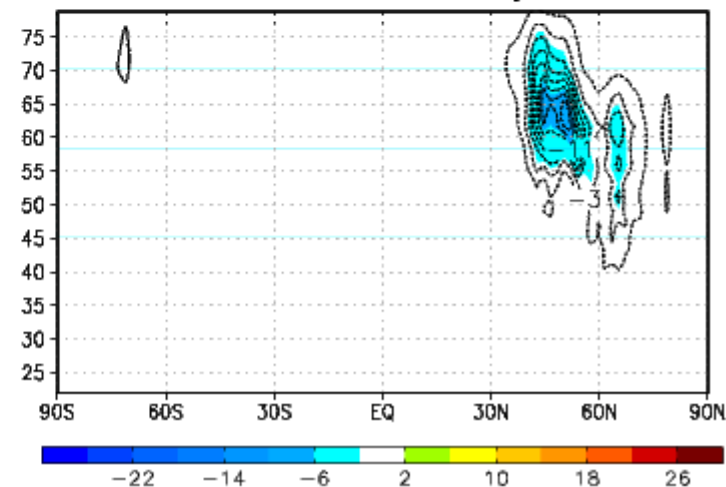
Globally spectral scheme



Smoking fronts



Convective GWs



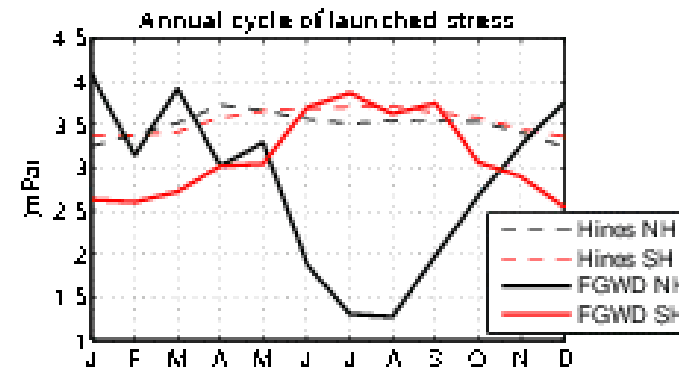
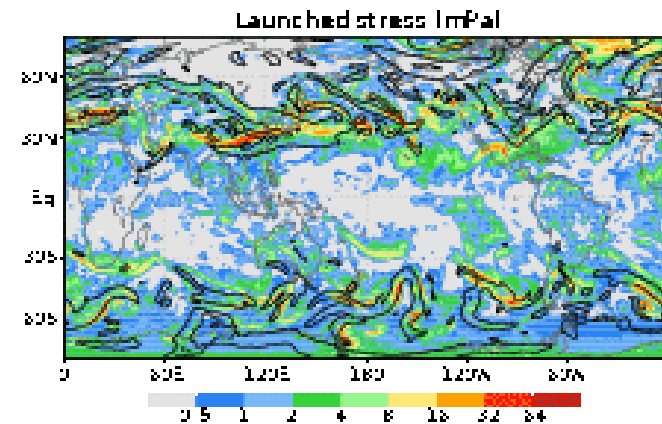
Mountains GWs

# General Circulation of the Stratosphere and modelisation

## f) Frontal gravity waves parameterization

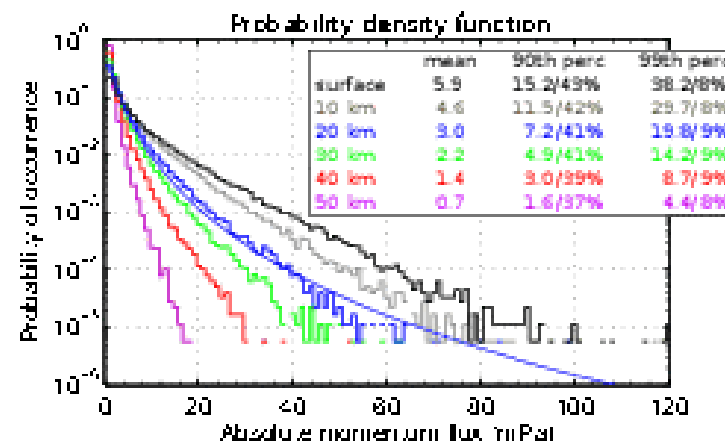
Launched GWs stress amplitude, and  
 $\|\nabla T\|$  at 600hPa:

The waves predicted come from frontal  
 zones



The wave stress  
 now has an annual  
 Cycle...

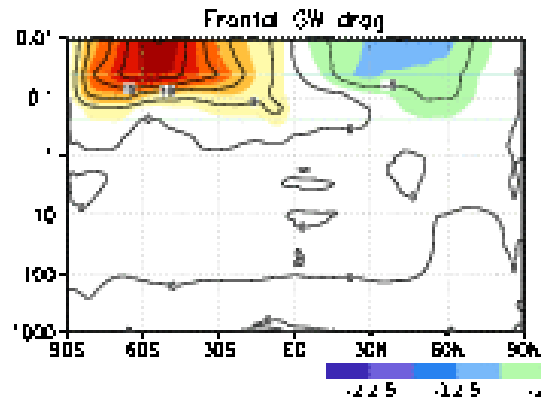
and realistic intermittency



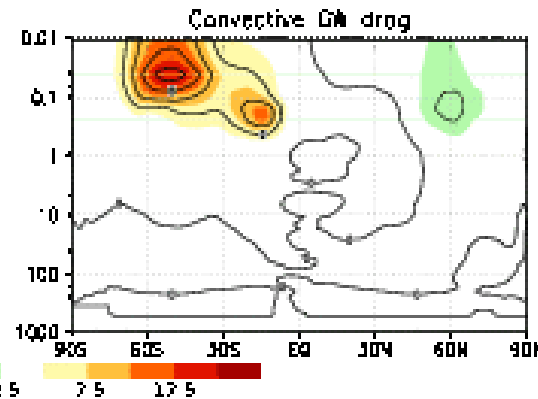
# General Circulation of the Stratosphere and modelisation

## f) Frontal gravity waves parameterization

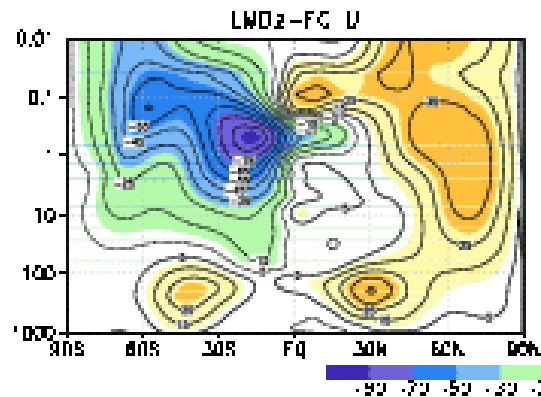
Frontal GWs drag



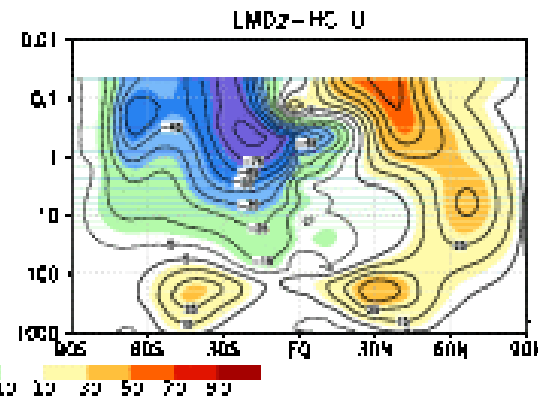
Convective GWs drag



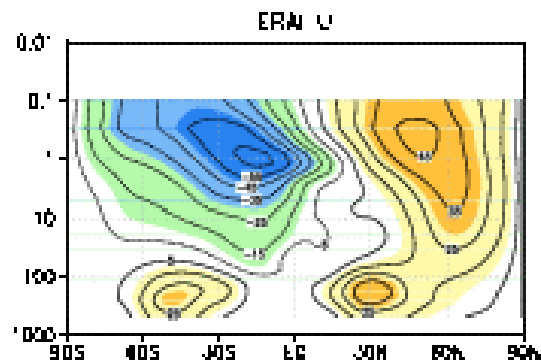
Run with Hines  
+  
Convective waves



Frontal + Convective  
Stochastic GWs



ERA



On line test with LMDz GCM  
(de la Camara and Lott 2015)

# General Circulation of the Stratosphere and modelisation

## f) Frontal gravity waves parameterization

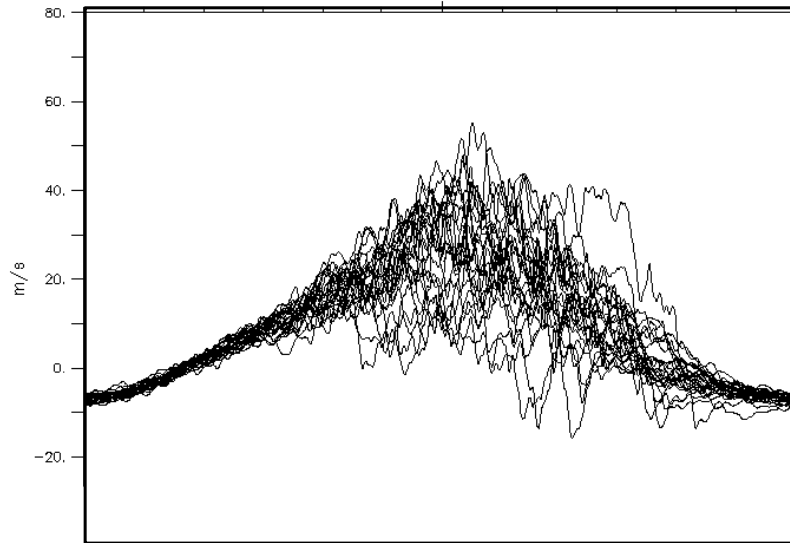
His the stronger GWs annual cycle impact the GCM's annual cycle?

U at 30hPA

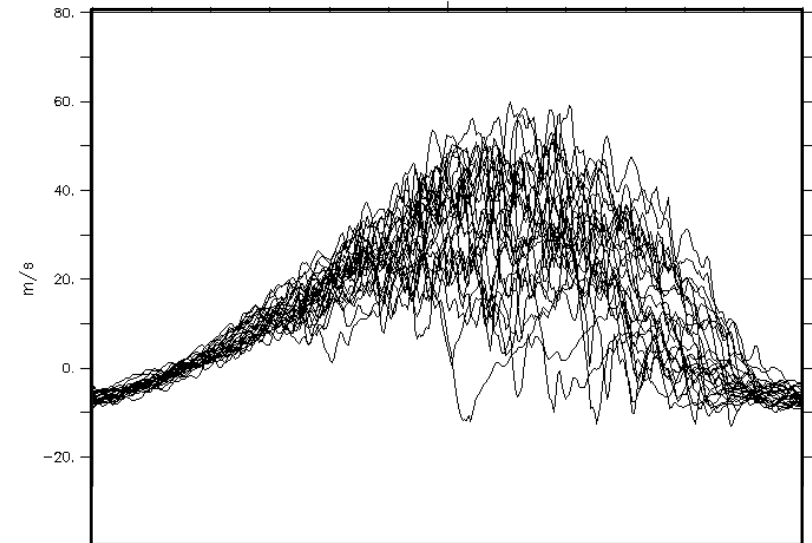
ERA-Interim 1980-2005

LMDz toward CMIP6

NH  
60°N

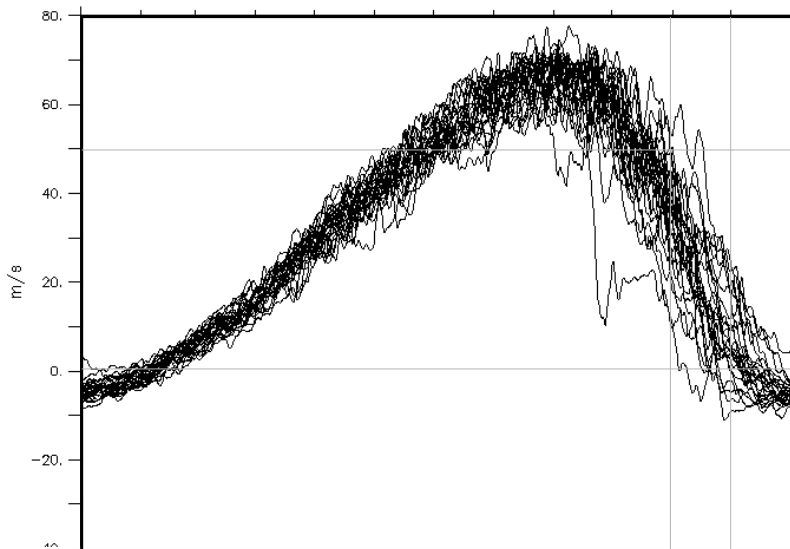


JUL AUG SEP OCT NOV DEC JAN FEB MAR APR MAY JUN

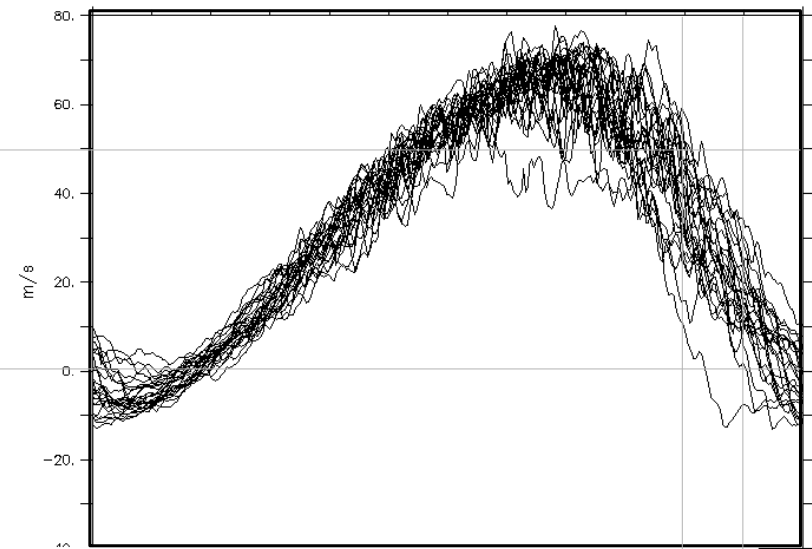


JUL AUG SEP OCT NOV DEC JAN FEB MAR APR MAY JUN

SH  
60°S



JAN FEB MAR APR MAY JUN JUL AUG SEP OCT NOV DEC



JAN FEB MAR APR MAY JUN JUL AUG SEP OCT NOV DEC



# General Circulation of the Stratosphere and modelisation Perspectives

Will this physically based stochastic approaches increase the spread of climate Simulations?

For instance via an improvement of the year to year variability of the SH stratospheric winter vortex breakdown?

Now that the GWs are tied to the tropospheric weather, we can address their contribution to the climate change in the middle atmosphere

Does our unbalanced responses to upper-level PV anomalies modify the triggering of surface synoptic waves?

Extent stochastic methods to mountain waves?