Atmosphere-surface coupling in LMDZ

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Technical note : Description of the interface with the surface and the computation of the turbulent diffusion in LMDZ
http://www.lmd.jussieu.fr/~jldufres/publi/pbl_surface.pdf

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Atmosphere-surface interactions

The **atmosphere and the surface are coupled** through *turbulent diffusion* (in boundary layer) and *radiation* (SW and LW). Currently, there are no direct influence of the surface to other parametrizations.

The surface impacts the atmosphere via the orography (factors constant with time)

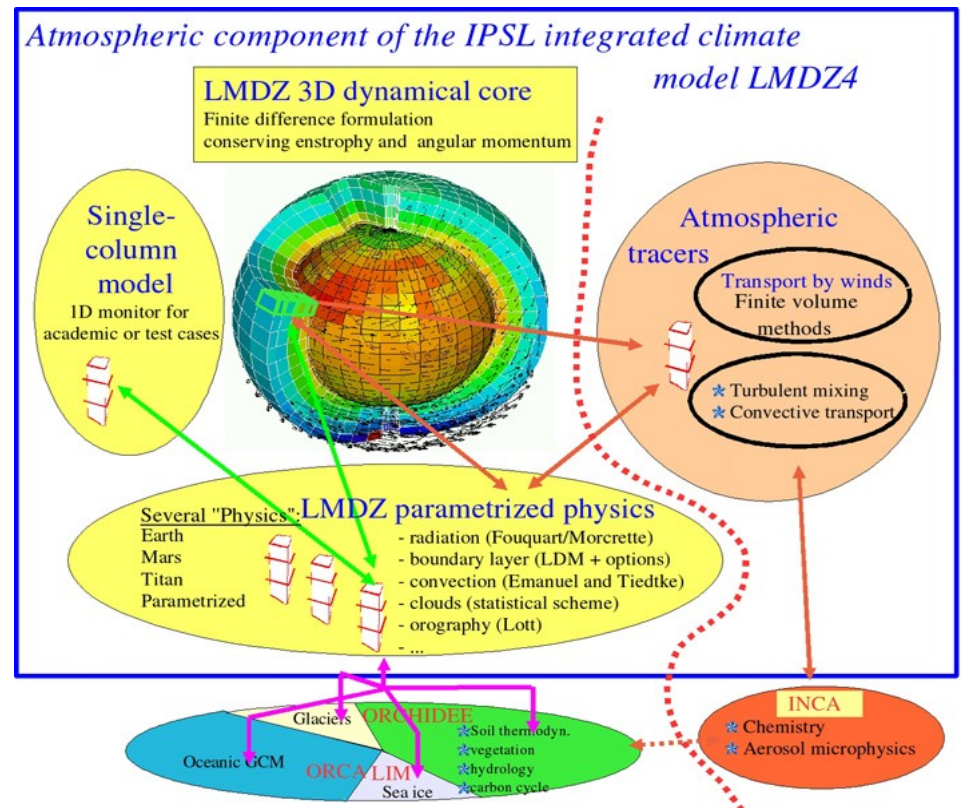The surface "receive" precipitation from the atmosphere (no direct feedback).

In LMDZ:

Each surface grid may be decomposed in a maximum of 4 sub-grids of different types: land (_ter), continental ice (_lic), open ocean (_oce), sea-ice (_sic)

Radiation depends only on mean surface properties

Turbulent diffusion depends on local sub-grid property

No influence of sub-surface properties to any other parameterization.

Atmospheric component of the IPSL integrated climate
model LMDZ4

LMDZ 3D dynamical core
Finite difference formulation
conserving enstrophy and angular momentum

Single-column model
1D monitor for academic or test cases

Atmospheric tracers

Transport by winds
Finite volume methods

* Turbulent mixing
* Convective transport

Several "Physics":   LMDZ parametrized physics
Earth   - radiation (Fouquart/Morcrette)
Mars   - boundary layer (LDM + options)
Titan   - convection (Emanuel and Tiedtke)
Parametrized   - clouds (statistical scheme)
                                   - orography (Lott)
                                   - ...

Glaciers ORCHIDEE
Oceanic GCM   *Soil thermodyn.
                       *vegetation
ORCA LIM   *hydrology
Sea ice   *carbon cycle

INCA
* Chemistry
* Aerosol microphysics

Turbulent diffusion

The change of a variable X with time due to vertical diffusion is:

$$\rho \partial_t X = -\partial_z \phi \tag{8}$$

where ρ is the volumic mass ($kg.m^{-3}$). Variable X can be the specific humidity, moist static energy, momentum, tracer.... ϕ is the flux of X and is defined as:

$$\phi = -\rho k_z \partial_z X \tag{9}$$

with k_z is the diffusion coefficient ($m^2.s^{-1}$).

Space discretization. We consider n layers from $l = 1$ (surface) to $l = n$ (top of atmosphere, TOA) and $n+1$ interfaces from $l = 1$ (surface) to $l = n+1$ (TOA). The space discretization of above equations gives

$$m_l \partial_t X_l = \phi_l - \phi_{l+1} \tag{10}$$
$$\phi_l = K_l(X_{l-1} - X_l) \tag{11}$$

with X_l average value of X for layer l, m_l mass per unit surface ($kg.m^{-2}$) of layer l, ϕ_l flux at interface l and

$$K_l = -\frac{k_z \rho^2 g}{P_l - P_{l-1}} \tag{12}$$

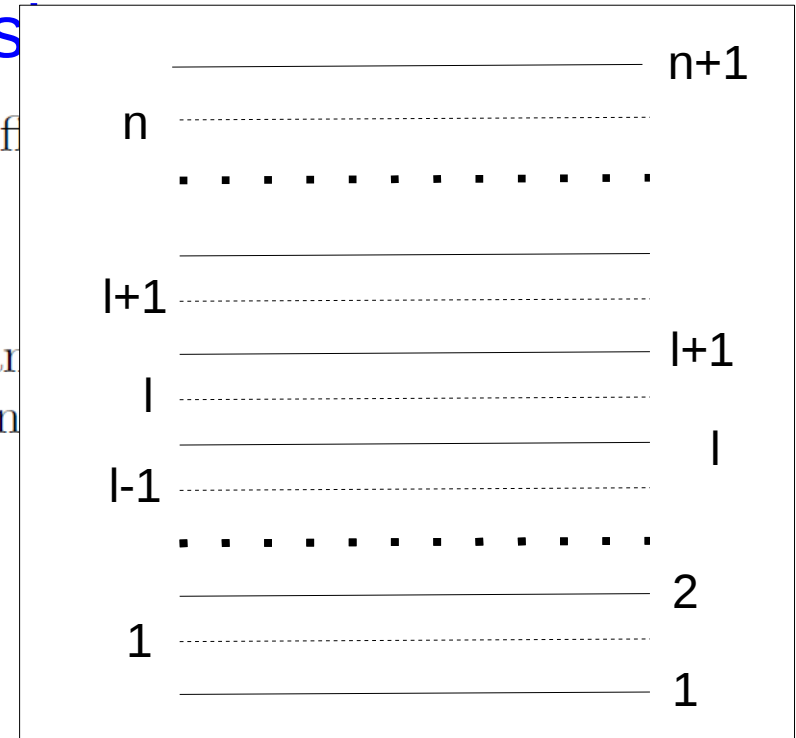with P_l pressure at interface l.

Turbulent diffus[...]

The change of a variable X with time due to vertical dif[...]

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Turbulent diffusion

$$m_l \partial_t X_l = \phi_l - \phi_{l+1}$$
$$\phi_l = K_l(X_{l-1} - X_l)$$

Time discretization. We use an implicit scheme:

$$m_l \frac{X_l(t + \delta t) - X_l(t)}{\delta t} = \phi_l(t + \delta t) - \phi_{l+1}(t + \delta t)$$

$$m_l \frac{X_l - X_l^0}{\delta t} = \phi_l - \phi_{l+1}$$
$$= K_{l+1}(X_{l+1} - X_l) - K_l(X_l - X_{l-1})$$

with : $X_l = X_l(t + \delta t)$ and $X_l^0 = X_l(t)$.

$$\left(\frac{m_l}{\delta t} + K_{l+1} + K_l\right) X_l = \frac{m_l}{\delta t} X_l^0 + K_{l+1} X_{l+1} + K_l X_{l-1}$$

Tridiagonal system that can be solved for vector X

$$-K_l X_{l-1} + \left(\frac{m_l}{\delta t} + K_{l+1} + K_l\right) X_l + K_{l+1} X_{l+1} = \frac{m_l}{\delta t} X_l^0$$

Solving the tridiagonal system

$$\left(\frac{m_l}{\delta t} + K_{l+1} + K_l\right) X_l = \frac{m_l}{\delta t} X_l^0 + K_{l+1} X_{l+1} + K_l X_{l-1}$$

which may be written as:

$$\left(\delta P_l + R_{l+1}^X + R_l^X\right) X_l = \delta P_l \, X_l^0 + R_{l+1}^X \, X_{l+1} + R_l^X \, X_{l-1} \quad (2 \leq l < n)$$

$$\text{with } R_l^X = g\delta t K_l$$

At the top

$$\left(\delta P_n + R_n^X\right) X_n = \delta P_n \, X_n^0 + R_n^X \, X_{n-1}$$

At the bottom

$$\left(\delta P_1 + R_1^X\right) X_1 = \delta P_1 \, X_1^0 + R_2^X \, X_2 - g\delta t F_1^X$$

With F_1^X : flux of X at the bottom of the first layer (i.e. between the surface and the atmosphere)

Solving the tridiagonal system

Starting from top:

$$\left(\delta P_n + R_n^X\right) X_n = \delta P_n \, X_n^0 + R_n^X \, X_{n-1}$$

can be written as:

$$X_n = C_n^X + D_n^X X_{n-1}$$

with

$$C_n^X = \frac{X_n^0 \delta P_n}{\delta P_n + R_n^X}$$

$$D_n^X = \frac{R_n^X}{\delta P_n + R_n^X}$$

Solving the tridiagonal system

$$X_{l+1} = C_{l+1}^X + D_{l+1}^X X_l$$

$$\left(\delta P_l + R_{l+1}^X + R_l^X\right) X_l = \delta P_l\, X_l^0 + R_{l+1}^X\, X_{l+1} + R_l^X\, X_{l-1} \quad (2 \leq l < n)$$

$$\left(\delta P_l + R_{l+1}^X\left(1 - D_{l+1}^X\right) + R_l^X\right) X_l = \delta P_l\, X_l^0 + R_{l+1}^X\, C_{l+1}^X + R_l^X\, X_{l-1}$$

So we obtain by reccurence:

$$X_l = C_l^X + D_l^X X_{l-1} \qquad (2 \leq l \leq n)$$

with, for $(2 \leq l < n)$

$$C_l^X = \frac{X_l^0 \delta P_l + R_{l+1}^X C_{l+1}^X}{\delta P_l + R_l^X + R_{l+1}^X (1 - D_{l+1}^X)}$$

$$D_l^X = \frac{R_l^X}{\delta P_l + R_l^X + R_{l+1}^X (1 - D_{l+1}^X)}$$

Solving the tridiagonal system

At the bottom of the boundary layer

$$X_2 = C_2^X + D_2^X X_1$$

$$\left(\delta P_1 + R_2^X\right) X_1 = \delta P_1 \, X_1^0 + R_2^X \, X_2 - g\delta t F_1^X$$

replacing X_2 in the equation above:

$$\boxed{X_1 = A_1^X + B_1^X . F_1^X . \delta t}$$

with

$$A_1^X = \frac{X_1^0 \delta P_1 + R_2^X C_2^X}{\delta P_1 + R_2^X (1 - D_2^X)}$$

$$B_1^X = \frac{-g}{\delta P_1 + R_2^X (1 - D_2^X)}$$

If F_1 is known, then X_1 and all other X_l are knwon, and also the flux Φ_l

boundary layer:

$$X_1 = f(F_1^X)$$

exchange with surface:

$$F_1^X = g(X_1, X_s) \Rightarrow F_1^X = g(f(X_1), X_s) \Rightarrow F_1^X = \hat{g}(X_s)$$

energy budget at surface:

$$X_s = h(F_1^X) \Rightarrow X_s = h(\hat{g}(X_s)) \Rightarrow X_s = \ldots$$

Coupling with the surface

Equation for the variables of the first layer

$$X_1 = A_1^X + B_1^X . F_1^X . \delta t$$

Sensitivity of X_1 to the flux at surface F_1

Value if the flux $F_1 = 0$

X: temperature T, humidity q, velocity Vx and Vy
F^X: Flux of heat, flux of water mass or flux of momentum

Typical expression of the flux with the surface
$F_1 = K_1 (T_1 - T_s)$

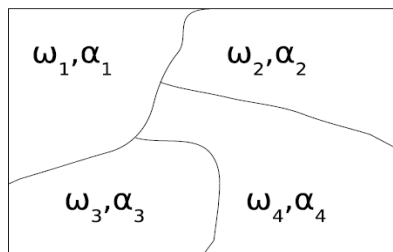Each surface model has to compute the flux F_1 using variables X_1, A_1 and B_1

In LMDZ, the turbulent flux are computed separately over each sub-surface type

Coupling between atmospheric column(s) and sub-surfaces

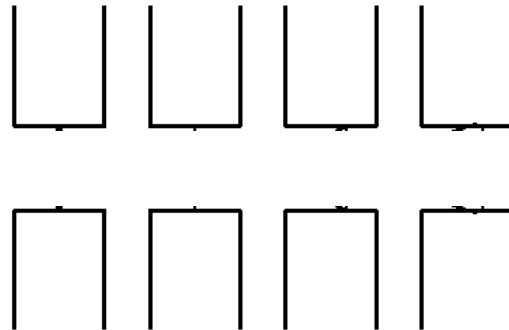Each grid cell is divided into several sub-areas or ``sub-surfaces'' of fractions ω_i

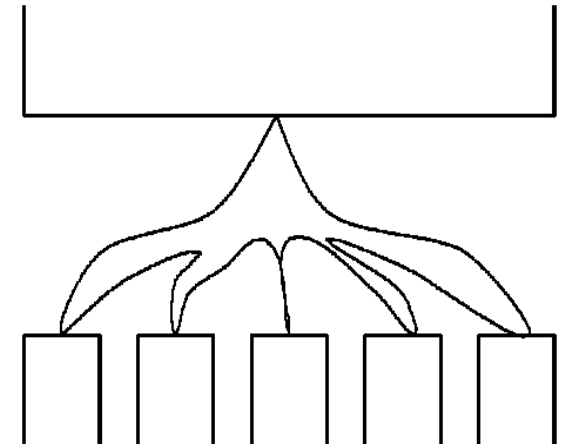| Sub-surfaces	Turbulent flux	Radiative flux
$\sum_i \omega_i = 1$	One PBL over **each** sub-surface	One column **covers** **all** the sub-surface

Derivation of local sub-surface **net solar radiation** from grid average net solar radiation

The grid average net flux Ψ_s at surface has been computed for each grid point by the radiative code.

We want (1) to conserve energy and (2) to take into account the value of the local albedo α_i of the sub-surface.

We compute the downward SW radiation as $\quad F_\downarrow^s = \dfrac{\Psi_s}{(1-\alpha)}$

with the mean albedo $\quad \alpha = \sum_i \omega_i \alpha_i$

For each sub-surface, the absorbed solar radiation reads: $\quad \psi_i^s = (1-\alpha_i) F_\downarrow^s$

$$\boxed{\psi_i^s = \frac{(1-\alpha_i)}{(1-\alpha)} \bar{\Psi}^s}$$

One may verified that this procedure ensure energy conservation, i.e. $\quad \sum_i \omega_i \psi_i^s = \Psi_s$

Derivation of local sub-surface **net longwave radiation** from grid average net longwave radiation

The net longwave (LW) radiation $\bar{\Psi}^L$ has been computed by the radiative code for each grid cell. How to split it depending on the sub-surfaces local properties and ensuring energy conservation?

If the downward longwave flux $F_\downarrow$ is uniform within each grid, the net LW flux for a sub-surface i may be written as:

$$\psi_i^L(T_i) = \epsilon_i \left(F_\downarrow - \sigma T_i^4 \right) \tag{1}$$

where T_i is the surface temperature of sub-surface i and ϵ_i its emissivity. A linearization around the mean temperature $\bar{T}$ gives:

$$\psi_i^L(T_i) \approx \epsilon_i \left(F_\downarrow - \sigma \bar{T}^4 \right) - 4\epsilon_i \sigma \bar{T}^3 (T_i - \bar{T}) \tag{2}$$

To conserve the energy, the following relationship must be true:

$$\sum_i \omega_i \psi_i^L = \bar{\Psi}^L \tag{3}$$

Using Eq. 2 gives

$$\sum_i \omega_i \psi_i^L = \bar{\epsilon} \left(F_\downarrow - \sigma \bar{T}^4 \right) - 4\sigma \bar{T}^3 \sum_i \omega_i \epsilon_i \left(T_i - \bar{T} \right) \tag{4}$$

where $\bar{\epsilon} = \sum_i \omega_i \epsilon_i$ is the mean emissity.

Derivation of local sub-surface **net longwave radiation** from grid average net longwave radiation

$$\sum_i \omega_i \psi_i^L = \bar{\epsilon}\left(F_\downarrow - \sigma\bar{T}^4\right) - 4\sigma\bar{T}^3 \sum_i \omega_i \epsilon_i \left(T_i - \bar{T}\right) \tag{4}$$

where $\bar{\epsilon} = \sum_i \omega_i \epsilon_i$ is the mean emissity. The second term on the right hand side is zero if

$$\bar{T} = \frac{\sum_i \omega_i \epsilon_i T_i}{\bar{\epsilon}} \tag{5}$$

To ensure energy conservation, we need in addition to verify:

$$\bar{\Psi}^L = \bar{\epsilon}\left(F_\downarrow - \sigma\bar{T}^4\right) \tag{6}$$

Which is consistent with the definition of the net LW flux at the surface. We rewrite now Eq. 2 as:

$$\psi_i^L(T_i) \approx \frac{\epsilon_i}{\bar{\epsilon}}\bar{\Psi}^L - 4\epsilon_i\sigma\bar{T}^3(T_i - \bar{T}) \tag{7}$$

Due to radiative code limitation, in LMDZ, we always must have $\epsilon_i = 1$

Call tree

In subroutine PHYSIQ
loop over time steps
CALL change_srf_frac : Update fraction of the sub-surfaces (pctsrf)
....
CALL pbl_surface Main subroutine for the interface with surface
  Calculate net radiation at sub-surface
  Loop over the sub-surfaces nsrf
    Compress variables (Consider only one surface type and only the points for which the fraction for this sub-surface in not zero)
    CALL clcdrag: coefficients for turbulent diffusion at surface (cdragh and cdragm)
    CALL coef_diff_turb: coef. turbulent dif. in the atmosphere (ycoefm et ycoefm.)
    CALL climb_hq_down downhill for henthalpie H and humidity Q
    CALL climb_wind_down downhill for wing (U and V)
    CALL surface models for the various surface types: **surf_land, surf_landice, surf_ocean or surf_seaice**. **Each surface model computes:**
    • evaporation, latent heat flux, sensible heat flux
    • surface temperature, albedo
    CALL climb_hq_up : compute new values of henthalpie H and humidity Q
    CALL climb_wind_up : compute new values of wind (U and V)
    Uncompress variables : (some variables are per unit of sub-surface fraction, some are per unit of grid surface fraction)
    Cumulate in global variables after weighting by sub-surface fractions
    Surface diagnostics : (T2m, Q2m, wind at 10m...)
  End Loop over the sub-surfaces
  Calculate the mean values over all sub-surfaces for some variables
End pbl-surface